

# Energy-Efficient UAV-Aided Computation Offloading on THz Band: A MADRL Solution

Yuanjian Li<sup>1</sup>, A.S. Madhukumar<sup>1</sup>,  
Tan Zheng Hui Ernest<sup>2</sup>, Gan Zheng<sup>3</sup>, Walid Saad<sup>4</sup>, and Hamid Aghvami<sup>5</sup>

**1**, College of Computing and Data Science  
Nanyang Technological University, Singapore

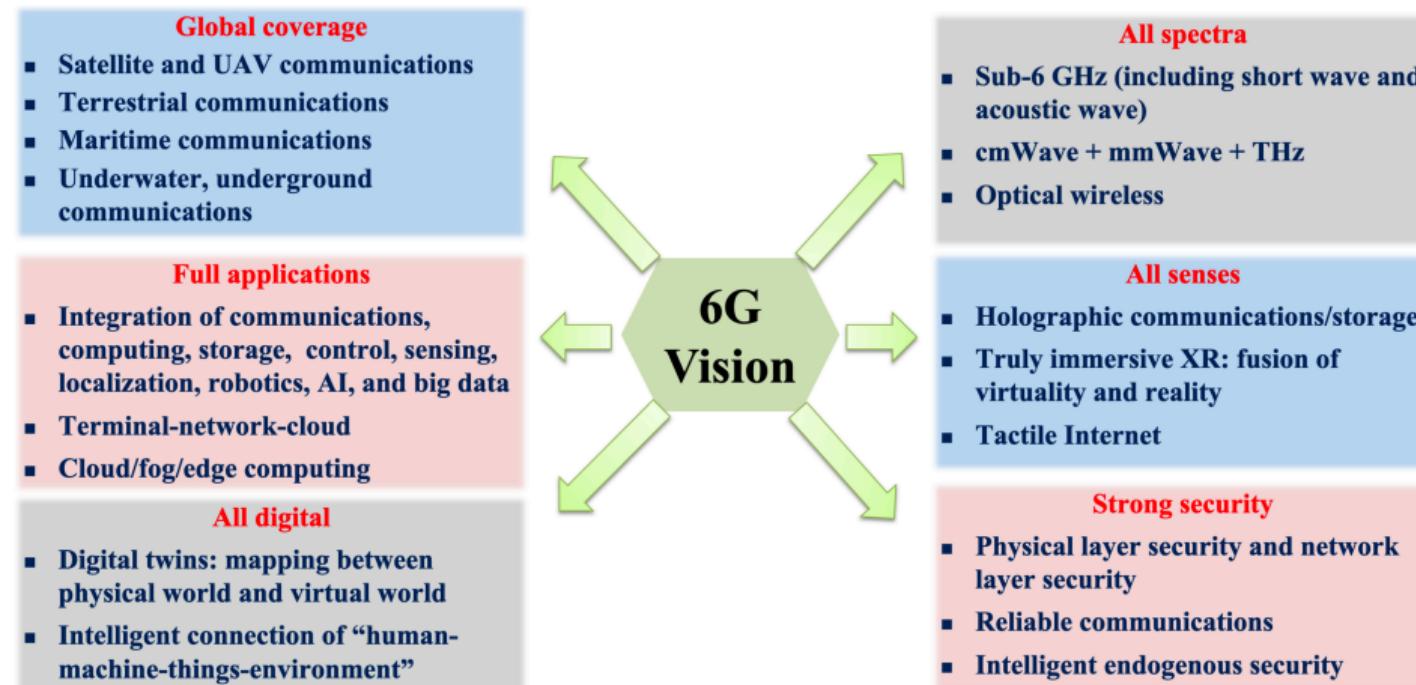
**2**, Agency for Science, Technology and Research, Singapore

**3**, the University of Warwick, the UK

**4**, Virginia Tech, the US

**5**, King's College London, the UK

# The Next-Gen (6G) Wireless Systems



C.-X. Wang, X. You, X. Gao, X. Zhu, Z. Li, C. Zhang, H. Wang, Y. Huang, Y. Chen, H. Haas et al., “On the road to 6G: Visions, requirements, key technologies, and testbeds,” *IEEE Communications Surveys & Tutorials*, vol. 25, no. 2, pp. 905–974, 2023.

