

CS 188: Artificial Intelligence

Neural Nets (wrap-up) and Decision Trees



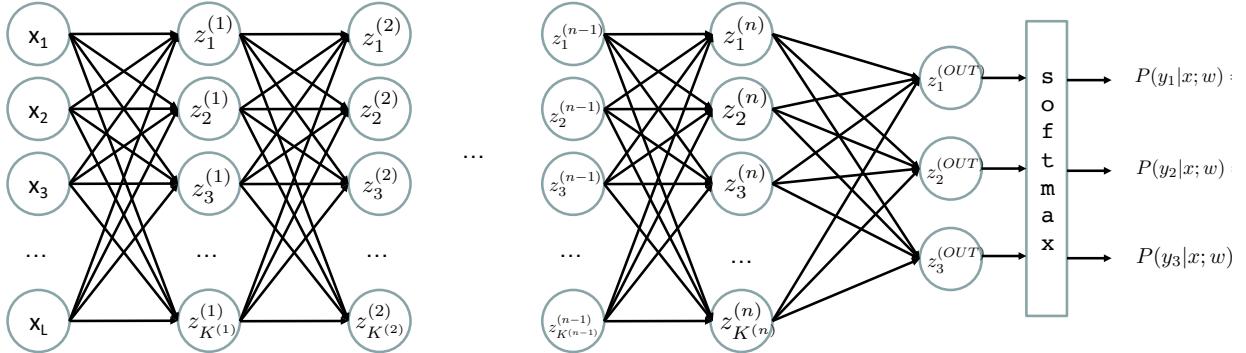
Instructors: Pieter Abbeel and Dan Klein --- University of California, Berkeley

[These slides were created by Dan Klein and Pieter Abbeel for CS188 Intro to AI at UC Berkeley. All CS188 materials are available at <http://ai.berkeley.edu>.]

Today

- Neural Nets -- wrap
- Formalizing Learning
 - Consistency
 - Simplicity
- Decision Trees
 - Expressiveness
 - Information Gain
 - Overfitting

Deep Neural Network



$$z_i^{(k)} = g\left(\sum_j W_{i,j}^{(k-1,k)} z_j^{(k-1)}\right) \quad \text{g = nonlinear activation function}$$

Deep Neural Network: Also Learn the Features!

- Training the deep neural network is just like logistic regression:

$$\max_w ll(w) = \max_w \sum_i \log P(y^{(i)}|x^{(i)}; w)$$

just w tends to be a much, much larger vector ☺

→ just run gradient ascent

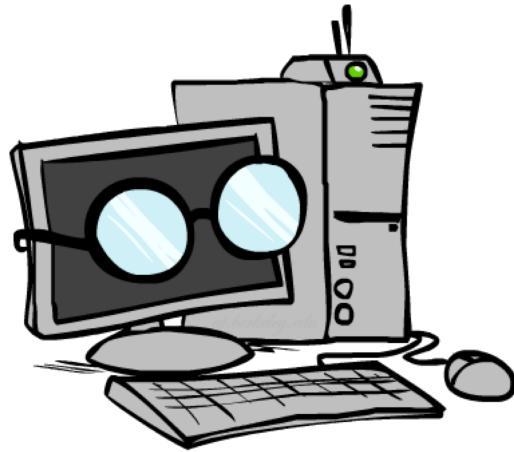
+ stop when log likelihood of hold-out data starts to decrease

Neural Networks Properties

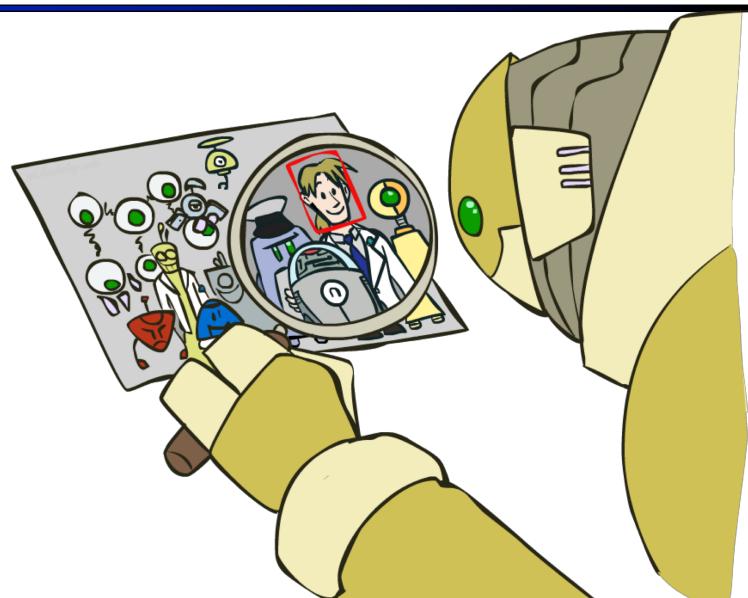
- Theorem (Universal Function Approximators). A two-layer neural network with a sufficient number of neurons can approximate any continuous function to any desired accuracy.
- Practical considerations
 - Can be seen as learning the features
 - Large number of neurons
 - Danger for overfitting
 - (hence early stopping!)

