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1 Basic

1.1 Default code

```
#include < bits / stdc++.h>
#include<chrono> // for timing
#pragma GCC optimize("03,unroll-loops")
#pragma target optimize("avx2,bmi,bmi2,lzcnt,popcnt")
#define IO ios_base::sync_with_stdio(0);cin.tie(0);cout
     .tie(0);
#define pii pair<int,int>
#define ft first
#define sd second
#define int long long
#define double long double
#define PI acos(-1)
#define SZ(x) (int)x.size()
#define all(v) (v).begin(), (v).end()
#define _for(i,a,b) for(int i=(a);i<(b);++i)</pre>
using namespace std;
template<typename T>
ostream& operator<<((ostream& os,const vector<T>& vn){
  for(int i=0;i<vn.size();++i)os<<vn[i]<<" ";</pre>
  return os;
template<typename T>
ostream& operator<<(ostream& os,const set<T>& vn){
  for(typename set<T>::iterator it=vn.begin();it!=vn.
       end();++it)os<<*it<<" ";
  return os;
mt19937 mt(hash<string>()("Mashu_AC_Please")); //mt();
// mt19937 mt(chrono::steady_clock::now().
    time_since_epoch().count());
// g++ a.cpp -Wall -Wshadow -fsanitize=undefined -o a.
    exe
// ./a.exe
const int MXN=2e5+5;
const int INF=INT_MAX;
void sol() {}
signed main() {
    // auto start=chrono::high_resolution_clock::now();
    // #ifdef LOCAL
    // freopen("input.txt","r",stdin);
    // freopen("output.txt","w",stdout);
    // #endif
    ΙO
    int t=1;
    // cin>>t;
    while(t--) {sol();}
    // auto stop = chrono::high_resolution_clock::now()
    // auto duration = chrono::duration_cast<chrono::</pre>
        milliseconds>(stop - start);
    // cerr<<"Time:"<<duration.count()<<" ms\n";</pre>
}
```

1.2 Misc

```
| iota(vec.begin(),vec.end(),1);// 產生1~size的整數列 | stoi(s.begin(),s.end(),k);// 法1,字串轉成k進位int | string s;cin>>s; | int x=stoi(s,0,2); // 法2,2可以改其他進位 | __builtin_popcountl1 // 二進位有幾個1 | __builtin_clzl1 // 左起第一個1前0的個數 | __builtin_parityl1 // 1的個數的奇偶性 | __builtin_mul_overflow(a,b,&res) // a*b是否溢位 | // double 轉整數 請加 int b=round(a) | // 或是 int b =floor(a+0.5) (floor向下取整)
```

1.3 Fast read & write

```
inline int read() {
   char c = getchar(); int x = 0, f = 1;
   while(c < '0' || c > '9') {if(c == '-') f = -1; c =
      getchar();}
```

1.4 Sort cmp

```
struct cmp{inline bool operator()(const int a,const int
    b){return a<b;}};//common use
auto cmp=[](vector<int> a, vector<int> b) {return a[1]<
    b[1];};//for set use
set<vector<int>, decltype(cmp)> prepare, done;
```

1.5 Discretization

```
vector<int> vec;
sort(vec.begin(),vec.end());
vec.resize(unique(vec.begin(),vec.end())-vec.begin());
for(int i=0;i<n;++i){//+1是讓 index是1到N 可以不要
    arr[i]=lower_bound(vec.begin(),vec.end(),ll[i])-vec
    .begin()+1;
}</pre>
```

1.6 Custom unordered_map

1.7 int128 read

```
_int128_t p;
// __tnt120_t p
// lll n=qr(p);
#define 111 __int128
template < class type_name > inline type_name qr(type_name
     sample)
    type_name ret=0,sgn=1;
    char cur=getchar();
    while(!isdigit(cur))
        sgn=(cur=='-'?-1:1),cur=getchar();
    while(isdigit(cur))
        ret=(ret<<1)+(ret<<3)+cur-'0',cur=getchar();
    return sgn==-1?-ret:ret;
inline void print(__int128 x){
    if(x < 0)
        putchar('-');
        x = -x;
    if(x > 9)
        print(x / 10);
    putchar(x % 10 + '0');
```

1.8 字典序 a 嚴格小於 b

```
template < class T > //字典序a嚴格小於b
bool lexicographicallySmaller(const vector < T > & a, const
    vector < T > & b) {
    int n=a.size();
    int m=b.size();
    int i;
    for(int i=0;i<n && i<m;++i) {
        if(a[i] < b[i]) return true;
        else if(b[i] < a[i]) return false;
    }
    return (i==n && i<m);
}</pre>
```

1.9 Radom

```
| mt19937 gen(0x5EED);
int randint(int lb, int ub)
{ return uniform_int_distribution<int>(lb, ub)(gen); }
```

2 對拍

2.1 run.bat

```
@echo off
g++ ac.cpp -o ac.exe
g++ wa.cpp -o wa.exe
g++ gen1.cpp -o gen.exe

:loop
    echo %%x
    gen.exe > input
    ac.exe < input > ac
    wa.exe < input > wa
    fc ac wa
if not errorlevel 1 goto loop
```

2.2 run.sh

```
for ((i=0;;i++))
do
    echo "$i"
    python3 gen.py > input
    ./ac < input > ac.out
    ./wa < input > wa.out
    diff ac.out wa.out || break
done
```

3 Flow & Matching

3.1 Dicnic

```
// flow.init(n,s,t):有n個點(0~n-1), 起點s終點t
// flow.add_edge(u,v,f):建一條邊,從u點到v點流量為f
// flow.solve():回傳網路最大流答案
//時間複雜度: O(V^2*E)
struct Dinic{
    struct Edge{ int v,f,re; };
    int n,s,t,level[MXN];
    vector<Edge> E[MXN];
    void init(int _n, int _s, int _t){
        n = _n; s = _s; t = _t;
for (int i=0; i<n; i++) E[i].clear();</pre>
    void add_edge(int u, int v, int f){
        E[u].push_back({v,f,(int)(E[v]).size()});
        E[v].push_back({u,0,(int)(E[u]).size()-1});
    bool BFS(){
        for (int i=0; i<n; i++) level[i] = -1;</pre>
        queue<int> que;
        que.push(s);
        level[s] = 0;
        while (!que.empty()){
```

```
int u = que.front(); que.pop();
            for (auto it : E[u]){
            if (it.f > 0 && level[it.v] == -1){
                level[it.v] = level[u]+1;
                que.push(it.v);
        } } }
        return level[t] != -1;
    int DFS(int u, int nf){
        if (u == t) return nf;
        int res = 0;
        for (auto &it : E[u]){
            if (it.f > 0 && level[it.v] == level[u]+1){
            int tf = DFS(it.v, min(nf,it.f));
            res += tf; nf -= tf; it.f -= tf;
            E[it.v][it.re].f += tf;
            if (nf == 0) return res;
        if (!res) level[u] = -1;
        return res;
    int solve(int res=0){
    while ( BFS() )
        res += DFS(s,2147483647);
    return res;
} }flow;
```

3.2 最大流最小花費

```
|//最大流量上的最小花費
//最大流量優先,相同才是找最小花費,複雜度O(V^2*E^2)
// flow.init(n,s,t):有n個點(0~n-1), 起點s終點t
// flow.add\_edge(u,v,f,c):建一條邊,從u點到v點流量為f,
    每一單位流量的花費為c
// flow.solve():回傳一個pair(maxFlow,minCost)
// 限制:圖不能有負環
// 網路最大流的add_edge(u,v,f)可以無痛轉成最大流量上的
     最 小 花 費 add_edge (u, v, 1, f) 即 建 立 一 條 從 u 到 v 的 邊 流 量 為
    1,單位流量花費為f
//0(V^2 E^2)
#define 11 long long
struct zkwflow{
    static const int maxN=20000;
    struct Edge{ int v,f,re; ll w;};
    int n,s,t,ptr[maxN]; bool vis[maxN]; ll dis[maxN];
    vector<Edge> E[maxN];
    void init(int _n,int _s,int _t){
        n=_n,s=_s,t=_t;
        for(int i=0;i<n;i++) E[i].clear();</pre>
    void add_edge(int u,int v,int f,ll w){
        E[u].push_back({v,f,(int)E[v].size(),w});
        E[v].push_back({u,0,(int)E[u].size()-1,-w});
    bool SPFA() {
        fill_n(dis, n, LLONG_MAX);
        fill_n(vis, n, false);
        queue<int> q;
        q.push(s); dis[s]=0;
        while(!q.empty()) {
            int u = q.front(); q.pop();
            vis[u] = false;
            for(auto &it: E[u]){
               if(it.f>0 && dis[it.v]>dis[u]+it.w){
                   dis[it.v] = dis[u]+it.w;
                   if(!vis[it.v]) {vis[it.v] = true; q
                       .push(it.v);}
               }
           }
        if(dis[t]==LLONG_MAX) return false;
        // 不管流量是多少,花費不能是正數時加上這行 (最
            小花費可行流)
        // if(dis[t] >= 0) return false;
        return true;
    int DFS(int u, int nf) {
        if(u==t) return nf;
        int res = 0; vis[u] = true;
```

for(int &i=ptr[u] ; i<(int)E[u].size() ; i++) {</pre>

```
auto &it = E[u][i];
            if(it.f>0 && dis[it.v]==dis[u]+it.w && !vis
                 [it.v]) {
                int tf = DFS(it.v, min(nf, it.f));
                res += tf;
                nf-=tf;
                it.f-=tf;
                E[it.v][it.re].f += tf;
                if(nf==0) { vis[u]=false; break; }
        }
        return res;
    pair<int,ll> solve(){
        int flow = 0; 11 cost = 0;
        while (SPFA()){
            fill_n(ptr, n, 0);
            int f = DFS(s, INT_MAX);
            flow += f;
            cost += dis[t]*f;
        return {flow, cost};
    } // reset: do nothing
} flow;
```

3.3 Hungarian

```
//匈牙利演算法-二分圖最大匹配
//記得每次使用需清空vis數組
//O(nm)
//其中Map為鄰接表(Map[u][v]為u和v是否有連接) S為紀錄這
   個點與誰匹配(S[i]為答案i和誰匹配)
const int M=505, N=505;
bool Map[M][N] = {0};
int S[N];
bool vis[N];
bool dfs(int u){
   for(int i=0;i<N;i++){</pre>
       if(Map[u][i]&&!vis[i]){ //有連通且未拜訪
          vis[i]=1; //紀錄是否走過
          if(S[i]==-1||dfs(S[i])){ //紀錄匹配
              S[i]=u:
              return true; //反轉匹配邊以及未匹配邊
                  的狀態
          }
       }
   return false;
//此二分圖為左邊M個點右邊N個點, 跑匈牙利只要跑1~M就可以
   了, (S[右邊的點] -> 左邊的點)
memset(S,-1,sizeof(S));
int ans = 0;
for(int i=0;i<M;i++){</pre>
   memset(vis,0,sizeof(vis));
   if(dfs(i)) ans++;
   //跑匈牙利
cout<<ans<<"\n";</pre>
for(int i=0 ; i<N ;i++) {</pre>
   if(S[i]!=-1) cout<<"pair: "<<S[i]<<" "<<i<<"\n";</pre>
```