# Motivations

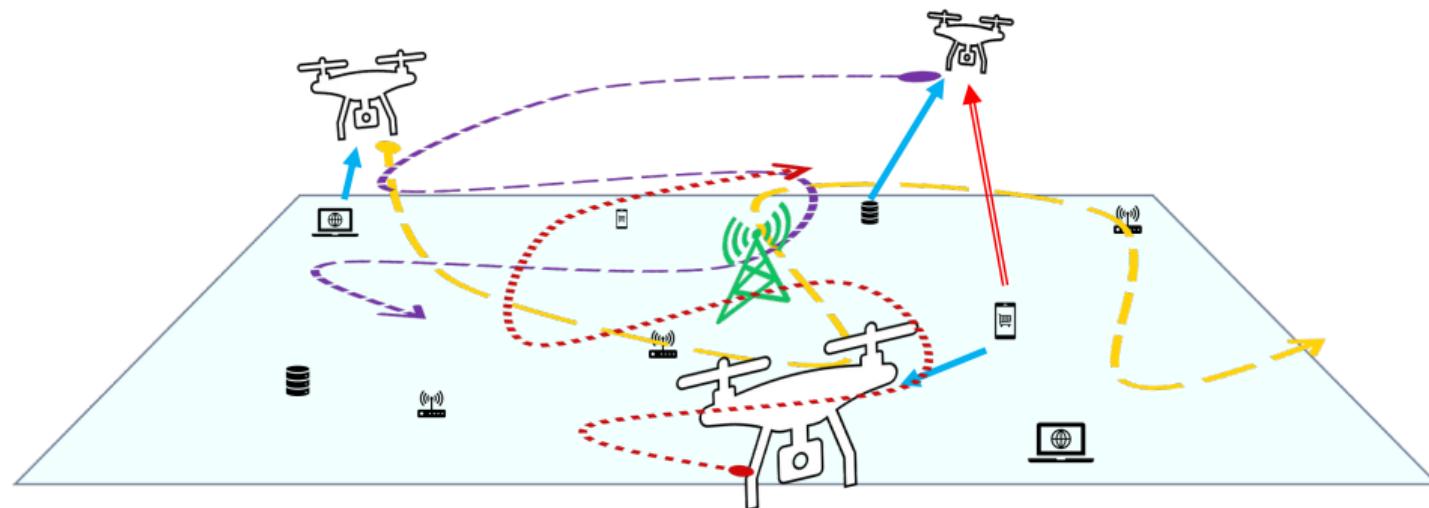
- IoT user equipments (UEs) have **limited power and computing resources**, yet require prolonged operation, emphasizing **energy efficiency**.
- **THz technology** enables **low-latency** and **high data rate** multi-access edge computing (MEC) services, such as task offloading.
- **UAV-aided MEC on THz** mitigates propagation limits, blockages, and coverage issues by leveraging UAVs' **mobility** and short-range **LoS links**.

## Contributions

- **The Gap:** Limited research exists on energy-efficient UAV-aided MEC systems operating on the THz band.
- **The Difficulty:** AI-native solutions for adapting to dynamic wireless environments remain inherently challenging and lacking.
- **Core Contribution:** This work addresses the gap by proposing an AI-native algorithm for energy efficiency maximization in UAV-aided MEC networks over the THz band.

# System Model Diagram of Multi-UAV Computation Offloading for Many IoT UEs

Multiple UAVs are deployed to provide multiple energy-limited computation-scarce terrestrial IoT user equipments (UEs) with accessible task offloading services on THz band.



## Key Considerations

To enable energy-efficient multi-UAV-assisted MEC frameworks in IoT, the following challenges must be addressed:

- How to design UAV trajectories to establish high-quality ground-to-air (G2A) links for efficient task offloading in multi-UE scenarios?
- How to jointly optimize communication and computation resources, including transmit power, UAV-UE associations, CPU clock speeds, and time slicing, to enhance system metrics like energy efficiency?
- How to develop an agile multi-agent learning framework capable of handling non-stationarity and dynamically adapting to the challenges of MUME UAV-assisted MEC systems?