How well does it work?

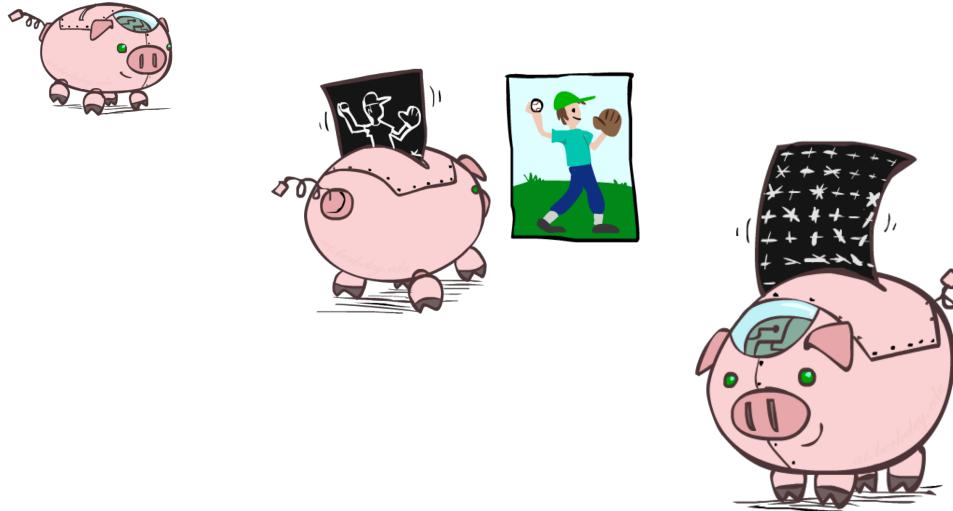
Computer Vision



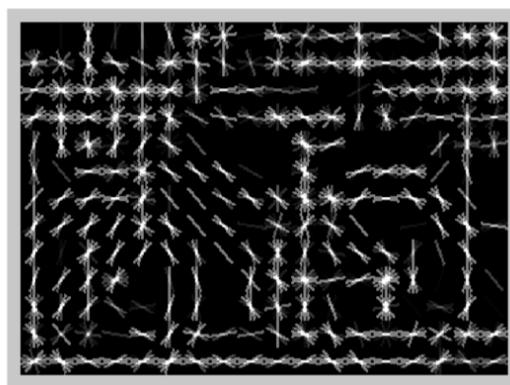
Object Detection



Manual Feature Design



Features and Generalization

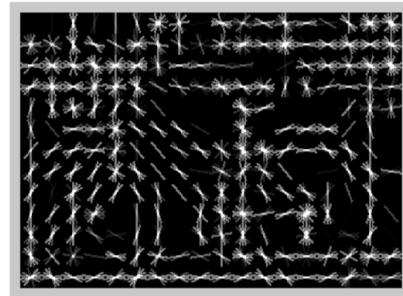


[HoG: Dalal and Triggs, 2005]