3.4 KM

}

```
|//二分圖最大權完美匹配
|//二分圖左邊的點都要匹配到右邊的點,且每條邊都有權重,

求權重最大值,複雜度O(V^3)
|// graph.init(n):二分圖左右各n個點
|// graph.add_edge(u,v,w):建一條邊,從u點到v點權重為w
|// graph.solve():回傳最大權重
struct KM{ // max weight, for min negate the weights
int n, mx[MXN], my[MXN], pa[MXN];
ll g[MXN][MXN], lx[MXN], ly[MXN], sy[MXN];
bool vx[MXN], vy[MXN];
void init(int _n) { // 1-based, N個節點
n = _n;
```

```
for(int i=1; i<=n; i++) fill(g[i], g[i]+n+1, 0)</pre>
     void add_edge(int x, int y, ll w) {g[x][y] = w;} //
          左邊的集合節點x連邊右邊集合節點y權重為w
     void augment(int y) {
          for(int x, z; y; y = z)
            x=pa[y], z=mx[x], my[y]=x, mx[x]=y;
     void bfs(int st) {
          for(int i=1; i<=n; ++i) sy[i]=INF, vx[i]=vy[i</pre>
              ]=0;
          queue<int> q; q.push(st);
          for(;;) {
              while(q.size()) {
                   int x=q.front(); q.pop(); vx[x]=1;
                   for(int y=1; y<=n; ++y) if(!vy[y]){</pre>
                       11 t = 1x[x]+1y[y]-g[x][y];
                       if(t==0){
                            pa[y]=x;
                            if(!my[y]){augment(y);return;}
                            vy[y]=1, q.push(my[y]);
                       }else if(sy[y]>t) pa[y]=x,sy[y]=t;
                   }
              11 cut = INF;
              for(int y=1; y<=n; ++y)</pre>
                   if(!vy[y]&&cut>sy[y]) cut=sy[y];
              for(int j=1; j<=n; ++j){
    if(vx[j]) lx[j] -= cut;
    if(vy[j]) ly[j] += cut;</pre>
                   else sy[j] -= cut;
              for(int y=1; y<=n; ++y) if(!vy[y]&&sy[y</pre>
                   ]==0){
                   if(!my[y]){augment(y);return;}
                   vy[y]=1, q.push(my[y]);
         }
     11 solve(){ // 回傳值為完美匹配下的最大總權重
          fill(mx, mx+n+1, 0); fill(my, my+n+1, 0);
fill(ly, ly+n+1, 0); fill(lx, lx+n+1, -INF);
          for(int x=1; x<=n; ++x) for(int y=1; y<=n; ++y)</pre>
               // 1-base
            lx[x] = max(lx[x], g[x][y]);
          for(int x=1; x<=n; ++x) bfs(x);</pre>
          for(int y=1; y<=n; ++y) ans += g[my[y]][y];</pre>
          return ans;
|} graph;
```

4 Graph

4.1 BCC

```
//無向圖上,不會產生割點的連通分量稱為點雙連通分量,
    0base
#define PB push_back
#define REP(i, n) for(int i = 0; i < n; i++)</pre>
struct BccVertex {
    int n, nScc, step, dfn[MXN], low[MXN];
    vector<int> E[MXN], sccv[MXN];
    int top, stk[MXN];
    void init(int _n) {
        n = _n;
        nScc = step = 0;
        for (int i = 0; i < n; i++)</pre>
            E[i].clear();
    void addEdge(int u, int v) {
        E[u].PB(v); E[v].PB(u);
    void DFS(int u, int f) {
        dfn[u] = low[u] = step++;
        stk[top++] = u;
        for (auto v : E[u]) {
            if (v == f) continue;
            if (dfn[v] == -1) {
                DFS(v, u);
```

```
low[u] = min(low[u], low[v]);
                if (low[v] >= dfn[u]) {
                     int z;
                     sccv[nScc].clear();
                     do {
                         z = stk[--top];
                         sccv[nScc].PB(z);
                     } while (z != v);
                     sccv[nScc++].PB(u);
            else low[u] = min(low[u], dfn[v]);
        }
    }
    vector<vector<int>> solve() {//回傳每個點雙聯通分量
        vector<vector<int>> res;
        for (int i = 0; i < n; i++)</pre>
            dfn[i] = low[i] = -1;
        for (int i = 0; i < n; i++)</pre>
            if (dfn[i] == -1) {
                top = 0;
                DFS(i, i);
        REP(i, nScc) res.PB(sccv[i]);
        return res:
} graph;
```

```
* **想法(把2-SAT 轉 SCC)**
把n個boolean值分成true和false兩種節點(共$2n$個節點)
如果有一個條件 (p and q),則建兩條邊
not p -> q (if p為false 則 q必為true)
not q -> p (if q為false 則 p必為true)
然後跑一次SCC
我們可以知道對於當前變數$a i$有true和false兩種
* 如果($a_i$和$¬a_i$)在同一個強連通分量裡表示
   (if $a_i$為true 則 $a_i$必為false,因為有一條路徑從
      $a_i$到$¬a_i$)
   (if $a_i$為false 則 $a_i$必為true,因為有一條路徑從
      $¬a_i$到$a_i$)
   很明顯矛盾了...(無解)
* 如果($a_i$和$-a_i$)**不**在同一個強連通分量裡表示
   如果把SCC縮點成DAG
   則會有$a_i$的強連通分量流到$-a_i$的強連通分量 or
      $-a_i$的強連通分量流到$a_i$的強連通分量(其一)
   if (有$a_i$的強連通分量流到$¬a_i$的強連通分量) 則表
      如果 $a_i$為true 則 $a_i$必為false,但
      沒有表示
      ~~如果 $a_i$為false 則 $a_i$必為true~~
      此時把 $a_i$的值設false即可
   ps: 在模板中如果有$a_i$的強連通分量流到$¬a_i$的強連
      通分量則$bln[¬a i]>bln[a i]$
```

4.2 SCC

```
//在有向圖裡的任兩點u \times v,皆存在至少一條 u 到 v 的路徑
    以及 v 到 u 的路徑
//fill zero 注意多筆測資要改fill
//注意要0base
#define PB push_back
#define FZ(x) memset(x, 0, sizeof(x))
const int MXN = 1e5;
struct Scc {
    int n, nScc, vst[MXN], bln[MXN];//nScc 有幾個強連通
        分量
    vector<int> E[MXN], rE[MXN], vec;
    void init(int _n) {
        n = _n;
        for (int i = 0; i < MXN; i++)</pre>
            E[i].clear(), rE[i].clear();
    void addEdge(int u, int v) {
        E[u].PB(v); rE[v].PB(u);
    void DFS(int u) {
        vst[u] = 1;
        for (auto v : E[u])
            if (!vst[v]) DFS(v);
        vec.PB(u);
    void rDFS(int u) {
        vst[u] = 1;
        bln[u] = nScc;
        for (auto v : rE[u])
            if (!vst[v]) rDFS(v);
    void solve() {
        nScc = 0;
        vec.clear();
        FZ(vst);
        for (int i = 0; i < n; i++)</pre>
            if (!vst[i]) DFS(i);
        reverse(vec.begin(), vec.end());
        FZ(vst);
        for (auto v : vec)
            if (!vst[v]) {rDFS(v); nScc++;}
} scc;
```

4.3 2SAT

```
|有N個 boolean 變數$a_1 図 a_N$
|ex: 滿足 (¬a1 or a2)and(a2 or a3)and(¬a3 or ¬a4) 的解
```

4.4 MaximalClique

```
//極大團
//對於一張圖選任意的點子集,如果不能在多選一個點使得選
     的點子集為更大的團
#define N 80
struct MaxClique{ // 0-base
  typedef bitset<N> Int;
  Int lnk[N] , v[N];
  int n;
  void init(int _n){
    n = _n;
for(int i = 0 ; i < n ; i ++){</pre>
      lnk[i].reset(); v[i].reset();
  } }
  void addEdge(int a , int b)
  { v[a][b] = v[b][a] = 1; }
  int ans , stk[N], id[N] , di[N] , deg[N];
  Int cans;
  void dfs(int elem_num, Int candi, Int ex){
    if(candi.none()&&ex.none()){
      cans.reset();
      for(int i = 0 ; i < elem_num ; i ++)</pre>
         cans[id[stk[i]]] = 1;
      ans = elem_num; //cans=1 is in maximal clique
      return;
    int pivot = (candi|ex)._Find_first();
    Int smaller_candi = candi & (~lnk[pivot]);
    while(smaller_candi.count()){
      int nxt = smaller_candi._Find_first();
       candi[nxt] = smaller_candi[nxt] = 0;
      ex[nxt] = 1;
       stk[elem_num] = nxt;
      dfs(elem_num+1,candi&lnk[nxt],ex&lnk[nxt]);
  } }
  int solve(){
    for(int i = 0 ; i < n ; i ++){</pre>
      id[i] = i; deg[i] = v[i].count();
    sort(id , id + n , [&](int id1, int id2){
           return deg[id1] > deg[id2]; });
     for(int i = 0 ; i < n ; i ++) di[id[i]] = i;</pre>
    for(int i = 0 ; i < n ; i ++)</pre>
      for(int j = 0; j < n; j ++)</pre>
        if(v[i][j]) lnk[di[i]][di[j]] = 1;
    ans = 1; cans.reset(); cans[0] = 1;
    dfs(0, Int(string(n,'1')), 0);
    return ans;
} }solver:
```