## The Energy Efficiency Maximization Problem under Investigation

We seek to maximize expected energy efficiency for multi-UAV multi-UE computation offloading systems over the THz band.

$$\begin{aligned} & \max_{\{\mathbf{v}_u[n], f_g[n], \psi_g^u[n], \tau_g^u[n], P_g[n]\}} \frac{1}{N} \sum_{n=1}^N \frac{d[n]}{E[n]}, \\ \text{s.t. } & (1), (2), (3), (4), (5), (6), (8), (9) \end{aligned}$$

$$\begin{aligned} d[n] &= \sum_{g \in \mathcal{G}} d_g[n] \\ E[n] &= \sum_{g \in \mathcal{G}} E_g[n] + \sum_{u \in \mathcal{U}} (E_u[n] + \Re E_u^p[n]) \end{aligned}$$

We **jointly** optimize communication and computation resources, including:

- ⇒ UAVs' trajectories ( $\mathbf{v}_u[n]$ ),
- ⇒ UEs' local central processing unit (CPU) clock speeds ( $f_g[n]$ ),
- ⇒ UAV-UE associations ( $\psi_g^u[n]$ ),
- ⇒ time slot slicing factor ( $\tau_g^u[n]$ ),
- ⇒ UEs' offloading powers ( $P_g[n]$ ).

## Why AI-Aided Solution?

Solving the formulated multi-dimensional maximization problem with classical optimization techniques, such as game theory or convex optimization, is extremely **difficult** due to the following key challenges:

- **Non-convex objective function:** The objective consists of accumulated fractional functions with multiple summations, making it a non-convex mixed-integer non-linear programming (MINLP) problem that is **NP-hard**.
- **Coupled optimization parameters:** The parameters, including discrete binary variables  $\psi_g^u[n]$ , vector  $\mathbf{v}[n]$ , and ranged floats  $f_g[n]$ ,  $\tau_g^u[n]$ , and  $P_g[n]$ , are intertwined in both the objective and constraints.

# Why AI-Aided Solution?

○ **Non-convex constraints:** Examples include:

- Norm inequality in the mobility constraint,
- Binary index-involved UAV-UE association constraint,
- Time slot allocation constraints.

These lead to high computational and algorithmic overheads.

**Alternative Solution:** An AI-native solution from a data driven perspective, i.e., model-free DRL-aided algorithm, will be proposed to efficiently tackle the formulated optimization problem by training with raw experiences from interactions between DRL agents and the task offloading environment.

# Why Multi-Agent Reinforcement Learning?

- Enables distributed implementation of wireless protocols at the edge.
- Facilitates experience sharing, allowing less-trained agents to learn from more skilled ones.
- Accommodates heterogeneous agents with diverse learning goals and device capabilities.

## Main Difficulties in Solving the Joint Computation and Communication Resource Management Problem

- **High-dimensional spaces:** Continuous state and action spaces cause severe dimensionality challenges.
- **Exploration vs. Exploitation:** Balancing new strategy exploration with exploiting learned policies is complex in infinite action-state spaces.
- **Non-stationarity:** Dynamic environments cause state transitions and rewards to depend on joint actions, with agent behaviors evolving over time.
- **Scalability:** Complexity grows exponentially as the number of agents, e.g., thousands of devices, increases.
- **Sample inefficiency:** Multi-agent learning requires a large number of samples to establish effective policies or equilibria.

