

# Module Interface Specification for Re-ProtGNN

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# 1 Revision History

Date	Version	Notes
Mar 19, 2025	1.0	Initial Draft

## 2 Symbols, Abbreviations and Acronyms

See SRS Documentation at <https://github.com/Yuanqi-X/Re-ProtGNN/blob/main/docs/SRS/SRS.pdf>.

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## 3 Introduction

The following document details the Module Interface Specifications for Re-ProtGNN, a re-implementation of an interpretable Graph Neural Network (GNN) Framework.

Complementary documents include the System Requirement Specifications and Module Guide. The full documentation and implementation can be found at <https://github.com/Yuanqi-X/Re-ProtGNN/tree/main>.

## 4 Notation

The structure of the MIS for modules comes from Hoffman and Strooper (1995), with the addition that template modules have been adapted from Ghezzi et al. (2003). The mathematical notation comes from Chapter 3 of Hoffman and Strooper (1995). For instance, the symbol  $:=$  is used for a multiple assignment statement and conditional rules follow the form  $(c_1 \Rightarrow r_1 | c_2 \Rightarrow r_2 | \dots | c_n \Rightarrow r_n)$ .

The following table summarizes the primitive data types used by Re-ProtGNN.

Data Type	Notation	Description
integer	$\mathbb{Z}$	a number without a fractional component in $(-\infty, \infty)$
natural number	$\mathbb{N}$	a number without a fractional component in $[1, \infty)$
real	$\mathbb{R}$	any number in $(-\infty, \infty)$
boolean	<code>bool</code>	Boolean value: either <code>True</code> or <code>False</code>
string	<code>str</code>	A sequence of Unicode characters
tensor	<code>Tensor</code>	A multi-dimensional array object from PyTorch
graph	<code>Data</code>	A graph object from PyTorch Geometric, with node and edge attributes
dataset	<code>Dataset</code>	A collection of graph objects for training or evaluation
dataloader	<code>DataLoader</code>	A PyTorch Geometric data loader for batching graph data
dictionary	<code>dict[K <math>\rightarrow</math> V]</code>	A mapping from keys of type <code>K</code> to values of type <code>V</code>
list	<code>list[T]</code>	A sequence of elements of type <code>T</code>
function	<code>Customized Function</code>	A self-defined callable function

Re-ProtGNN uses functions, which are defined by the data types of their inputs and outputs. Local functions are described by giving their type signature followed by their specification.



## 5 Module Decomposition

The following table is taken directly from the Module Guide document for this project.

Level 1	Level 2
Hardware-Hiding	
Behaviour-Hiding Module	Configuration Module Input Format Module Control Module Training Module Output Visualization Module
Software Decision Module	Model Module Inference Module Explanation Module Pytorch Module Pytorch Geometric Module GUI Module

Table 1: Module Hierarchy

## 6 MIS of Configuration Module

### 6.1 Module

Configuration

### 6.2 Uses

None

### 6.3 Syntax

#### 6.3.1 Exported Constants

None

#### 6.3.2 Exported Access Programs

None

### 6.4 Semantics

#### 6.4.1 State Variables

- `data_args`: `DataParser` — Stores dataset-level configuration such as name, directory, splitting strategy, and seed.
- `model_args`: `ModelParser` — Stores GNN architecture settings and prototype-related parameters.
- `train_args`: `TrainParser` — Stores training hyperparameters including learning rate, batch size, and epoch count.
- `mcts_args`: `MCTSParser` — Stores Monte Carlo Tree Search and explanation-specific rollout parameters.
- `random_seed`: `int` — Stores the global seed used for generating random numbers.

#### 6.4.2 Environment Variables

None

### 6.4.3 Access Routine Semantics

None - The state variables in this module are initialized when the system loads and are accessed directly by other modules using:

```
from utils.Configures import data.args, train.args, model.args, mcts.args
```

As such, no explicit accessor routines are exported.

### 6.4.4 Local Functions

**DataParser(name: str, dir: str, split: list[ $\mathbb{R}$ ], seed: int)  $\rightarrow$  DataParser**

- output: Returns a configuration object for dataset settings including `name`, `dir`, `split`, and `seed`.