4.5 MaximumClique

```
//最大團:圖上最多可以選幾個點,使選的彼此之間都有連邊
//最大獨立集:圖上最多可以選幾個點,使選的彼此之間都沒有
//最大獨立集通常會轉換為用補圖做最大團
//0(1.1888<sup>n</sup>)
#define N 111
struct MaxClique{ // 0-base
  typedef bitset<N> Int;
  Int linkto[N] , v[N];
  int n;
  void init(int _n){
    n = _n;
    for(int i = 0 ; i < n ; i ++){</pre>
      linkto[i].reset(); v[i].reset();
  void addEdge(int a , int b)
{ v[a][b] = v[b][a] = 1; }
  int popcount(const Int& val)
  { return val.count(); }
  int lowbit(const Int& val)
  { return val._Find_first(); }
  int ans , stk[N];
  int id[N] , di[N] , deg[N];
  Int cans;
  void maxclique(int elem_num, Int candi){
    if(elem_num > ans){
      ans = elem_num; cans.reset();
      for(int i = 0 ; i < elem_num ; i ++)</pre>
        cans[id[stk[i]]] = 1;
    int potential = elem_num + popcount(candi);
    if(potential <= ans) return;</pre>
    int pivot = lowbit(candi);
    Int smaller_candi = candi & (~linkto[pivot]);
    while(smaller_candi.count() && potential > ans){
      int next = lowbit(smaller_candi);
      candi[next] = !candi[next];
      smaller_candi[next] = !smaller_candi[next];
      potential --;
      if(next == pivot || (smaller_candi & linkto[next
          ]).count()){
        stk[elem_num] = next;
        maxclique(elem_num + 1, candi & linkto[next]);
  } } }
  int solve(){//回傳值為最大團的點數量
    for(int i = 0 ; i < n ; i ++){</pre>
      id[i] = i; deg[i] = v[i].count();
    sort(id , id + n , [&](int id1, int id2){
          return deg[id1] > deg[id2]; });
    for(int i = 0; i < n; i ++) di[id[i]] = i;
for(int i = 0; i < n; i ++)</pre>
      for(int j = 0 ; j < n ; j ++)</pre>
        if(v[i][j]) linkto[di[i]][di[j]] = 1;
    Int cand; cand.reset();
    for(int i = 0; i < n; i ++) cand[i] = 1;</pre>
    ans = 1;
    cans.reset(); cans[0] = 1;
    maxclique(0, cand);
    return ans;
} }solver;
```

4.6 Minimum Mean Cycle

```
//給定一張有向圖,邊上有權重,要找到一個環其平均權重最
小
/* minimum mean cycle O(VE) */
struct MMC{
#define E 101010
#define V 1021
#define inf 1e9
#define eps 1e-6
struct Edge { int v,u; double c; };
int n, m, prv[V][V], prve[V][V], vst[V];
Edge e[E];
vector<int> edgeID, cycle, rho;
double d[V][V];
void init( int _n )
```

```
\{ n = _n; m = 0; \}
  // WARNING: TYPE matters
  //建一條單向邊 (u, v) 權重為 w
  void addEdge( int vi , int ui , double ci )
  \{ e[m ++] = \{ vi, ui, ci \}; \}
  void bellman_ford() {
    for(int i=0; i<n; i++) d[0][i]=0;
for(int i=0; i<n; i++) {</pre>
      fill(d[i+1], d[i+1]+n, inf);
      for(int j=0; j<m; j++) {
  int v = e[j].v, u = e[j].u;</pre>
        if(d[i][v]<inf && d[i+1][u]>d[i][v]+e[j].c) {
           d[i+1][u] = d[i][v]+e[j].c;
           prv[i+1][u] = v;
           prve[i+1][u] = j;
  double solve(){//回傳值為最小平均權重 (小數)
    // returns inf if no cycle, mmc otherwise
    double mmc=inf;
    int st = -1;
    bellman_ford();
    for(int i=0; i<n; i++) {</pre>
      double avg=-inf;
      for(int k=0; k<n; k++) {</pre>
        if(d[n][i]<inf-eps) avg=max(avg,(d[n][i]-d[k][i</pre>
             ])/(n-k));
        else avg=max(avg,inf);
      }
      if (avg < mmc) tie(mmc, st) = tie(avg, i);</pre>
    fill(vst,0); edgeID.clear(); cycle.clear(); rho.
         clear();
    for (int i=n; !vst[st]; st=prv[i--][st]) {
      vst[st]++;
      edgeID.PB(prve[i][st]);
      rho.PB(st);
    while (vst[st] != 2) {
      if(rho.empty()) return inf;
      int v = rho.back(); rho.pop_back();
      cycle.PB(v);
      vst[v]++;
    reverse(ALL(edgeID));
    edgeID.resize(SZ(cycle));
    return mmc;
} }mmc;
```

4.7 Dominator Tree

```
|// 給一張有向圖,圖上有一個起點 S 可以走到所有點。
// 定義 "支配" 為從起點 S 出發,所有能走到節點 x 的路徑
     的最後一個必經點
// 最後 idom[i] 為點 i 的支配點
struct DominatorTree{ // O(n+m)
#define REP(i,s,e) for(int i=(s);i<=(e);i++)</pre>
#define REPD(i,s,e) for(int i=(s);i>=(e);i--)
  int n , s;
  vector< int > g[ MAXN ] , pred[ MAXN ];
  vector< int > cov[ MAXN ];
  int dfn[ MAXN ] , nfd[ MAXN ] , ts;
  int par[ MAXN ]; //idom[u] s到u的最後一個必經點
  int sdom[ MAXN ] , idom[ MAXN ];
  int mom[ MAXN ] , mn[ MAXN ];
inline bool cmp( int u , int v )
   { return dfn[ u ] < dfn[ v ]; }
  int eval( int u ){
    if( mom[ u ] == u ) return u;
     int res = eval( mom[ u ] );
    if(cmp( sdom[ mn[ mom[ u ] ] ] , sdom[ mn[ u ] ] ))
      mn[ u ] = mn[ mom[ u ] ];
    return mom[ u ] = res;
  //節點數量,起點編號 1-base
  void init( int _n , int _s ){
    ts = 0; n = _n; s = _s;
    REP( i, 1, n ) g[ i ].clear(), pred[ i ].clear();
  void addEdge( int u , int v ){
    g[ u ].push_back( v );
```

```
pred[ v ].push_back( u );
  void dfs( int u ){
    ts++;
    dfn[ u ] = ts;
    nfd[ ts ] = u;
    for( int v : g[ u ] ) if( dfn[ v ] == 0 ){
      par[ v ] = u;
      dfs(v);
  } }
  void build(){// 建立支配樹
    REP( i , 1 , n ){
      dfn[ i ] = nfd[ i ] = 0;
      cov[ i ].clear();
      mom[ i ] = mn[ i ] = sdom[ i ] = i;
    dfs(s);
    REPD( i , n , 2 ){
      int u = nfd[ i ];
      if( u == 0 ) continue ;
      for( int v : pred[ u ] ) if( dfn[ v ] ){
        eval( v );
        if( cmp( sdom[ mn[ v ] ] , sdom[ u ] ) )
          sdom[ u ] = sdom[ mn[ v ] ];
      cov[ sdom[ u ] ].push_back( u );
      mom[ u ] = par[ u ];
      for( int w : cov[ par[ u ] ] ){
        eval( w );
        if( cmp( sdom[ mn[ w ] ] , par[ u ] ) )
          idom[ w ] = mn[ w ];
        else idom[ w ] = par[ u ];
      cov[ par[ u ] ].clear();
    REP( i , 2 , n ){
      int u = nfd[ i ];
      if( u == 0 ) continue ;
      if( idom[ u ] != sdom[ u ] )
        idom[ u ] = idom[ idom[ u ] ];
} } domT;
```

5 DP

5.1 數位 DP

```
// dp[位數][狀態]
// dp[pos][state]: 定義為目前位數在前導狀態為state的時
   候的計數
// ex: 求數字沒有出現66的數量 L~r
// -> dp[pos][1] 可表示計算pos個位數在前導出現一個6的計
   數 -> dp[3][1] 則計算 6XXX
// 模板的pos是反過來的,但不影響(只是用來dp記憶用)
// pos: 目前位數
// state: 前導狀態
// Lead: 是否有前導0 (大部分題目不用但有些數字EX:00146
   如果有影響時要考慮)
// Limit: 使否窮舉有被num限制
vector<int> num;
int dp[20][state];
int dfs(int pos, int state, bool lead, bool limit) {
   if(pos==num.size()) {
      //有時要根據不同state回傳情況
       return 1:
   if(limit==false && lead==false && dp[pos][state
       ]!=-1) return dp[pos][state];
   int up = limit?num[pos]:9;
   int ans = 0;
   for(int i=0 ; i<=up ; i++) {</pre>
       //有時要考慮那些狀況要continue
       ans += dfs(pos+1, state||(check[i]==2), lead&&i
          ==0, limit&&i==num[pos]);
   if(limit==false && lead==false) dp[pos][state] =
       ans;
   return ans;
}
```

6 Math

6.1 Formulas

```
|//五次方冪次和
|a(n) = n^2*(n+1)^2*(2*n^2+2*n-1)/12
|//四次方冪次和
|a(n) = n*(n+1)*(2n+1)*(3n^3+3n-1)/30
```

6.2 Primes

```
1097774749, 1076767633, 100102021, 999997771
1001010013, 1000512343, 987654361, 999991231
999888733, 98789101, 987777733, 999991921, 1010101333
```

6.3 Quick Pow

6.4 Mat quick Pow

```
struct mat{
    long long a[200][200],r,c; // resize
    mat(int _r,int _c){r=_r;c=_c;memset(a,0,sizeof(a))
    void build(){for(int i=0;i<r;++i)a[i][i]=1;}</pre>
};
mat operator * (mat &x,mat &y){
    mat z(x.r,y.c);
    for(int i=0;i<x.r;++i)for(int j=0;j<x.c;++j)for(int</pre>
         k=0;k< y.c;++k)
        z.a[i][j]=(z.a[i][j]+x.a[i][k]*y.a[k][j]%MOD)%
             MOD;
    return z;
mat qpow(mat a,int k){
    mat r(a.r,a.r); r.build(); while(k){if(k&1)r=r*a; a=a*
        a;k>>=1;}return r;
}
```

6.5 Primes Table

6.6 Phi 函數

```
// 計算小於n的數中與n互質的有幾個
// O(sqrtN)
int phi(int n){
    int res = n, a=n;
    for(int i=2;i*i<=a;i++){
        if(a%i==0) {
            res = res/i*(i-1);
            while(a%i==0) a/=i;
        }
    if(a>1) res = res/a*(a-1);
    return res;
}
```

6.7 Factor Table

6.8 卡塔蘭數

```
|// O(N), 要記得開Long Long 跟設定 MOD
cat[0]=1; cat[1]=1;
for(ll i=1; i<N; i++) {
    cat[i+1] = cat[i]*(i*4+2)%MOD*qpow(i+2, MOD-2)%MOD;
}
```

6.9 Miller Rabin

```
// n < 4,759,123,141
                             3 : 2, 7, 61
// n < 1,122,004,669,633
                             4 : 2, 13, 23, 1662803
// n < 3,474,749,660,383
                                     : pirmes <= 13
// n < 2^64
// 2, 325, 9375, 28178, 450775, 9780504, 1795265022
// Make sure testing integer is in range [2, n-2] if
// you want to use magic.
LL magic[]={}
bool witness(LL a, LL n, LL u, int t){
  if(!a) return 0;
  LL x=mypow(a,u,n);
  for(int i=0;i<t;i++) {</pre>
    LL nx=mul(x,x,n);
    if(nx==1&&x!=1&&x!=n-1) return 1;
    x=nx;
  return x!=1;
bool miller_rabin(LL n) {
  int s=(magic number size)
  // iterate s times of witness on n
  if(n<2) return 0;</pre>
  if(!(n&1)) return n == 2;
  ll u=n-1; int t=0;
  // n-1 = u*2^t
  while(!(u&1)) u>>=1, t++;
  while(s--){
    LL a=magic[s]%n;
    if(witness(a,n,u,t)) return 0;
  return 1:
}
```