# The Proposed MADRL Algorithm

## Algorithm 1: The Proposed DSPAC-MN Solution

```

1 Initialization: Initialize online NNs' layers, as per OWI. Synchronize the
exploratory actor networks and shadow networks via  $\Theta^{p_u} \leftarrow \Theta^{a_u}$ ,
 $\Theta^{a_u^-} \leftarrow \Theta^{a_u}$  and  $\Theta^{c_j^-} \leftarrow \Theta^{c_j}$ . Initialize replay buffer  $\mathcal{B}$  of size  $\mathbf{B}$ 
and the mini-batch sampler  $\mathcal{D}$  of size  $\mathbf{D}$ . Set total training step  $n_t = 0$ ;
2 for  $t \in [1, t_{max}]$  do
    Reset time step  $n = 0$ , UAVs' locations to  $\mathbf{q}_u[n]$  and queues to  $\mathcal{Q}_g[n] =$ 
     $0$ , then the current state  $s[n] = \{\mathbf{q}_u[n], \mathcal{Q}_g[n]\}$  is generated;
    repeat
        Perturb each exploratory actor via  $\Theta^{p_u} \leftarrow \Theta^{a_u} + \Theta^p$ ;
        Each UAV observes  $s[n]$  and outputs  $a_u[n] = \pi_u(s[n]|\Theta^{p_u}) +$ 
         $\mathbf{N}$ , then the joint action  $\mathbf{a}[n] = [a_u[n]]_{u \in \mathcal{U}}$  is formulated;
        Execute the joint action  $\mathbf{a}[n]$ , observe the next state  $s[n+1]$  and
        receive the immediate common reward  $r[n]$ ;
        if  $|\mathcal{B}| \geq \mathbf{B}$  then
            Archive experience  $\langle s[n], \mathbf{a}[n], s[n+1], r[n] \rangle$  into  $\mathcal{B}$ ;
        else
            Replace the earliest stored experiences in  $\mathcal{B}$  with the new
            transition  $\langle s[n], \mathbf{a}[n], s[n+1], r[n] \rangle$ ;
        if  $|\mathcal{B}| \geq \mathbf{D}$  then
            Randomly sample a mini-batch of size  $\mathbf{D}$  from  $\mathcal{B}$  into  $\mathcal{D}$ , i.e.,
             $(s_m, \mathbf{a}_m, s_{m+1}, r_m) \in \mathcal{D} \sim \mathcal{B}$ ;
            for  $u \in \mathcal{U}$  do
                The shadow actor outputs  $\pi_u(s_{m+1}|\Theta^{a_u^-}) + \mathbf{N}^-$  to
                calculate the target Q value;
                Update the dual online critics' trainable parameters  $\Theta^{c_j}$  by
                batch gradient descent on MSE loss  $\ell(\Theta^{c_j})$  in (17);
                Increment the total training step  $n_t \leftarrow n_t + 1$ ;
                if  $n_t \% N_s == 0$  then
                    for  $u \in \mathcal{U}$  do
                        The online actor generates  $\pi_u(s_m|\Theta^{a_u})$ ;
                        Update all the online actors' tunable parameters  $\Theta^{a_u}$  by
                        batch gradient ascent by the chain rule as per (19);
                        Update shadow networks  $\Theta^{a_u} \leftarrow \tau_s \Theta^{a_u} + (1 - \tau_s) \Theta^{a_u^-}$ 
                        and  $\Theta^{c_j^-} \leftarrow \tau_s \Theta^{c_j} + (1 - \tau_s) \Theta^{c_j^-}$ ;
                    Trigger time step incrementation  $n \leftarrow n + 1$ ;
                    until  $\|\mathbf{q}_u - \mathbf{q}_{u'}\|_{\{u' \in \mathcal{U} \setminus u\}} < D$ ,  $\exists u, \exists u' \mid \mathbf{q}_u(n) \neq \mathbf{q}_{u'}(n)$   $\mid n = N_{max}$ ;
    
```

## Update the trainable parameters of the critics:

$$\Theta^{c_j} \leftarrow \Theta^{c_j} - \alpha_c \nabla_{\Theta^{c_j}} \ell(\Theta^{c_j}),$$

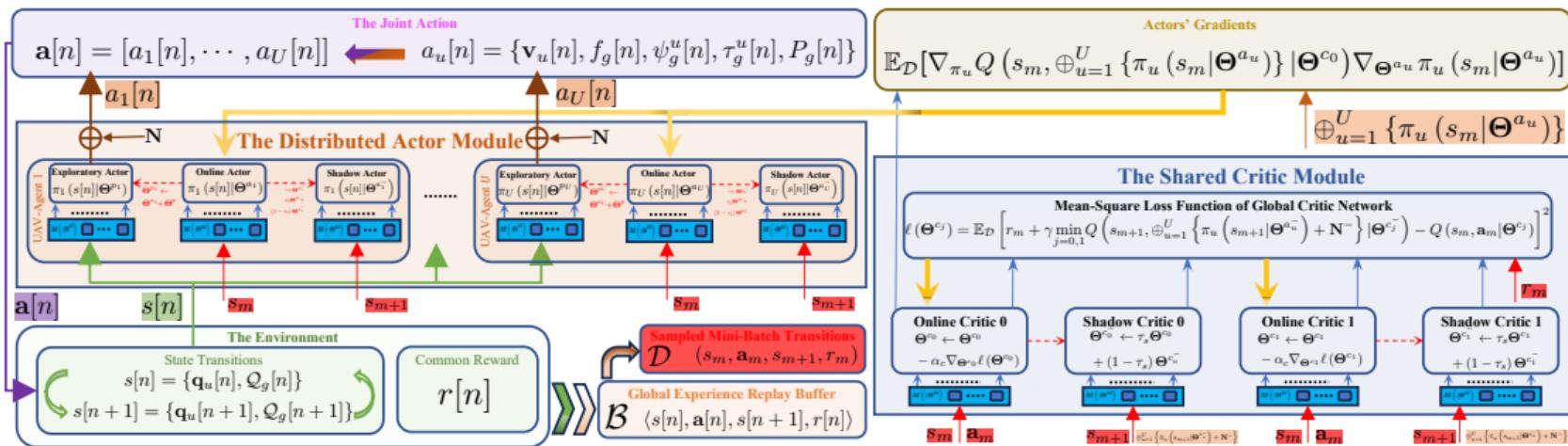
$$\ell(\Theta^{c_j}) = \mathbb{E}_{(s_m, \mathbf{a}_m, s_{m+1}, r_m) \in \mathcal{D} \sim \mathcal{B}} [\mathbf{y}_m - Q(s_m, \mathbf{a}_m | \Theta^{c_j})]^2,$$