**ModelParser(model\_name: str, hidden\_dim:  $\mathbb{N}$ , num\_prototypes:  $\mathbb{N}$ )  $\rightarrow$  ModelParser**

- output: Returns a configuration object containing the GNN model name, hidden dimension, and prototype count.

**TrainParser(batch\_size:  $\mathbb{N}$ , lr:  $\mathbb{R}$ , epochs:  $\mathbb{N}$ )  $\rightarrow$  TrainParser**

- output: Returns a configuration object with the training hyperparameters: `batch_size`, `lr`, and `epochs`.

**MCTSParser(num\_rollouts:  $\mathbb{N}$ , exploration\_const:  $\mathbb{R}$ )  $\rightarrow$  MCTSParser**

- output: Returns a configuration object specifying the number of rollouts and exploration constant for MCTS-based explanation.

## 7 MIS of Input Format Module

### 7.1 Module

dataUtils

### 7.2 Uses

PyTorch Geometric Module (15), PyTorch Module (14), Configuration Module (6), Output Visualization Module (10)

### 7.3 Syntax

#### 7.3.1 Exported Constants

None

#### 7.3.2 Exported Access Programs

Name	In	Out	Exceptions
load_dataset	-	tuple[Dataset, int, int, dict[str → DataLoader]]	FileNotFoundError, ValueError, NotImplementedError

### 7.4 Semantics

#### 7.4.1 State Variables

None

#### 7.4.2 Environment Variables

- **dataset\_dir:** str — Filesystem path to the dataset root directory, obtained from `data_args.dataset_dir` defined in the Configuration Module.
- **log\_file:** str — Path to the log file used by the `append_record()` routine exported from the Output Visualization Module.

#### 7.4.3 Access Routine Semantics

`load_dataset()`:

- transition:
  - Loads the dataset using `data_args.dataset_name` and `data_args.dataset_dir`, where `data_args` are defined in the Configuration Module.

- Logs the dataset name using `append_record(data_args.dataset_name)`, where `append_record()` is a routine exported from the Output Visualization Module
- output:
  - Returns a tuple: `(dataset, input_dim, output_dim, dataloader)` where:
    - \* `dataset`: graph dataset object loaded using `_get_dataset()`
    - \* `input_dim`: number of node features from `dataset.num_node_features`
    - \* `output_dim`: number of output classes from `dataset.num_classes`
    - \* `dataloader`: dictionary of DataLoaders split via `_get_dataloader()`
- exception:
  - `FileNotFoundError`: Raised if required dataset files are missing in the specified directory, such as missing raw `‘.pkl‘` or `‘.txt‘` files for the dataset.
  - `ValueError`: Raised if raw data files exist but are empty or malformed (e.g., missing node labels).
  - `NotImplementedError`: Raised if `data_args.dataset_name` does not match any supported dataset (i.e., not MUTAG, BA\_2Motifs, or a MoleculeNet dataset).

#### 7.4.4 Local Functions

`_get_dataset(dataset_dir: str, dataset_name: str) → Dataset`

- output: Selects an appropriate dataset loader based on `dataset_name` and returns the resulting dataset loaded from `dataset_dir`. See the Pytorch Geometric Module 15 for the type `Dataset`.

`_get_dataloader(dataset: Dataset, batch_size:  $\mathbb{N}$ , data_split_ratio: list[ $\mathbb{R}$ ]) → dict[str → DataLoader]`

- output: Splits the input `dataset` into train/eval/test sets according to `data_split_ratio`, and returns DataLoaders batched by `batch_size`. See the PyTorch Geometric Module 15 for the type `DataLoader`.

## 8 MIS of Control Module

### 8.1 Module

main

### 8.2 Uses

Configuration Module (6), Input Format Module (7), Model Module (11), Training Module (9), Inference Module (12), Explanation Module (13), PyTorch Module (14)

### 8.3 Syntax

#### 8.3.1 Exported Constants

None

#### 8.3.2 Exported Access Programs

Name	In	Out	Exceptions
main	clst: $\mathbb{R}$ , sep: $\mathbb{R}$	-	-

### 8.4 Semantics

#### 8.4.1 State Variables

None

#### 8.4.2 Environment Variables

- **dataset\_dir:** `str` — Filesystem path to the dataset root directory (from `data_args.dataset_dir`).
- **checkpoint\_dir:** `str` — Directory path for saving and loading model checkpoints, constructed using `data_args.dataset_name`.
- **device:** `str` — Device identifier used by PyTorch for model training and inference (e.g., ‘cpu’ or ‘cuda’).