6.10 PollarRho

```
// does not work when n is prime O(n^(1/4))
LL f(LL x, LL mod){ return add(mul(x,x,mod),1,mod); }
LL pollard_rho(LL n) {
   if(!(n&1)) return 2;
   while(true){
      LL y=2, x=rand()%(n-1)+1, res=1;
   for(int sz=2; res==1; sz*=2) {
      for(int i=0; i<sz && res<=1; i++) {</pre>
```

```
x = f(x, n);
res = __gcd(abs(x-y), n);
}
y = x;
}
if (res!=0 && res!=n) return res;
}
```

6.11 PrimeFactorO(logn)

```
#define i64 __int64
vector<i64> ret;
void fact(i64 x) {
    if (miller_rabin(x)) {
        ret.push_back(x);
        return;
    }
    i64 f = pollard_rho(x);
    fact(f); fact(x/f);
}
```

6.12 O(1)mul

```
LL mul(LL x,LL y,LL mod){
  LL ret=x*y-(LL)((long double)x/mod*y)*mod;
  // LL ret=x*y-(LL)((long double)x*y/mod+0.5)*mod;
  return ret<0?ret+mod:ret;
}</pre>
```

6.13 Josephus Problem

6.14 Harmonic Sum

```
struct Harmonic{
    const double gamma = 0.5772156649;
    //求第N個調和級數
    double nthHarmonic(int n){
        double result = log(n)+gamma;
        return result;
    }
    //求項數n的Sn>k
    int findNearstN(int k){
        int n = \exp(k-gamma) + 0.5;
        return n;
    // 16n
    // n/1 + n/2 + n/3 + ... + n/n
    //就是這東西
        [20, 10, 6, 5, 4, 3, 2, 2, 2, 2, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1]
    //這是N以下的全因數和
    int nthHarmonicSum9(int n){
        int inv2=qpow(2,MOD-2,MOD),ans=0;
        for(int i=1;i<=n;){</pre>
            int v = n/i; int j = n/v;
```

7 Data Structure

7.1 BIT

```
//注意值域
#define lowbit(x) (x & -x)
const int N = 1e5+5;
int bit[N];
struct BIT {
    int n;
    void init(int n){this->n = n;}
    void update(int x, int val) {
        for (; x <= n; x += lowbit(x))</pre>
             bit[x] += val;
    int query(int x) {
        int res = 0;
        for (; x; x \rightarrow lowbit(x))
             res += bit[x];
        return res;
    int query(int L, int R) { return query(R) - query(L
          - 1); }
}
```

7.2 BIT 二維

```
struct BIT {
    static const int mxn = 2005;
    int bit[mxn][mxn] = {0};
    int low(int x) {return x&-x;}
    void add(int x, int y, int val) {
        for(int i=x ; i<mxn ; i+=low(i)) for(int j=y ;</pre>
             j<mxn ; j+=low(j)) bit[i][j]+=val;</pre>
    int query(int x, int y) {
        int ans = 0;
        for(int i=x ; i ; i-=low(i)) for(int j=y ; j ;
             j-=low(j)) ans+=bit[i][j];
        return ans:
    int range_query(int a, int b, int x, int y) {
        return query(x, y) - query(x, b-1) - query(a-1, y)
             y) + query(a-1, b-1);
} bit;
```

7.3 稀疏表 0(1) 區間最大最小值

```
//st[i][j]表示[i,i+2^j-1]的最值,區間最大長度為Log2(n)
//i為1base
const int N = 5e4+5;
int stMax[N][20],stMin[N][20],a[N];
struct ST{
    int k;
    void build(int n,int a[]){
        k=log2(n);
        for(int i = 1; i <= n; i++) stMin[i][0] =</pre>
            stMax[i][0] = a[i];
        for(int j = 1; j <= k; j++){</pre>
            for(int i = 1; i + (1 << j) - 1 <= n; i++){}
                stMax[i][j] = max(stMax[i][j - 1],
                    stMax[i + (1 << (j - 1))][j - 1]);
                stMin[i][j] = min(stMin[i][j
                                              - 1],
                    stMin[i + (1 << (j - 1))][j - 1]);
        }
```

```
int queryMax(int 1,int r){
    int j = log2(r-l+1);
    return max(stMax[l][j],stMax[r-(1<<j)+1][j]);
}
int queryMin(int 1,int r){
    int j = log2(r-l+1);
    return min(stMin[l][j],stMin[r-(1<<j)+1][j]);
}
}st;</pre>
```

7.4 Segment Tree

```
struct seg {
    #define left (index<<1)</pre>
     #define right (index<<1|1)</pre>
     static const int MXN = 200005;
     int val[MXN*4], tag[MXN*4];
     int a[MXN];
     void push(int index, int 1, int r) {
         if(tag[index]!=0) {
             val[index]+=tag[index]*(r-1+1);
             if(1!=r) {
                 tag[left] += tag[index];
                 tag[right] += tag[index];
             tag[index]=0;
         }
     void pull(int index, int 1, int r) {
         int mid = 1+r>>1;
         push(left, 1, mid);
         push(right, mid+1, r);
         val[index] = val[left]+val[right];
     void build(int index, int l, int r) {
         if(l==r) {
             val[index] = a[1];
             return;
         int mid = (l+r)>>1;
         build(left, 1, mid);
         build(right, mid+1, r);
         pull(index, l, r);
     void add(int index, int s, int e, int l, int r, int
          v) {
         if(e<1 || r<s) return;</pre>
         if(1<=s && e<=r) {
             tag[index] += v;
             push(index, s, e);
             return;
         int mid = (s+e)>>1;
         push(index, s, e);
         add(left, s, mid, l, r, v);
         add(right, mid+1, e, l, r, v);
         pull(index, s, e);
     int query(int index, int s, int e, int l, int r) {
         if(e<1 || r<s) return 0;</pre>
         if(1<=s && e<=r) {
             push(index, s, e);
             return val[index];
         push(index, s, e);
         int mid = (s+e)>>1;
         return query(right, mid+1, e, l, r)
             +query(left, s, mid, l, r);
} tree;
```

7.5 持久化線段樹

```
vector<Node*> version;
    void pull(Node* node) {
        node->val = node->l->val+node->r->val;
    Node* build(int l,int r) {
        Node* node=new Node;
        if(l==r) {
           node->val = 0; //初始值
           return node;
        int mid = (1+r)/2;
        node->1 = build(1,mid);
        node->r = build(mid+1,r);
        pull(node);
        return node;
    Node* update(Node* cur,int l,int r,int pos,int v) {
        Node* node=new Node;
        if(l==r){
            //改成加值换這行
            //node->val=cur->val + v;
            node->val=v;
            return node;
        int mid=(1+r)/2;
        if(pos<=mid) {</pre>
            node->l=update(cur->l,l,mid,pos,v);
            node->r=cur->r;
        } else {
            node->1=cur->1;
            node->r=update(cur->r,mid+1,r,pos,v);
        pull(node);
        return node;
    int query(Node* cur,int s, int e, int ql, int qr){
        if(ql<=s && e<=qr) return cur->val;
        int ans = 0;
        int mid = (s+e)/2;
        if(ql<=mid) ans += query(cur->l, s, mid, ql, qr
        if(mid+1<=qr) ans += query(cur->r, mid+1, e, ql
            , qr);
        return ans;
    }
} tree;
// push 初始的樹
// tree.version.push_back(tree.build(1, n));
// update(舊版, 1, n, pos, v) return 新版
|// 把pos值改成v
```

7.6 Time Segment Tree

```
#include <bits/stdc++.h>
#define int long long int
using namespace std;
int n, q;
struct node{
    int val;
    node *1, *r;
    node(int v) {val=v; l=r=nullptr;}
    node() {val=0; l=r=nullptr;}
vector<node*> timing;
node* build(int s, int e) {
    node *ret = new node();
    if(s==e) return ret;
    int mid = (s+e)>>1;
    ret->l = build(s, mid);
    ret->r = build(mid+1, e);
    ret->val = ret->l->val + ret->r->val;
    return ret;
node* update(node* pre, int s, int e, int pos, int v) {
    node *ret = new node();
    if(s==e) {ret->val=pre->val+v; return ret;}
    int mid = (s+e)>>1;
    if(pos<=mid) {</pre>
        ret->l = update(pre->l, s, mid, pos, v);
```

```
ret->r = pre->r;
    } else {
        ret->r = update(pre->r, mid+1, e, pos, v);
        ret->1 = pre->1;
    ret->val = ret->l->val + ret->r->val;
    return ret;
void add(int pos, int v) {
    timing.push_back(update(timing.back(), 1, n, pos, v
int que(node* pre, node* now, int 1, int r, int k) {
    if(l==r) return r;
    int mid = (l+r)>>1;
    int diff = now->l->val - pre->l->val;
    //printf("now %d~%d diff %d\n", l, r, diff);
    if(diff>=k) return que(pre->l, now->l, l, mid, k);
    else return que(pre->r, now->r, mid+1, r, k-diff);
    return -1;
int query(int 1, int r, int k) {
    return que(timing[l], timing[r], 1, n, k);
int num[100005];
vector<int> sor;
map<int, int> mp;
signed main() {
    cin>>n>>q;
    timing.push_back(build(1, n));
    for(int i=0,a ; i<n ; i++) {</pre>
        cin>>a; num[i] = a; sor.push_back(a);
    // add: 1 1 1 2 1
    // num: 3 3 3 4 3
    // sor: 3 4
    sort(sor.begin(), sor.end());
    sor.erase(unique(sor.begin(), sor.end()), sor.end()
    for(int i=0 ; i<n ;i++) {</pre>
        int pos = lower_bound(sor.begin(), sor.end(),
            num[i]) - sor.begin() + 1;
        //printf("mp[%d] = %d\n", pos, num[i]);
        mp[pos] = num[i];
        num[i] = pos;
        add(num[i], 1);
    while(q--) {
        int a, b, c; cin>>a>>b>>c;
        cout<<mp[query(a, b, c)]<<endl;</pre>
}
```