$$\mathbf{y}_m = r_m + \gamma \min_{j=0,1} Q\left(s_{m+1}, \bigoplus_{u=1}^U \left\{ \pi_u\left(s_{m+1} | \Theta^{a_u^-}\right) + \mathbf{N}^- \right\} | \Theta^{c_j^-} \right)$$

## Update the trainable parameters of the actors:

$$\begin{aligned} \Theta^{a_u} \leftarrow \Theta^{a_u} + \alpha_a \mathbb{E}_{s_m \in \mathcal{D}} & [\nabla_{\pi_u} Q(s_m, \bigoplus_{u=1}^U \{\pi_u(s_m | \Theta^{a_u})\} | \Theta^{c_0}) \\ & \times \nabla_{\Theta^{a_u}} \pi_u(s_m | \Theta^{a_u})] \end{aligned}$$

# Workflow of the Proposed DSPAC-MN Algorithm



- **Distributed Agents:** explore in parallel
- **Shared Critic:** cooperative learning

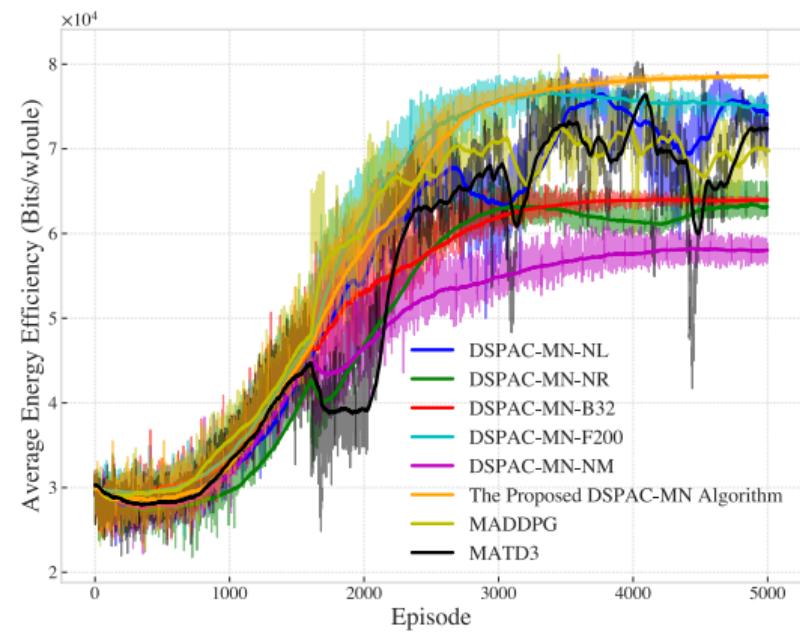
- **Modularized Inputs:** balanced dimension
- **Perturbed Actors:** enhanced exploration

# Setups for System Parameters and Hyperparameters of the Learning Process

Table I: Setups for System Parameters and Hyperparameters of the Learning Process