#### 8.4.3 Access Routine Semantics

`main(clst, sep):`

- transition:
  - Loads the dataset and dataloaders using `load_dataset()`, which references `dataset_dir`.

- Initializes a GNN model and loss function using `setup_model(input_dim, output_dim, model_args)` from Model Module (11).
  - Constructs `checkpoint_dir := './src/checkpoint/{data_args.dataset_name}/'`.
  - Trains the model using `train(clst, sep, dataset, dataloader, gnnNets, output_dim, criterion, checkpoint_dir)` from Training Module (9).
  - Loads the best checkpoint from `checkpoint_dir`, and updates model weights using `update_state_dict()`.
  - Evaluates the trained model via `test(dataloader['test'], gnnNets, criterion)` from Inference Module (12).
  - Generates explanations using `exp_visualize(dataset, dataloader, gnnNets, output_dim)` from Explanation Module (13).
- output: None
  - exception: None

#### 8.4.4 Local Functions

None

## 9 MIS of Training Module

### 9.1 Module

Train

### 9.2 Uses

Configuration Module (6), Model Module (11), Explanation Module (13), Output Visualization Module (10), PyTorch Module (14)

### 9.3 Syntax

#### 9.3.1 Exported Constants

None

#### 9.3.2 Exported Access Programs

Name	In	Out	Exceptions
train	clst: $\mathbb{R}$ , sep: $\mathbb{R}$ , dataset: <code>-</code> Dataset, dataloader: <code>dict[str</code> <code>→ DataLoader]</code> , gnnNets: GnnNets, output_dim: $\mathbb{N}$ , cri- terion: <code>Customized Function</code> , ckpt_dir: <code>str</code>	-	None

### 9.4 Semantics

#### 9.4.1 State Variables

None

#### 9.4.2 Environment Variables

- `checkpoint_dir: str` — Path to the directory for saving model checkpoints.
- `device: str` — Target computation device, used to allocate model weights and prototype vectors.

#### 9.4.3 Access Routine Semantics

`train(clst, sep, dataset, dataloader, gnnNets, output_dim, criterion, ckpt_dir):`

- transition:



- Initializes the optimizer using parameters from `gnnNets` and `train_args`.
  - Logs statistics for `dataset` using `_log_dataset_stats(dataset)`.
  - Iteratively trains the model using batches from `dataloader['train']` with cluster/separation losses weighted by `clst` and `sep`.
  - Periodically projects prototypes onto embedding space using `_project_prototypes(gnnNets, dataset, ...)`.
  - Evaluates performance on the validation set using `_evaluate(dataloader['eval'], gnnNets, criterion)`.
  - Saves model checkpoints to `ckpt_dir`.
- output: None
  - exception: None

#### 9.4.4 Local Functions

`_evaluate(eval_dataloader: DataLoader, model: GnnNets, criterion: Customized Function) → dict[str → float]`

- transition: None
- output: Runs model evaluation on `eval_dataloader` and computes loss/accuracy basing on `criterion`. Returns a dictionary with keys 'loss' and 'acc'.

`_log_dataset_stats(dataset: Dataset) → None`

- transition: Computes average number of nodes and edges from `dataset`, and prints the result.
- output: None

`_project_prototypes(model: GnnNets, dataset: Dataset, indices: list[ $\mathbb{N}$ ], output_dim:  $\mathbb{N}$ ) → None`

- transition: Updates each prototype vector in `model` with a real example from `dataset` using `get_explanation()` from Explanation Module (13).
- output: None

## 10 MIS of Output Visualization Module

### 10.1 Module

outputUtils

### 10.2 Uses

PyTorch Module (14), PyTorch Geometric Module (15), GUI Module (16)

### 10.3 Syntax

#### 10.3.1 Exported Constants

None

#### 10.3.2 Exported Access Programs

Name	In	Out	Exceptions
ExpPlot	dataset_name: <code>str</code>	ExpPlot instance	-
draw	graph: <code>networkx.Graph</code> , nodelist: <code>list[int]</code> , figname: <code>str</code> , kwargs: <code>dict</code>	-	NotImplementedError
append_record	info: <code>str</code>	-	FileNotFoundError
save_best	ckpt_dir: <code>str</code> , epoch: <code>N</code> , gnnNets: <code>GnnNets</code> , model_name: <code>str</code> , eval_acc: $\mathbb{R}$ , is_best: <code>bool</code>	-	-