7.7 Treap

```
struct Treap {
  int sz, val, pri, tag;
  Treap *1 , *r;
Treap(int _val){
    val=_val; sz=1;
    pri=rand(); l=r=NULL; tag=0;
};
int Size(Treap *a) {return a?a->sz:0;}
void pull(Treap *a) {
  a\rightarrow sz = Size(a\rightarrow l) + Size(a\rightarrow r) + 1;
//val of a is always bigger than val of b
Treap* merge(Treap *a ,Treap *b) {
  if(!a || !b) return a ? a : b;
  if(a->pri>b->pri) {
    a->r = merge(a->r,b);
    pull(a);
     return a;
  } else {
     b->1 = merge( a , b->1 );
    pull(b);
     return b;
}
```

```
void split(Treap *t, int k, Treap*&a, Treap*&b){
  if(!t) {a=b=NULL; return; }
  if(k <= t->val) {
    b = t;
    split(t->1, k, a, b->1);
    pull(b);
  else {
    a = t:
    split(t->r,k,a->r,b);
    pull(a);
Treap* add(Treap *t, int v) {
    Treap *val = new Treap(v);
Treap *l = NULL, *r = NULL;
    split(t, v, l, r);
    return merge(merge(1, val), r);
Treap* del(Treap *t, int v) {
    Treap *1, *mid, *r, *temp;
    split(t, v, 1, temp);
    split(temp, v+1, mid, r);
    return merge(1, r);
// base 1
int position(Treap *t, int p) {
    if(Size(t->1)+1==p) return t->val;
    if(Size(t->1)<p) return position(t->r, p-Size(t->1)
         -1):
    else return position(t->1, p);
//num\ of\ >=\ k
int query(Treap *t, int k) {
    if(!t) return 0;
    if(t->val==k) return Size(t->l)+1;
    if(t->val>k) return query(t->l, k);
    return Size(t->1)+1+query(t->r, k);
```

7.8 PBDS

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#define ordered_set tree<int, null_type,less<int>,
            rb_tree_tag,tree_order_statistics_node_update>
using namespace __gnu_pbds;
// ordered_set s;
// s.insert(1); s.erase(s.find(1));
// order_of_key (k) : Number of items strictly smaller
            than k .
// find_by_order(k) : K-th element in a set (counting
            from zero). (return iterator)
```

8 String

8.1 SA

```
#pragma GCC optimize("03,unroll-loops")
#pragma target optimize("avx2,bmi,bmi2,lzcnt,popcnt")
#include<bits/stdc++.h>
#include<chrono>
#define mid (1 + r) / 2
using namespace std;
const int N = 100010;
struct SA{
#define REP(i,n) for ( int i=0; i<int(n); i++ )</pre>
#define REP1(i,a,b) for ( int i=(a); i<=int(b); i++ )</pre>
  bool _t[N*2];
  int _s[N*2], _sa[N*2], _c[N*2], x[N], _p[N], _q[N*2],
       hei[N], r[N];
 int operator [] (int i){ return _sa[i]; }
 void build(int *s, int n, int m){
    memcpy(_s, s, sizeof(int) * n);
    sais(_s, _sa, _p, _q, _t, _c, n, m);
    mkhei(n);
```

```
void mkhei(int n){
    REP(i,n) r[_sa[i]] = i;
    hei[0] = 0;
    REP(i,n) if(r[i]) {
      int ans = i>0 ? max(hei[r[i-1]] - 1, 0) : 0;
      while(_s[i+ans] == _s[_sa[r[i]-1]+ans]) ans++;
      hei[r[i]] = ans;
    }
  void sais(int *s, int *sa, int *p, int *q, bool *t,
      int *c, int n, int z){
    bool uniq = t[n-1] = true, neq;
    int nn = 0, nmxz = -1, *nsa = sa + n, *ns = s + n,
         lst = -1;
#define MSO(x,n) memset((x),0,n*sizeof(*(x)))
#define MAGIC(XD) MS0(sa, n); \
    memcpy(x, c, sizeof(int) * z); \
    XD; \
    memcpy(x + 1, c, sizeof(int) * (z - 1)); \
    REP(i,n) if(sa[i] && !t[sa[i]-1]) sa[x[s[sa[i
         ]-1]]++] = sa[i]-1; \setminus
    memcpy(x, c, sizeof(int) * z); \
    for(int i = n - 1; i >= 0; i--) if(sa[i] && t[sa[i]
         ]-1]) sa[--x[s[sa[i]-1]]] = sa[i]-1;
    MSO(c, z);
    REP(i,n) uniq \&= ++c[s[i]] < 2;
    REP(i,z-1) c[i+1] += c[i];
    if (uniq) { REP(i,n) sa[--c[s[i]]] = i; return; }
for(int i = n - 2; i >= 0; i--) t[i] = (s[i]==s[i
         +1] ? t[i+1] : s[i]<s[i+1]);
    MAGIC(REP1(i,1,n-1) if(t[i] && !t[i-1]) sa[--x[s[i
         ]]]=p[q[i]=nn++]=i);
    REP(i, n) if (sa[i] && t[sa[i]] && !t[sa[i]-1]) {
      \label{eq:neq_state} \mbox{neq=lst<0} \mbox{$\mid$ memcmp(s+sa[i],s+lst,(p[q[sa[i]]+1]-sa$} \\
           [i])*sizeof(int));
      ns[q[lst=sa[i]]]=nmxz+=neq;
    sais(ns, nsa, p + nn, q + n, t + n, c + z, nn, nmxz
          + 1);
    MAGIC(for(int i = nn - 1; i >= 0; i--) sa[--x[s[p[
         nsa[i]]]]] = p[nsa[i]]);
 }
}sa;
int H[ N ], SA[ N ];
void suffix_array(int* ip, int len) {
  // should padding a zero in the back
  // ip is int array, len is array length
  // ip[0..n-1] != 0, and ip[len] = 0
  ip[len++] = 0;
  sa.build(ip, len, 128);
  for (int i=0; i<len; i++) {</pre>
    H[i] = sa.hei[i + 1];
    SA[i] = sa.\_sa[i + 1];
  // resulting height, sa array \in [0,len)
bool check(string &s,string &t,int p){
    for(int i=0;i<t.size() && i+p<s.size();++i){</pre>
         if(t[i]<s[i+p])return 1;</pre>
         else if(t[i]>s[i+p]) return 0;
    if(t.size()>s.size()-p) return 0;
    return 1;
//example for finding patterns in a string
string s,t;
int ip[N],len;
int main(){
    int n;
    cin>>s>>n;
    len = s.length();
    for(int i=0;i<len;++i) ip[i]=(int)s[i];</pre>
    ip[len] = 0;
    suffix_array(ip,len);
    int 1,r;
    for(int i=0;i<n;++i){</pre>
        cin>>t;
         l = 0, r = s.size()-1;
        while(1!=r){
             if(check(s,t,SA[mid])) r=mid;
             else 1 = mid+1;
```

```
bool f=1;
if(t.size()>s.size()-SA[1]){
    cout<<"NO\n",f=0;
    continue;
}
for(int j=0;j<t.size();++j){
    if(t[j]!=s[j+SA[1]]){
        cout<<"NO\n",f=0;
        break;;
    }
}
if(f) cout<<"YES\n";
}
</pre>
```

8.2 KMP

```
// 回傳所有匹配成功的起始位置,s為文本,t為匹配字串
// nxt表示為匹配失敗時要退回的位置,也是t字串的相等前綴
    後綴的最大長度
// *注意前綴後綴為長度最多為n-1的子字串
// nxt[j] = -1 if j=0
// 0 if 沒有相等的前綴後綴
        K k 為相等前綴後綴的最大長度
//
// 以下為例子
//
       j: 0 1 2 3 4 5 6
//
       t: abaabe
// nxt[j]:-1 0 0 1 1 2 0
// O(n+m),n為s長,m為t長
const int MXN = 1e6+5;
int nxt[MXN];
vector<int> KMP(string s,string t){
    int slen = s.length(), tlen = t.length(), i=0,j=0,k
        =-1;
    nxt[0]=-1:
    while(j<tlen){//build nxt</pre>
       if(k==-1 || t[j]==t[k]) nxt[++j] = ++k;
       else
              k=nxt[k]:
    i=0,j=0;
    vector<int> ret;
    while(i<slen){// matching</pre>
       if(j==-1||s[i]==t[j]) i++,j++;
       else j=nxt[j];
       if(j==tlen){
           ret.push_back(i-tlen+1);//1-base
           j=nxt[j];
       }
    return ret;
}
//另一版
//if t is the substring of s:
//if t in s:
bool cmp(string s, string t) {
    vector<int> front(t.size(), 0);
    for(int i=1, j=0 ; i<t.size() ; i++) {</pre>
       while(j>0 && t[i]!=t[j]) j = front[j-1];
       if(t[i]==t[j]) j++;
       front[i] = j;
    int j=0, i=0;
    while(i<s.size()) {</pre>
       if(s[i]==t[j]) j++,i++;
       else {i += (j==0); j = (j<1?0:front[j-1]);}
       if(j>=t.size()) return true;
    return false;
```

8.3 Single Hash

```
|//字串雜湊前的idx是0-base,雜湊後為1-base
|//H[R] - H[L-1] * p^(R-L+1)
|//cmp的+modl是為了防止負數
|//記得build完之後要buildPow
```

```
//小心遇到hash出負數要記得+modL
#define int long long
const int p = 75577, modl = 1e9 + 7,MXN = 1e6+5;
int Hash[MXN],qpow[MXN];
void build(const string& s) {
    Hash[0]=0;
    for(int i=1; i<=s.size(); i++)</pre>
        Hash[i] = (Hash[i-1] * p + s[i-1]) % modl;
void buildPow(){
    qpow[0]=1;
    for(int i=1;i<MXN;++i) qpow[i]=qpow[i-1]*p%modl;</pre>
bool cmp(int i, int j, int len) {
    return (Hash[i+len-1] - Hash[i-1] * qpow[len] %
        mod1 + mod1) % mod1 ==
    (Hash[j+len-1] - Hash[j-1] * qpow[len] % modl +
        mod1) % mod1;
int get(int i, int j) {
    return (Hash[j]-Hash[i-1]*qpow[j-i+1]%modl+modl)%
        mod1;
}
```

8.4 Double Hash