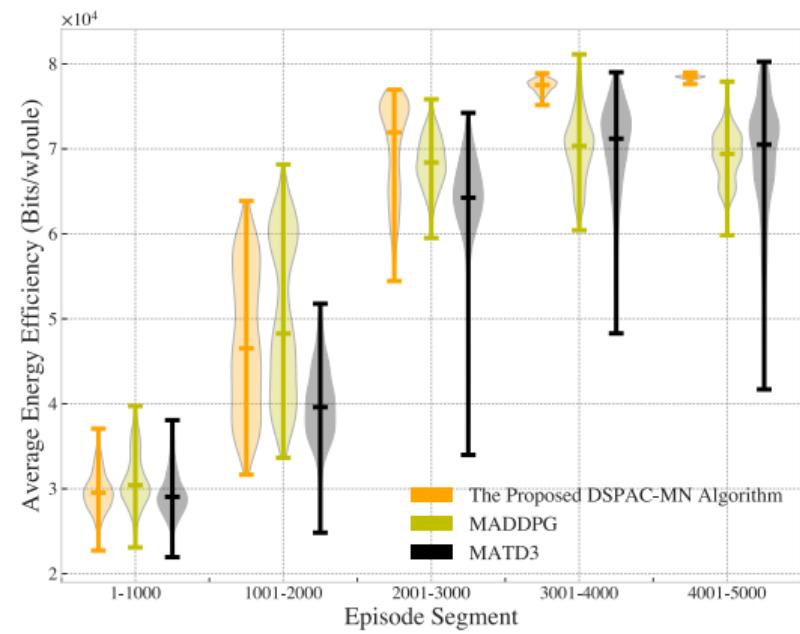
Parameters	Values	Parameters	Values	Parameters	Values
Number of terrestrial UEs $ \mathcal{G}  = G$	6	Number of UAVs $ \mathcal{U}  = U$	2	Replay buffer $\mathcal{B}$ 's capacity $\mathbf{B}$	$10^5$
Length of time slot $\delta_t$	0.5 s	Queue capacity $A_g^*$	$5 \times 10^7$ bits	Mini-batch sampler $\mathcal{D}$ 's size $\mathbf{D}$	256
Safety distance for avoiding collision $D$	8 m	UEs' computation intensity $c_g$	$10^3$ cycles/bit	Exploration noise $\mathbf{N}$	Normal (0, 5)
UEs' maximum CPU-cycle frequency $f_g^*$	0.5 GHz	UEs' maximum transmit power $P_g^*$	30 dBm	Exploration noise variance decaying rate	0.999/episode
UEs' transmission bandwidth $B$	20 GHz	AWGN variance $\sigma^2$	-90 dBm	Staggered policy renewal frequency $N_s$	2
Computation overhead $c_o$	2	UAVs' computation intensity $c_u$	$10^3$ cycles/bit	Shadow policy tempering noise $\mathbf{N}^-$	Normal (0, 1)
UAVs' CPU-cycle frequency budget $f_u^*$	10 GHz	New task instances' variance $A_g$	$2 \times 10^6$ bits	Outbound/collision penalty $p_o/p_c$	100; 100
Minimum/maximum UAV speed $v^-/v^+$	10 m/s; 50 m/s	UAV altitude $z_u$	200 m	Dropout rate for online actors/critics	0.2
UEs' effective capacitance coefficient $\gamma_g$	$10^{-28}$	UEs' non-CPU power cost $E^*$	0 Joule	Learning rates $\alpha_a/\alpha_c$	$10^{-4}; 10^{-3}$
UAVs' effective capacitance coefficient $\gamma_u$	$10^{-28}$	UAVs' non-CPU power cost $\hat{E}_u^*$	0 Joule	Critic's/factors' Exponential learning rate scheduler factor	0.9999; 0.9999
Fuselage drag ratio $\varrho_0$ /Rotor solidity $\varrho_2$	0.6; 0.05	Air density $\varrho_1$	1.225 kg/m <sup>3</sup>	Discount factor $\gamma$ ; Parameter-wise noise variance $\sigma_p^2$	0.99; 0.1
Rotor disc area $\varrho_3$	0.503 m <sup>2</sup>	Blade angular velocity $\varrho_4$	300 radians/s	Polyak averaging coefficient $\tau_s$	$10^{-6}$
Rotor radius $\varrho_5$	0.4 m	Profile drag Coefficient $\varrho_6$	0.012	Maximum training episodes $t\epsilon_{\max}$	5000
Incremental correction factor to induced power $\varrho_7$	0.1	UAV weight $\varrho_8$	20 Newton	Step threshold $N_{\max}$	50
Average rotor induced velocity $v_0$	4.03 m/s	Rotor blade tip speed $v_{tip}$	120 m/s	Direction-aware collision penalty triggering factor $T_c$	1
Relative pressure	1013.25 hPa	Carrier frequency of THz channel $f_c$	0.3 THz	Dimension of each module's output $ \mathcal{M}_i $	10
Speed of light $C$	$3 \times 10^8$ m/s	Antenna gains $G_t/G_r$	20 dBi; 0 dBi	Number of modules inside each actor	$3(U + 1)$
Relative humidity; Energy regulation factor $\mathfrak{R}$	0.5; 0.02	Relative temperature	296.15 °K	Number of modules inside the shared circit	$4(U + 1 + 2U)$