### 10.4 Semantics

#### 10.4.1 State Variables

None

#### 10.4.2 Environment Variables

- `log_file: str` — Hardcoded path to the log file: `./results/log/hyper_search`.
- `device: str` — Computation device (e.g., ‘cuda’ or ‘cpu’) used to store model after saving.

### 10.4.3 Access Routine Semantics

**ExpPlot(dataset\_name):**

- transition: None
- output: Constructs an instance for drawing explanations for `dataset_name`. Returns an `ExpPlot` object.
- Note: Please see in PyTorch Geometric Module (15) for the type `networkx.Graph`.

**draw(graph, nodelist, figname, kwargs):**

- transition: Calls the drawing routine and uses GUI Module (16) to generate and save a figure to `figname`.
- output: None
- exception: `NotImplementedError` if `dataset_name` is unsupported.

**append\_record(info):**

- transition: Writes `info` as a new line to the file located at `log_file`.
- output: None
- exception: `FileNotFoundError` if the parent directory of `log_file` does not exist.

**save\_best(ckpt\_dir, epoch, gnnNets, model\_name, eval\_acc, is\_best):**

- transition:
  - Saves model weights and training metadata to `ckpt_dir`.
  - If `is_best=True`, copies this file to `ckpt_dir`.
  - Moves model between ‘cpu’ and `device := model_args.device`.
- output: None
- exception: None

### 10.4.4 Local Functions

None

## 11 MIS of Model Module

### 11.1 Module

GnnNets

### 11.2 Uses

PyTorch Module (14), Output Visualization Module (10)

### 11.3 Syntax

#### 11.3.1 Exported Constants

None

#### 11.3.2 Exported Access Programs

Name	In	Out	Exceptions
setup_model	input_dim: $\mathbb{N}$ , output_dim: $\mathbb{N}$ , model_args: dict	tuple[GnnNets, Customized Function]	-

### 11.4 Semantics

#### 11.4.1 State Variables

None

#### 11.4.2 Environment Variables

- **device:** `str` — Target device (e.g., ‘cuda’ or ‘cpu’), used to move the model after initialization.
- **log\_file:** `str` — Path to the log file used in `append_record()`.

#### 11.4.3 Access Routine Semantics

`setup_model(input_dim, output_dim, model_args):`

- **transition:** Instantiates a GNN model with specified `input_dim`, `output_dim`, and `model_args`. Moves the model to `device`. Writes the model name to `log_file` using `append_record()`.
- **output:** A tuple containing:

- `gnnNets`: a model instance supporting GNN forward/inference
- `criterion`: a cross-entropy loss function
- exception: None

#### 11.4.4 Local Functions

None

## 12 MIS of Inference Module

### 12.1 Module

evaluation.inference

### 12.2 Uses

Model Module (11), Output Visualization Module (10), PyTorch Module (14)

### 12.3 Syntax

#### 12.3.1 Exported Constants

None

#### 12.3.2 Exported Access Programs

Name	In	Out	Exceptions
run_inference	test_dataloader: <code>DataLoader</code> , model: <code>GnnNets</code> , criterion: <code>Customized Function</code>	<code>tuple[dict[str <math>\rightarrow</math> <math>\mathbb{R}</math>], <math>\mathbb{R}^{n \times c}</math>, <math>\mathbb{N}^n</math>]</code>	None

### 12.4 Semantics

#### 12.4.1 State Variables

None

#### 12.4.2 Environment Variables

- `log_file: str` — Path to the log file where final test performance is recorded via `append_record()`.

#### 12.4.3 Access Routine Semantics

`run_inference(test_dataloader, model, criterion):`

- transition:
  - Appends the final test loss and accuracy to the `log_file` using `append_record()`.
- output:
  - Returns a tuple (`test_state`, `all_probs`, `all_preds`):

- \* `test_state`: `dict[str → ℝ]` containing keys ‘`loss`’ and ‘`acc`’.
- \* `all_probs`:  $\mathbb{R}^{n \times c}$  — class probability matrix for  $n$  test samples and  $c$  classes, obtained by passing the data in `test_dataloader` into `model`.
- \* `all_preds`:  $\mathbb{N}^n$  — vector of predicted class labels.