```
|//字串雜湊前的idx是0-base,雜湊後為1-base
//即區間為 [0,n-1] -> [1,n]
//若要取得區間[L,R]的值則
//H[R] - H[L-1] * p^(R-L+1)
//cmp為比較從i開始長度為Len的字串和從j開始長度為Len的字
//(h[i+len-1] - h[i-1] * qpow(p, len) % modl + modl)
#define int long long
#define x first
#define y second
const int P1 = 75577, P2 = 17, MOD = 1e9 + 7, MXN = 1e6
pair<int,int> Hash[MXN];
int qpow[2][MXN];
void build(const string& s){
  pair<int,int> val = make_pair(0,0);
  Hash[0]=val;
  for(int i=1; i<=s.size(); i++){</pre>
  val.x = (val.x * P1 + s[i-1]) % MOD;
  val.y = (val.y * P2 + s[i-1]) % MOD;
  Hash[i] = val;
  }
void buildPow(){
     qpow[0][0]=qpow[1][0]=1;
     for(int i=1;i<MXN;++i){</pre>
         qpow[0][i]=qpow[0][i-1]*P1%MOD;
         qpow[1][i]=qpow[1][i-1]*P2%MOD;
bool cmp( int i, int j, int len ) {
     return ((Hash[i+len-1].x-Hash[i-1].x*qpow[0][len]%
         MOD+MOD)%MOD == (Hash[j+len-1].x-Hash[j-1].x*
         qpow[0][len]%MOD+MOD)%MOD)
     && ((Hash[i+len-1].y-Hash[i-1].y*qpow[1][len]%MOD+
         MOD)%MOD == (Hash[j+len-1].y-Hash[j-1].y*qpow
         [1][len]%MOD+MOD)%MOD);
pair<int, int> get(int i, int j) {
    return {(Hash[j].x-Hash[i-1].x*qpow[0][j-i+1]%MOD+
         \verb|MOD|| \verb|MOD|| % \verb|MOD|| (Hash[j].y-Hash[i-1].y*qpow[1][j-i]| 
         +1]%MOD+MOD)%MOD};
}
```

8.5 Trie

```
|//cnt為記錄有多少個一樣的單詞且end的時候才有數字
| const int MXN=1e6+5;//MXN取文本長
| int trie[MXN][26], cnt[MXN],tot=0;//0 base
| void update(string s){
| int p=0;//0 base
| for(int i=0;i<s.size();++i){
```

} }

//

z[0]=1;

// cin>>s;

// mx--:

8.9

```
int ch = s[i]-'a';
       if(!trie[p][ch]) trie[p][ch]=++tot;
       p = trie[p][ch];
    cnt[p]++;
int query(string s){
    int p=0;
    for(int i=0;i<s.size();++i){</pre>
       int ch=s[i]-'a';
       p = trie[p][ch];
       if(!p) return 0;
    return cnt[p];
void visualizeTrie(int node = 0, int depth = 0) {//for
    for (int i = 0; i < 26; ++i) {
       if (trie[node][i]) {
           for (int j = 0; j < depth; ++j) cout << "</pre>
           visualizeTrie(trie[node][i], depth + 1);
       }
    }
}
```

8.6 Z value

```
// O(n)
//z[i] = Lcp(s[1...],s[i...])
//1base
int z[MAXN];
void Z_value(const string& s) {
   int i, j, left, right, len = s.size();
   left=right=0; z[0]=len;
   for(i=1;i<len;i++) {
      j=max(min(z[i-left],right-i),0);
      for(;i+j<len&&s[i+j]==s[j];j++);
      z[i]=j;
      if(i+z[i]>right) {
        right=i+z[i];
        left=i;
   } }
}
```

8.7 MinRotation

```
//rotate(begin(s), begin(s)+minRotation(s), end(s))
//For example, rotations of acab are acab, caba, abac,
    and baca.
//find Lexicographically minimal rotation of a string
int minRotation(string s) {
    int a = 0, N = s.size(); s += s;
    for(int b=0;b<N;b++) for(int k=0;k<N;k++) {
        if(a+k == b || s[a+k] < s[b+k])
            {b += max(0, k-1); break;}
        if(s[a+k] > s[b+k]) {a = b; break;}
    } return a;
}
```

8.8 Manacher 馬拉車回文

```
|// O(N)求以每個字元為中心的最長回文半徑

|// 頭尾以及每個字元間都加入一個

|// 沒出現過的字元,這邊以'@'為例

|// s為傳入的字串,Len為字串長度

|// z為儲存以每個字元為中心的回文半徑+1(有包含'@'要小心)

|// ex: s = "abaac" -> "@a@b@a@a@c@"

|// z = [12141232121]

const int MXN = 1e6+5;

int z[2*MXN];

char s[2*MXN];

void z_value_pal(char *s,int len,int *z){

len=(len<<1)+1;

for(int i=len-1;i>=0;i--)
```

PalTree 回文樹

s[i]=i&1?s[i>>1]:'@';

++z[i];

// int mx=-1, mxi=0;

for(int i=1,l=0,r=0;i<len;i++){
 z[i]=i<r?min(z[l+l-i],r-i):1;</pre>

if(i+z[i]>r) l=i,r=i+z[i];

// z_value_pal(s,strlen(s),z);

// for(int i=0;i<=strlen(s);++i)</pre>

// for(int i=mxi-mx;i<=mxi+mx;++i)</pre>

if(s[i]!='@') cout<<s[i];

if(mx < z[i]) mx = z[i], mxi = i;

while(i-z[i]>=0&&i+z[i]<len&&s[i-z[i]]==s[i+z[i]])</pre>

```
// Len[s]是對應的回文長度
// num[s]是有幾個回文後綴
// cnt[s]是這個回文子字串在整個字串中的出現次數
// fail[s]是他長度次長的回文後綴, aba的fail是a
const int MXN = 1000010;
struct PalT{
    int nxt[MXN][26],fail[MXN],len[MXN];
    int tot,lst,n,state[MXN],cnt[MXN],num[MXN];
    int diff[MXN],sfail[MXN],fac[MXN],dp[MXN];
    char s[MXN]={-1};
    int newNode(int 1,int f){
       len[tot]=1,fail[tot]=f,cnt[tot]=num[tot]=0;
       memset(nxt[tot],0,sizeof(nxt[tot]));
       diff[tot]=(1>0?1-len[f]:0);
       sfail[tot]=(1>0&&diff[tot]==diff[f]?sfail[f]:f)
       return tot++;
    int getfail(int x){
       while(s[n-len[x]-1]!=s[n]) x=fail[x];
       return x;
    int getmin(int v){
       dp[v]=fac[n-len[sfail[v]]-diff[v]];
       if(diff[v]==diff[fail[v]])
           dp[v]=min(dp[v],dp[fail[v]]);
       return dp[v]+1;
    int push(){
       int c=s[n]-'a',np=getfail(lst);
       if(!(lst=nxt[np][c])){
           lst=newNode(len[np]+2,nxt[getfail(fail[np])
               ][c]);
           nxt[np][c]=lst; num[lst]=num[fail[lst]]+1;
       fac[n]=n;
       for(int v=lst;len[v]>0;v=sfail[v])
           fac[n]=min(fac[n],getmin(v));
       return ++cnt[lst],lst;
    void init(const char *_s){
       tot=1st=n=0;
       newNode(0,1),newNode(-1,1);
       for(;_s[n];) s[n+1]=_s[n],++n,state[n-1]=push()
       for(int i=tot-1;i>1;i--) cnt[fail[i]]+=cnt[i];
} palt;
// state 數組
      state[i] 代表第 i 個字元為結尾的最長回文編號(編號
    是甚麼不重要)
//
     S = "abacaaba"
//
//
      以第 2(0-base) 個字元為結尾的最長回文是 aba
      以第 7(0-base) 個字元為結尾的最長回文是 aba
//
      兩個最長回文都相同,因此 state[2] 會等於 state[7]
//
// Len 數組
     求出某個 state 的長度
```

```
//
//
      S = "aababa"
//
//
      (0-base)
      len[state[1]] = 2 ( "aa" )
len[state[3]] = 3 ( "aba" )
//
//
      len[state[5]] = 5 ( "ababa" )
//
// num 數組
//
      某個state的回文有幾個回文後綴
//
//
      假設某個 state 代表的回文為 =
                                  "ababa"
                                           為例
//
      state 代表的回文的 num = 3
      -> ababa -> aba -> a
//
// cnt 數組
//
      某個 state 的回文在整個字串中出現次數
//
      S = "aababaa"
//
      state[3] 代表的回文為 "aba" 在整個字串中出現 2
//
//
      因此 cnt[state[3]] = 2
// fail數組
      每個 state 的次長回文後綴的 state 編號
//
      S = "ababa"
//
      len[fail[4]] = 3 (fail[4] = "aba" )
//
      len[fail[2]] = 1 (fail[2] = "a"
//
//
      len[fail[0]] = 0 (fail[0] =
      0 所代表的 state 是空字串
///
```

8.10 DistinctSubsequence

```
//預設為小寫字母
//return the number of distinct non-empty subsequences
    of sting
#define int long long
int mod = 1e9 + 7;
vector<int> cnt(26);
int distinct_subsequences(string s) {
    for (char c : s)
    cnt[c - 'a'] = accumulate(begin(cnt), end(cnt), 1LL
        ) % mod;
    return accumulate(begin(cnt), end(cnt), 0LL) % mod;
}
```

9 Tree

9.1 TreeHash

```
// 1. dfs 先做子樹
// 2. 葉節點的hash值為1
// 3. 對於節點x,其hash值為紀錄x的所有子樹的hash值(紀錄
    到temp),然後由小排到大(排除子樹的隨機問題)
// 4. n表示節點x有幾個子樹, p和MOD通常為一個很大的質
    數,由此算出x的hash值
// 5. 樹根的hash值即為整顆樹的hash值,若兩顆樹的hash值
   相同,則兩棵樹就是同構
const int MXN = 200005;
int subtree_sz[MXN];
int hash_[MXN];
int base = 44560482149;
int MOD = 274876858367;
int dfs(int x, int fa, vector<int>* edge){
   vector<int> temp;
   subtree_sz[x] = 1;
   for(int child : edge[x]){
       if(child==fa) continue;
       temp.push_back(dfs(child, x, edge));
       subtree_sz[x] += subtree_sz[child];
   sort(temp.begin(), temp.end());
   int ret = subtree_sz[x];
   for(int v : temp){
       ret = (((ret * base + v + ret) % MOD + ret) %
          MOD + v) % MOD ;
```

```
hash_[x] = ret;
return ret;
}
```

9.2 輕重鏈剖分

```
const int MXN = 2e5+7;
int top[MXN], son[MXN], dfn[MXN], rnk[MXN], dep[MXN],
    father[MXN];
vector<int> edge[MXN];
int dfs1(int v, int fa, int d) {
    int maxsz = -1, maxu, total = 1;
    dep[v] = d;
    father[v] = fa;
    for(int u: edge[v]) {
        if(fa == u) continue;
        int temp = dfs1(u, v, d+1);
        total += temp;
        if(temp>maxsz) {
           maxsz = temp;
           maxu = u:
    if(maxsz==-1) son[v] = -1;
    else son[v] = maxu;
    return total;
int times = 1;
void dfs2(int v, int fa) {
    rnk[times] = v;
    dfn[v] = times++;
    top[v] = (fa==-1 || son[fa] != v ? v : top[fa]);
    if(son[v]!=-1) dfs2(son[v], v);
    for(int u: edge[v]) {
        if(fa == u || u == son[v]) continue;
        dfs2(u, v);
    }
//rnk: 剖分後的編號 (rnk[時間] = 原點)
//dfn: 剖分後的編號 (dfn[原點] = 時間)
//top: 剖分的頭頭
//son: 剖分的重兒子
```

10 Geometry

10.1 Definition2D