## Average Energy Efficiency versus Training Episode



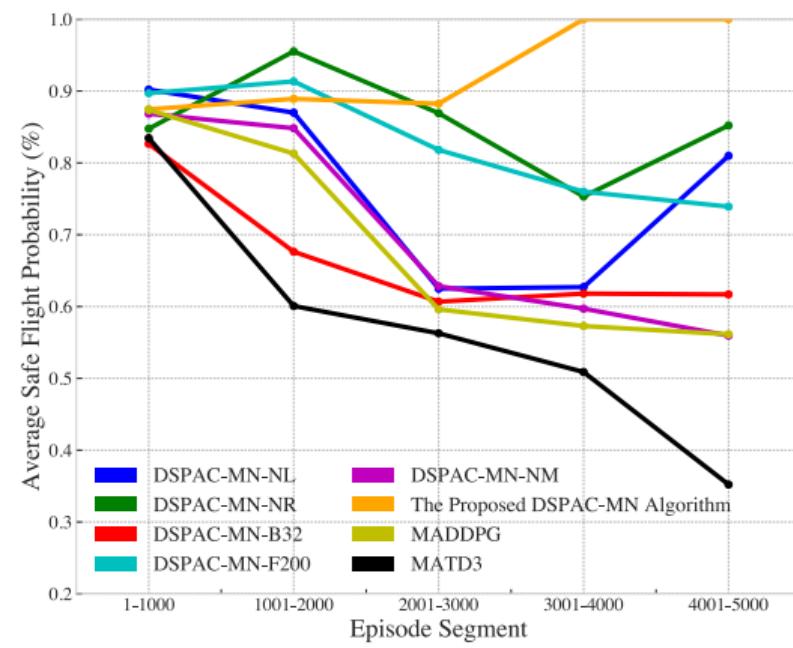
- MADDPG: an extension of deep deterministic policy gradient (DDPG) to handle multi-agent scenarios
- MATD3: an extension of twin-delayed DDPG (TD3) to reduce overestimation bias of MADDPG
- DSPAC-MN-NM: DSPAC-MN without modular networks
- DSPAC-MN-NR: Regularization-less DSPAC-MN
- DSPAC-MN-NL: DSPAC-MN without learning rate scheduling
- DSPAC-MN-B32: DSPAC-MN with batch size of 32
- DSPAC-MN-F200: DSPAC-MN with policy renewal frequency of 200

## Violin Plot versus Episode Segments



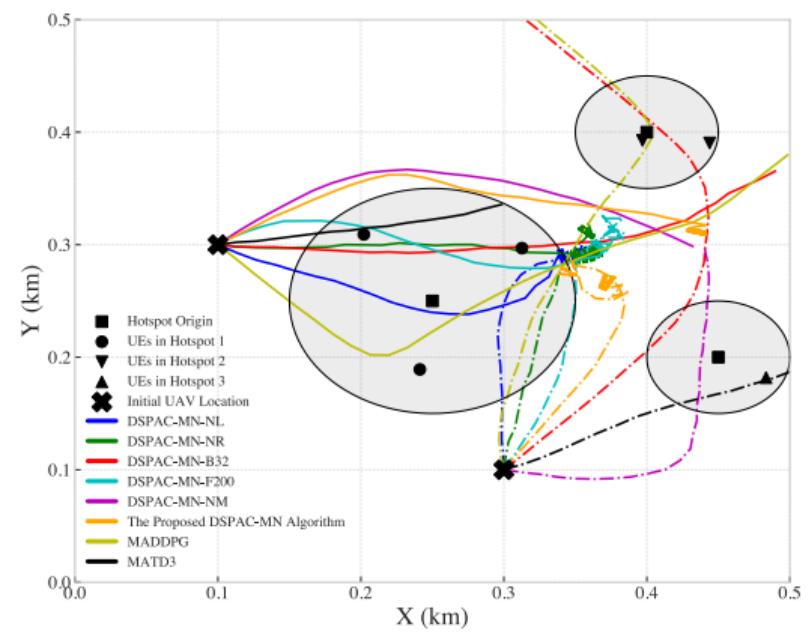
- The metric is measured in **bits/wJoule**, where wJoule accounts for a weighted sum energy consideration, ensuring magnitude **fairness** between computation/offloading and propulsion energy costs.
- The proposed DSPAC-MN **significantly outperforms** other baselines, demonstrating its **effectiveness** and **efficiency** through tailored components such as perturbed actors, a shared critic, and modularized inputs.