- `exception`: `None`

#### 12.4.4 Local Functions

`None`

## 13 MIS of Explanation Module

### 13.1 Module

Explanation

### 13.2 Uses

Configuration Module (6), Output Visualization Module (11), PyTorch Geometric Module (15), PyTorch Module (14)

### 13.3 Syntax

#### 13.3.1 Exported Constants

None

#### 13.3.2 Exported Access Programs

Name	In	Out	Exceptions
get_explanation	data: Data, gnnNet: GnnNets, prototype: $\mathbb{R}^d$	tuple[list[N], $\mathbb{R}$ , $\mathbb{R}^d$ ]	None
exp_visualize	dataset: Dataset, dataloader: dict[str → DataLoader], gnnNets: GnnNets, output_dim: N	-	FileNotFoundError

### 13.4 Semantics

#### 13.4.1 State Variables

None

#### 13.4.2 Environment Variables

- `save_dir: str` — Filesystem path for saving explanation plot images.

#### 13.4.3 Access Routine Semantics

`get_explanation(data, gnnNet, prototype):`

- `transition: None`
- `output:`



- Uses **data**, **gnnNet**, and **prototype** to invoke a Monte Carlo Tree Search (MCTS) via the local function `_mcts()`.
- MCTS explores subgraph coalitions within the graph structure of **data** and evaluates their similarity to the provided **prototype** using `_prot_similarity_scores()`.
- Returns:
  - \* **coalition**: list of node indices selected as the best explanation subgraph.
  - \* **P**: similarity score ( $\in \mathbb{R}$ ) between the selected subgraph and the **prototype**.
  - \* **embedding**: a masked subgraph embedding  $\in \mathbb{R}^{1 \times d}$  extracted by applying **gnnNet** to the subgraph induced by **coalition**.

- exception: None

**exp\_visualize(dataset, dataloader, gnnNets, output\_dim):**

- transition:
  - Computes  $K := \text{output\_dim} \times \text{model\_args.num\_prototypes\_per\_class}$  random prototype vectors of dimension  $d$ , fixed for visualization.
  - Samples 16 graphs from `dataloader['train']`.
  - For each selected graph and for each of the first 10 prototype vectors, calls `get_explanation(data, gnnNets, prototype)` to compute explanations.
  - Saves the explanations to image files in the environment variable **save\_dir**.
  - Sets **save\_dir** := `‘./results/plots/<dataset>_<model>_’` using values from `data_args.dataset_name` and `model_args.model_name`, imported from Configuration Module (6).
- output: None
- exception:
  - **FileNotFoundError**: if **save\_dir** cannot be created due to missing parent directories, invalid paths, or insufficient filesystem permissions.

#### 13.4.4 Local Functions

**\_mcts(data: Data, gnnNet: GnnNets, prototype:  $\mathbb{R}^d$ )  $\rightarrow$  tuple[list[N],  $\mathbb{R}$ ,  $\mathbb{R}^d$ ]**

- output: Applies a multi-step rollout procedure to search for the optimal node coalition in **data**, maximizing similarity to the reference vector **prototype**  $\in \mathbb{R}^d$ . Returns the selected node indices, similarity score, and final embedding.

**\_prot\_similarity\_scores(coalition: list[N], data: Data, gnnNet: GnnNets, prototype:  $\mathbb{R}^d$ )  $\rightarrow \mathbb{R}$**

- output: Computes a scalar similarity score  $\in \mathbb{R}$  between the subgraph embedding of nodes in **coalition** (produced by **gnnNet**) and the given reference vector **prototype**  $\in \mathbb{R}^d$ , based on squared Euclidean distance.