```
#define ld long double
const ld eps=1e-10;
int dcmp(ld x){if(fabs(x)<eps) return 0;else return x</pre>
    <0?-1:1;}
struct Pt{
    ld x,y;
    Pt(1d x=0,1d y=0):x(x),y(y){}
    Pt operator+(const Pt &a) const {
        return Pt(x+a.x, y+a.y); }
    Pt operator-(const Pt &a) const {
        return Pt(x-a.x, y-a.y);
    Pt operator*(const ld &a) const {
    return Pt(x*a, y*a); }
Pt operator/(const ld &a) const {
        return Pt(x/a, y/a); }
    ld operator*(const Pt &a) const {//dot
        return x*a.x + y*a.y;
    ld operator^(const Pt &a) const {//cross
        return x*a.y - y*a.x; }
    bool operator<(const Pt &a) const {</pre>
        return x < a.x || (x == a.x && y < a.y); }
        //return\ dcmp(x-a.x) < 0\ |\ (dcmp(x-a.x) == 0
            && dcmp(y-a.y) < 0); }
    bool operator>(const Pt &a) const {
        return x > a.x || (x == a.x && y > a.y); }
        //return \ dcmp(x-a.x) > 0 \ | \ (dcmp(x-a.x) == 0
            && dcmp(y-a.y) > 0); }
    bool operator==(const Pt &a) const {
        return dcmp(x-a.x) == 0 && dcmp(y-a.y) == 0; }
```

```
// return x == other.x && y == other.y;
}:
typedef Pt Vec;
ld Dot(Vec a, Vec b){return a.x*b.x+a.y*b.y;}
ld Cross(Vec a, Vec b){return a.x*b.y-a.y*b.x;}
ld Length(Vec a){return sqrt(Dot(a,a));}
ld Angle(Vec a, Vec b){return acos(Dot(a,b)/Length(a)/
    Length(b));}//弧度
ld Degree(Vec a, Vec b){return Angle(a,b)*180/acos(-1);}
    //角度
ld Area2(Pt a,Pt b,Pt c){return Cross(b-a,c-a);}//(a,b)
    X(a,c)的面積
Vec Rotate(Vec a,ld rad){return Vec(a.x*cos(rad)-a.y*
    sin(rad),a.x*sin(rad)+a.y*cos(rad));}//逆時針旋轉,
    rad為弧度
Vec Normal(Vec a){ld L=Length(a); return Vec(-a.y/L,a.x/
    L);}//單位法向量,確保a不是零向量
struct Line {
  Pt a, b, v; // start, end, end-start
  ld ang;
  Line(Pt _a=Pt(0, 0), Pt _b=Pt(0, 0)):a(_a),b(_b) { v
      = b-a; ang = atan2(v.y, v.x); }
  bool operator<(const Line &L) const {</pre>
    return ang < L.ang;</pre>
} };
```

10.2 Basic

```
getLineIntersection
//確保兩直線P+tv和Q+tw有唯一交點且Cross(v,w)非零
Point getLineIntersection(Point P, Vector v, Point Q,
    Vector w){
    Vector u=P-Q;
    double t=Cross(w,u)/Cross(v,w);
    return P+v*t;
}
distanceToLine
//點到直線距離
double distanceToLine(Point p,Point a,Point b){
    Vector v1=b-a, v2=p-a;
    return fabs(Cross(v1,v2)/Length(v1));
}
distanceToSegment
//點到線段距離
double distanceToSegment(Point p,Point a,Point b){
    if(a==b) return Length(p-a);
    Vector v1=b-a, v2=p-a, v3=p-b;
    if(dcmp(Dot(v1,v2))<0) return Length(v2);</pre>
    else if(dcmp(Dot(v1,v3))>0) return Length(v3);
    else return fabs(Cross(v1,v2)/Length(v1));
}
GetLineProjection
//點到直線投影
Point GetLineProjection(Point p,Point a,Point b){
    Vector v=b-a;
    return a+v*(Dot(v,p-a)/Dot(v,v));
}
getSymmetryPoint
//點p於直線ab的對稱點
Point getSymmetryPoint(Point p,Point a,Point b){
    Point q=getLineProjection(p,a,b);
    return q*2-p;
}
isSegmentProperIntersection
//判斷線段相交(剛好交一點),若兩線段共線->c1=c2=0
bool isSegmentProperIntersection(Point a1, Point a2,
    Point b1, Point b2){
    double c1=Cross(a2-a1,b1-a1),c2=Cross(a2-a1,b2-a1),
        c3=Cross(b2-b1,a1-b1),c4=Cross(b2-b1,a2-b1);
    return dcmp(c1)*dcmp(c2)<0&&dcmp(c3)*dcmp(c4)<0;</pre>
}
```

10.3 PolygonArea

```
//須注意Long Long 及 加上絕對值
double polygonArea(Point* p,int n){
    double area=0;
    for(int i=1;i<n-1;++i){
        area+=Cross(p[i]-p[0],p[i+1]-p[0]);
    }
    return area/2;
}</pre>
```

10.4 IsPointInPolygon

10.5 ConvexHull

```
//回傳凸包頂點數
//輸入不能有重複點,注意h的點未排序!
//如果有在邊上的輸入點,要把<=改成<
//若要求高精度用dcmp比較
vector<Pt> ch(MXN);
int convexHull(Pt* p,int n){
    sort(p,p+n);
    int m=0;
    for(int i=0;i<n;++i){//downHull</pre>
        while(m>1&&Cross(ch[m-1]-ch[m-2],p[i]-ch[m-2])
            <=0) m--;
        ch[m++]=p[i];
    int k=m;
    for(int i=n-2;i>=0;--i){//upHull
        while(m>k&&Cross(ch[m-1]-ch[m-2],p[i]-ch[m-2])
            <=0) m--;
        ch[m++]=p[i];
    if(n>1) m--;
    return m;
}
```

10.6 ConvexHullTrick

```
struct Convex {
    int n;
    vector<Pt> A, V, L, U;
    //init , pass convex hull points
    Convex(const vector<Pt> &_A) : A(_A), n(_A.size())
        \{ // n >= 3
        auto it = max_element(all(A));
        L.assign(A.begin(), it + 1);
        U.assign(it, A.end()), U.push_back(A[0]);
        for (int i = 0; i < n; i++) {</pre>
            V.push_back(A[(i + 1) % n] - A[i]);
    int PtSide(Pt p, Line L) {
        return dcmp((L.b - L.a)^(p - L.a));
    int inside(Pt p, const vector<Pt> &h, auto f) {
        auto it = lower_bound(all(h), p, f);
        if (it == h.end()) return 0;
        if (it == h.begin()) return p == *it;
        return 1 - dcmp((p - *prev(it))^(*it - *prev(
            it)));
    // 1. whether a given point is inside the Convex
        Hull
    // ret 0: out, 1: on, 2: in
    int inside(Pt p) {
        return min(inside(p, L, less{}), inside(p, U,
            greater{}));
    static bool cmp(Pt a, Pt b) { return dcmp(a ^ b) >
    // 2. Find tangent points of a given vector
    // ret the idx of far/closer tangent point
int tangent(Pt v, bool close = true) {
        assert(v != Pt{});
        auto 1 = V.begin(), r = V.begin() + L.size() -
            1;
        if (v < Pt{}) 1 = r, r = V.end();</pre>
        if (close) return (lower_bound(l, r, v, cmp) -
            V.begin()) % n;
        return (upper_bound(l, r, v, cmp) - V.begin())
            % n;
    // 3. Find 2 tang pts on CH of a given outside
    // return index of tangent points
    // return {-1, -1} if inside CH
    array<int, 2> tangent2(Pt p) {
        array<int, 2> t{-1, -1};
        if (inside(p) == 2) return t;
        if (auto it = lower_bound(all(L), p); it != L.
            end() and p == *it) {
            int s = it - L.begin();
            return {(s + 1) % n, (s - 1 + n) % n};
        if (auto it = lower_bound(all(U), p, greater{})
            ; it != U.end() and p == *it) {
            int s = it - U.begin() + L.size() - 1;
            return {(s + 1) % n, (s - 1 + n) % n};
        for (int i = 0; i != t[0]; i = tangent((A[t[0]
            = i] - p), 0));
        for (int i = 0; i != t[1]; i = tangent((p - A[t
            [1] = i]), 1));
        return t;
    int find(int 1, int r, Line L) {
        if (r < 1) r += n;
        int s = PtSide(A[1 % n], L);
        return *ranges::partition_point(views::iota(1,
            [&](int m) {
                return PtSide(A[m % n], L) == s;
    };
    // 4. Find intersection point of a given line
    // intersection is on edge (i, next(i))
    vector<int> intersect(Line L) {
```

10.7 Polar Sort

```
//極角排序,從270度開始逆時針排序
bool cmp(const Point& lhs,const Point&rhs){
    if(Cross((lhs < Point()),(rhs < Point())))
        return (lhs < Point()) < (rhs < Point());
    return Cross(lhs,rhs) > 0;
}

/* 若要以p[i]為原點排序->計算v=p[j]-p[i]
for(int j=0;j<n;++j){
    if(i!=j){
        Vector v = p[j]-p[i];
        node[nodeSz++] = {v,j};
    }
}
sort(node,node+nodeSz,cmp);
*/</pre>
```

10.8 PickTheorm

```
| int area,in,on;//area:多邊形面積 in:內部格點數 on:邊界格點數
| void PickTheorm(Point* p,int n){
| area=polygonArea(p,n);
| for(int i=0;i<n;++i){
| on+=__gcd(abs((int)p[i].x-(int)p[(i+1)%n].x),
| abs((int)p[i].y-(int)p[(i+1)%n].y));
| }
| in=abs(area)+1-on/2;
| }
```

10.9 最近點對

```
//最近點對距離注意若整數要define double long long
double closestEuclideanDistance(Point* p,int n){
    sort(p,p+n);
     set<Point> s={{p[0].y,p[0].x}};
    int j = 0;
    Point t;
    double dd=LLONG_MAX,d;
    for(int i=1;i<n;++i){</pre>
         d = sqrt(dd);
        while(j < i \&\& p[j].x < p[i].x-d){
             s.erase({p[j].y,p[j++].x});
         auto 1 = s.lower_bound({p[i].y-d,p[i].x-d});
         auto u = s.upper_bound({p[i].y+d,p[i].x+d});
         for(auto it=1;it!=u;it++){
            t = {it->y,it->x};
            dd =min(dd, Dot(p[i]-t,p[i]-t));
         s.emplace(p[i].y,p[i].x);
    return dd;
}
```

10.10 幾何中位數

```
//回傳為到每個頂點距離和最小的點
Point weiszfeld(const Point *p,int n){
    double nn=n;
    Point cur = p[0];
    for(int i=1;i<n;++i){
        cur.x+=p[i].x, cur.y+=p[i].y;</pre>
```

}