# Average Safe Flight Probability



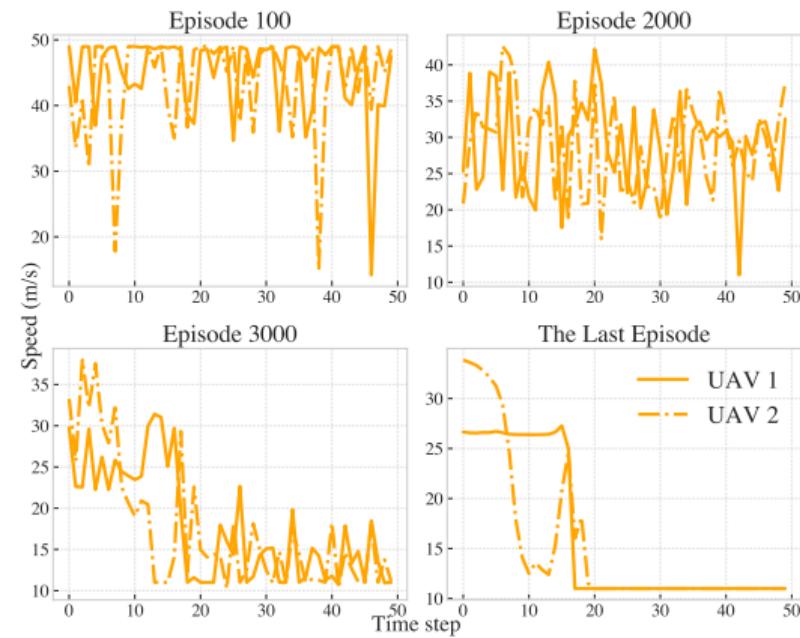
- A safe flight criterion is violated if any UAV flies **out of bounds** or if any pair of UAVs **collides**.
- The proposed DSPAC-MN approach is the only method achieving **100% safe flight navigation**, while other baselines have a **higher likelihood** of violating the rules imposed by the optimization problem.

# Visualization of and Comparison on Devised Trajectories over Various Algorithms



- The proposed DSPAC-MN solution generates trajectories that are **well-separated** and **clear of borders**.
- Baselines such as DSPAC-MN-B32, MADDPG, and MATD3 fail to prevent UAVs from **crashing into borders, violating mobility constraints**.
- Benchmarks like DSPAC-MN-NL, DSPAC-MN-NR, DSPAC-MN-F200, and DSPAC-MN-NM produce trajectories that result in **collisions, breaching collision constraints**.

# Safe Flight Probability and Designed Propulsion Speed



## Comparison on Safe Flight Probability

Algorithms	MADDPG	MATD3	DSPAC-MN-NM	DSPAC-MN-NR
<i>The last 1000 episodes</i>	0.5729	0.59992	0.73998	0.62
<i>The last 200 episodes</i>	0.5853	0.6015	0.74	0.62
<i>The last 10 episodes</i>	0.62	0.598	0.74	0.62

Algorithms	DSPAC-MN-NL	DSPAC-MN-B32	DSPAC-MN-F200	<b>DSPAC-MN</b>
<i>The last 1000 episodes</i>	0.73734	0.77556	0.90374	<b>1.0</b>
<i>The last 200 episodes</i>	0.8205	0.78	0.9905	<b>1.0</b>
<i>The last 10 episodes</i>	0.848	0.78	<b>1.0</b>	<b>1.0</b>

The End

# Thanks for your attentions