## 14 MIS of PyTorch Module

### 14.1 Module

Torch

### 14.2 Uses

None

### 14.3 Syntax

#### 14.3.1 Exported Constants

None

#### 14.3.2 Exported Access Programs

Name	In	Out	Exceptions
Tensor	shape: <code>list[int]</code> , dtype: <code>str</code>	Tensor	-
<code>cross_entropy</code>	logits: Tensor, labels: Tensor	Tensor	-
Adam	parameters: iterable, lr: $\mathbb{R}$	Optimizer	-

### 14.4 Semantics

#### 14.4.1 State Variables

None

#### 14.4.2 Environment Variables

None

#### 14.4.3 Assumptions

None

#### 14.4.4 Access Routine Semantics

**Tensor(shape, dtype):**

- output: Returns a tensor initialized with zeros of the given `shape` and `dtype`.

**cross\_entropy(logits, labels):**

- output: Computes the cross-entropy loss between `logits` and `labels`.

**Adam(parameters, lr):**

- output: Returns an Adam optimizer configured with the given **parameters** and learning rate **lr**.

#### 14.4.5 Local Functions

None

## 15 MIS of PyTorch Geometric Module

### 15.1 Module

PyG

### 15.2 Uses

Torch

### 15.3 Syntax

#### 15.3.1 Exported Constants

None

#### 15.3.2 Exported Access Programs

Name	In	Out	Exceptions
Data	x: Tensor, edge_index: Tensor	Data	-
MoleculeNet	root: str, name: str	Dataset	FileNotFoundError
DataLoader	dataset: Dataset, batch_size: N	DataLoader	-
to_networkx	data: Data	networkx.Graph	-

### 15.4 Semantics

#### 15.4.1 State Variables

None

#### 15.4.2 Environment Variables

None

### 15.4.3 Assumptions

None

### 15.4.4 Access Routine Semantics

**Data(x, edge\_index):**

- output: Constructs and returns a PyG graph object using **x** as node features and **edge\_index** as edge indices.

**MoleculeNet(root, name):**

- output: Loads the dataset specified by **name** from directory **root** and returns a **Dataset** object.
- exception: `FileNotFoundError` if **root** does not exist.

**DataLoader(dataset, batch\_size):**

- output: Returns a **DataLoader** that batches data from the given **dataset** with batch size **batch\_size**.

**to\_networkx(data):**

- output: Converts the input PyG **data** object into a NetworkX graph.

### 15.4.5 Local Functions

None

## 16 MIS of GUI Module

### 16.1 Module

Matplotlib

### 16.2 Uses

None

### 16.3 Syntax

#### 16.3.1 Exported Constants

None

### 16.3.2 Exported Access Programs

Name	In	Out	Exceptions
axis	axis_choice: <b>str</b>	-	-
title	title_sentence: <b>str</b>	-	-
save_fig	figname: <b>str</b>	-	FileNotFoundError
close	choice: <b>str</b>	-	-

## 16.4 Semantics

### 16.4.1 State Variables

None

### 16.4.2 Environment Variables

- **figure\_path**: **str** — Path where the current figure will be saved.
- **axis\_visible**: **bool** — Whether axes are displayed in the active figure.
- **figure\_title**: **str** — Title of the current figure.
- **figure\_open**: **bool** — Whether there are any open figures.

### 16.4.3 Assumptions

None.

### 16.4.4 Access Routine Semantics

**axis(axis\_choice)**:

- transition: If **axis\_choice** == 'off', sets **axis\_visible** := **False** and disables axes using `plt.axis('off')`. Otherwise sets **axis\_visible** := **True**.

**title(title\_sentence)**:

- transition: Sets **figure\_title** := **title\_sentence** and updates the title of the current figure using `plt.title()`.

**save\_fig(figname)**:

- transition: Sets **figure\_path** := **figname** and saves the current figure to the specified path using `plt.savefig(figname)`.
- exception: **FileNotFoundError** if **figname** refers to a non-existent directory.

**close(choice)**:

- transition: Closes all active figure windows using `plt.close(choice)` and sets **figure\_open** := **False**.

### 16.4.5 Local Functions

None

## References

- Carlo Ghezzi, Mehdi Jazayeri, and Dino Mandrioli. *Fundamentals of Software Engineering*. Prentice Hall, Upper Saddle River, NJ, USA, 2nd edition, 2003.
- Daniel M. Hoffman and Paul A. Strooper. *Software Design, Automated Testing, and Maintenance: A Practical Approach*. International Thomson Computer Press, New York, NY, USA, 1995. URL <http://citeseer.ist.psu.edu/428727.html>.