```
cur.x/=nn, cur.y/=nn;
    Point next;
    double w,numerX,numerY,denomin;
    while(1){
        numerX=numerY=denomin=0;
        bool update=0;
        double d;
        for(int i=0;i<n;++i){</pre>
             d=Length(cur-p[i]);
             if(d>eps){
                 w = 1.0/d;
                 numerX+=w*p[i].x;
                 numerY+=w*p[i].y;
                 denomin+=w;
                 update=1;
             }else{
                 next = p[i];
                 break;
             }
        if(update){
             next.x = numerX/denomin;
             next.y = numerY/denomin;
        if(Length(cur-next)<eps) break;</pre>
        cur = next;
    return next;
}
```

10.11 矩陣掃描線

```
#include <bits/stdc++.h>
#define int long long int
using namespace std;
int n, st[1000005<<2], lazy[1000005<<2], old</pre>
    [1000005<<2];
vector <tuple<int, int, int, int>> v;
vector<int> sor;
void pull(int index, int 1, int r) {
    if(lazy[index]) st[index] = old[index];
    else if(l==r) st[index] = 0;
    else st[index] = st[index<<1|1]+st[index<<1];</pre>
    // printf("pull %lld~%lld, %lld\n", l, r, st[index
         ]);
    return;
void insert(int index, int s, int e, int l, int r, int
    //printf("insert: range %lld~%lld, query %lld~%lld\
    n", s, e, l, r);
if(l<=s && e<=r) {
        lazy[index] +=k;
        pull(index, s, e);
        return;
    int mid = (s+e)/2;
    if(l<=mid) insert(index<<1, s, mid, l, r, k);</pre>
    if(mid<r) insert(index<<1|1, mid+1, e, 1, r, k);</pre>
    pull(index, s, e);
void input(int index, int 1, int r) {
    if(l==r) {
        old[index] = sor[l]-sor[l-1];
        return;
    int mid = (1+r)/2;
    input(index<<1, 1, mid);</pre>
    input(index<<1|1, mid+1, r);</pre>
    old[index] = old[index<<1] + old[index<<1|1];
//cout<<l<<" to "<<r<" is "<<old[index]<<endl;</pre>
    return;
// int diff=1000005;
signed main(){
    cin >> n;
    int 1, r, d, u;
    for (int i = 0; i < n; i++){
        cin >> 1 >> d >> r >> u;
```

```
// L+=diff;
    // d+=diff;
    // r+=diff;
    // u+=diff;
    sor.push_back(d);
    sor.push_back(u);
    v.push_back({1, d, u, 1});
    v.push_back({r, d, u, -1});
set<int> temp(sor.begin(), sor.end());
sor = vector<int>(temp.begin(), temp.end());
sort(sor.begin(), sor.end());
for(int i=0 ; i<v.size() ; i++) {</pre>
    auto [a, b, c, k] = v[i];
    v[i] = make_tuple(a, (int)(lower_bound(sor.
        begin(), sor.end(), b)-sor.begin()), (int)(
        lower_bound(sor.begin(), sor.end(), c)-sor.
        begin()), k);
input(1, 1, sor.size()-1);
// cout<<"get: "
// for(int i: sor) cout<<i<<" "; cout<<endl;</pre>
sort(v.begin(), v.end());
int pre=0;
int ans=0;
for(auto [pos, a, b, k]: v) {
    if(pre!=pos) {
        ans+=(pos-pre)*st[1];
        pre = pos;
    insert(1, 1, sor.size()-1, a+1, b, k);
    // printf("now act: pos %lld,
                                    %lld~%lld, act:
        %lld\n", pos, a+1, b, k);
    // printf("now ans: %[ld\n", st[1]);
cout<<ans<<endl;</pre>
```

10.12 Circle Definition

```
struct Circle {
  Pt o; ld r;
  Circle(Pt _o=Pt(0, 0), ld _r=0):o(_o), r(_r) {}
};
```

10.13 CircleCover

```
#define N 100
#define D long double
struct CircleCover{//O(N^2LogN)
  int C; Circle c[ N ]; //填入C(圓數量),c(圓陣列,0base)
  bool g[ N ][ N ], overlap[ N ][ N ];
  // Area[i] : area covered by "at least" i circles
  D Area[ N ];
  void init( int _C ){ C = _C; }//總共 _c 個圓
  bool CCinter( Circle& a , Circle& b , Pt& p1 , Pt& p2
    Pt o1 = a.o , o2 = b.o;
    D r1 = a.r , r2 = b.r;
    if( Length( o1 - o2 ) > r1 + r2 ) return {};
    if( Length( o1 - o2 ) < max(r1, r2) - min(r1, r2) )</pre>
         return {};
    D d2 = (o1 - o2) * (o1 - o2);
    D d = sqrt(d2);
    if( d > r1 + r2 ) return false;
    Pt u=(o1+o2)*0.5 + (o1-o2)*((r2*r2-r1*r1)/(2*d2));
    D A=sqrt((r1+r2+d)*(r1-r2+d)*(r1+r2-d)*(-r1+r2+d));
    Pt v=Pt( o1.y-o2.y , -o1.x + o2.x ) * A / (2*d2);
p1 = u + v; p2 = u - v;
    return true;
  struct Teve {
    Pt p; D ang; int add;
    Teve() {}
    Teve(Pt _a, D _b, int _c):p(_a), ang(_b), add(_c){}
    bool operator<(const Teve &a)const</pre>
    {return ang < a.ang;}
  }eve[ N * 2 ];
```

```
// strict: x = 0, otherwise x = -1
  bool disjuct( Circle& a, Circle &b, int x )
  {return dcmp( Length( a.o - b.o ) - a.r - b.r ) > x;}
  bool contain( Circle& a, Circle &b, int x )
  {return dcmp( a.r - b.r - Length( a.o - b.o ) ) > x;}
  bool contain(int i, int j){
    /* c[j] is non-strictly in c[i]. */
    return (dcmp(c[i].r - c[j].r) > 0 ||
            (dcmp(c[i].r - c[j].r) == 0 && i < j) ) &&
                 contain(c[i], c[j], -1);
  void solve(){
    for( int i = 0 ; i <= C + 1 ; i ++ )</pre>
      Area[ i ] = 0;
    for( int i = 0 ; i < C ; i ++ )</pre>
      for( int j = 0 ; j < C ; j ++</pre>
        overlap[i][j] = contain(i, j);
    for( int i = 0 ; i < C ; i ++ )</pre>
      for( int j = 0 ; j < C ; j ++ )</pre>
        g[i][j] = !(overlap[i][j] || overlap[j][i] ||
                    disjuct(c[i], c[j], -1));
    for( int i = 0 ; i < C ; i ++ ){</pre>
      int E = 0, cnt = 1;
      for( int j = 0 ; j < C ; j ++ )</pre>
        if( j != i && overlap[j][i] )
          cnt ++;
      for( int j = 0 ; j < C ; j ++ )</pre>
        if( i != j && g[i][j] ){
          Pt aa, bb;
          CCinter(c[i], c[j], aa, bb);
          D A=atan2(aa.y - c[i].o.y, aa.x - c[i].o.x);
          D B=atan2(bb.y - c[i].o.y, bb.x - c[i].o.x);
          eve[E ++] = Teve(bb, B, 1);
          eve[E ++] = Teve(aa, A, -1);
          if(B > A) cnt ++;
      if( E == 0 ) Area[ cnt ] += PI * c[i].r * c[i].r;
      else{
        sort( eve , eve + E );
        eve[E] = eve[0];
        for( int j = 0 ; j < E ; j ++ ){</pre>
          cnt += eve[j].add;
          Area[cnt] += (eve[j].p ^ eve[j + 1].p) * 0.5;
          D theta = eve[j + 1].ang - eve[j].ang;
          if (theta < 0) theta += 2.0 * PI;</pre>
          Area[cnt] +=
            (theta - sin(theta)) * c[i].r*c[i].r * 0.5;
}}}};
```

11 特殊題目

11.1 包含子字串計數

```
|// * 給一個字串s
// * 求長度為Len且有包含s的字串有幾種
// * 呼叫solve(s, len)
const int len = 1005;
int aut[len][26];
int dp[len][len];
const int mod = 1e9+7;
void prefix(string &s, vector<int> &pi) {
    for(int i=1, j=0; i<s.size(); i++) {</pre>
        while(j>0 && s[i]!=s[j]) j = pi[j-1];
        if(s[i]==s[j]) j++;
        pi[i] = j;
void automata(string &s, vector<int> &pi) {
    for(int i=0 ; i<s.size() ; i++) {</pre>
        for(int c=0 ; c<26 ; c++) {</pre>
            if(i>0 && c+'A' != s[i]) aut[i][c] = aut[pi
                 [i-1]][c];
            else aut[i][c] = i + (c + 'A'==s[i]);
        }
    }
int quai(int x, int n) {
    if(n==0) return 1;
    int mid = quai(x,n/2);
    mid = mid*mid%mod;
    if(n&1) return mid*x%mod;
```

```
return mid;
int solve(string s, int len) {
    vector<int> pi(s.size(), 0);
    prefix(s, pi);
    automata(s, pi);
    int n = s.size(), ans = quai(26, len);
    dp[0][0] = 1;
    for(int i=0 ; i<len ; i++) {</pre>
        for(int j=0 ; j<n ; j++) {</pre>
             for(int c=0 ; c<26 ; c++) {</pre>
                 dp[i+1][aut[j][c]] += dp[i][j];
                 dp[i+1][aut[j][c]] %= mod;
        }
    for(int i=0 ; i<n ; i++) ans = (ans - dp[len][i] +</pre>
        mod)%mod;
    return ans;
```

12 Python

12.1 Decimal

```
from decimal import Decimal, getcontext, ROUND_FLOOR
getcontext().prec = 250 # set precision (MAX_PREC)
getcontext().Emax = 250 # set exponent limit (MAX_EMAX)
getcontext().rounding = ROUND_FLOOR # set round floor
itwo,two,N = Decimal(0.5),Decimal(2),200
pi = angle(Decimal(-1))
```

12.2 Fraction

```
from fractions import Fraction
import math
"""專門用來表示和操作有理數,可以進行算"""
frac1 = Fraction(1)
                    # 1/1
frac2 = Fraction(1, 3) # 1/3
frac3 = Fraction(0.5) # 1/2
frac4 = Fraction('22/7') # 22/7
frac5 = Fraction(8, 16) # 自動約分為 1/2
frac9 = Fraction(22, 7)
frac9.numerator # 22
frac9.denominator # 7
x = Fraction(math.pi)
y2 = x.limit_denominator(100) # 分母限制為 100
print(y2) # 311/99
float(x) #轉換為浮點數
```

12.3 Misc