Features and Generalization



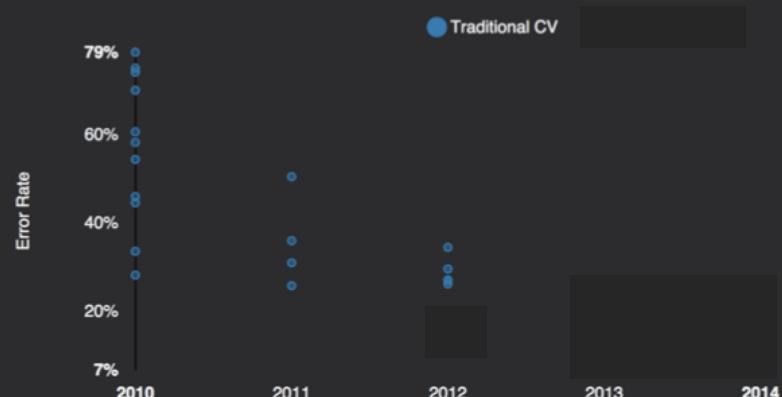
Image



HoG

Performance

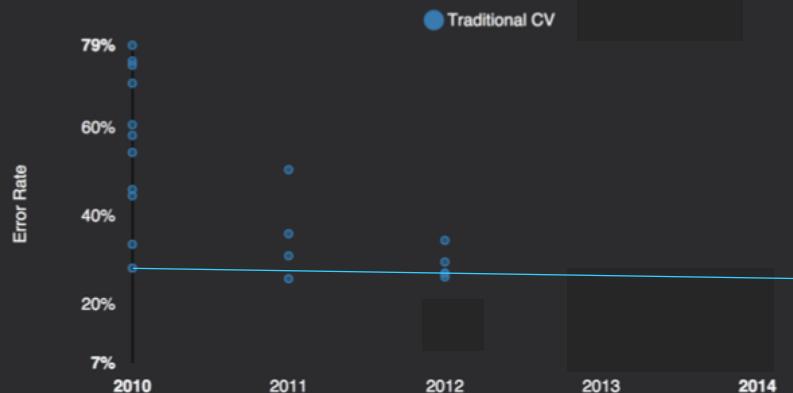
ImageNet Error Rate 2010-2014



graph credit Matt
Zeiler, Clarifai

Performance

ImageNet Error Rate 2010-2014



graph credit Matt
Zeiler, Clarifai

Performance

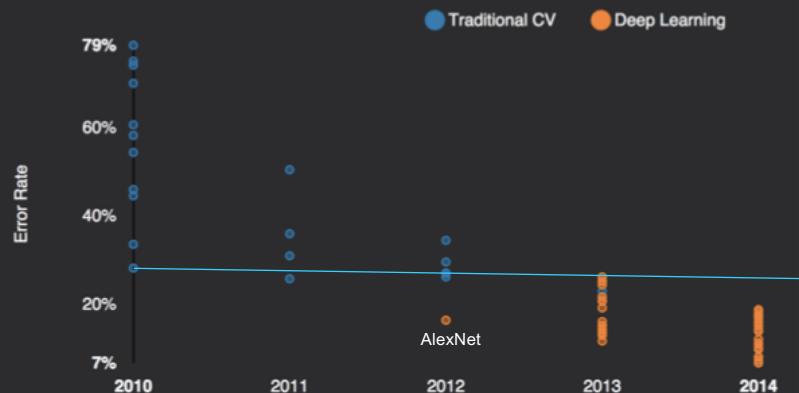
ImageNet Error Rate 2010-2014



graph credit Matt
Zeiler, Clarifai

Performance

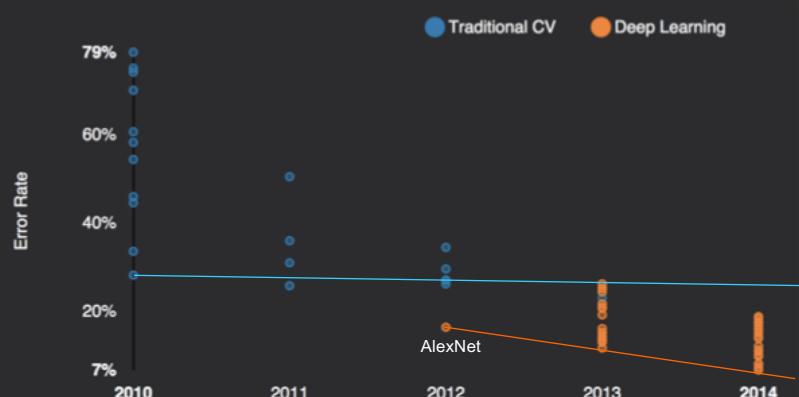
ImageNet Error Rate 2010-2014



graph credit Matt
Zeiler, Clarifai

Performance

ImageNet Error Rate 2010-2014



graph credit Matt
Zeiler, Clarifai

MS COCO Image Captioning Challenge



"man in black shirt is playing guitar."



"construction worker in orange safety vest is working on road."



"two young girls are playing with lego toy."



"boy is doing backflip on wakeboard."



"girl in pink dress is jumping in air."



"black and white dog jumps over bar."



"young girl in pink shirt is swinging on swing."



"man in blue wetsuit is surfing on wave."

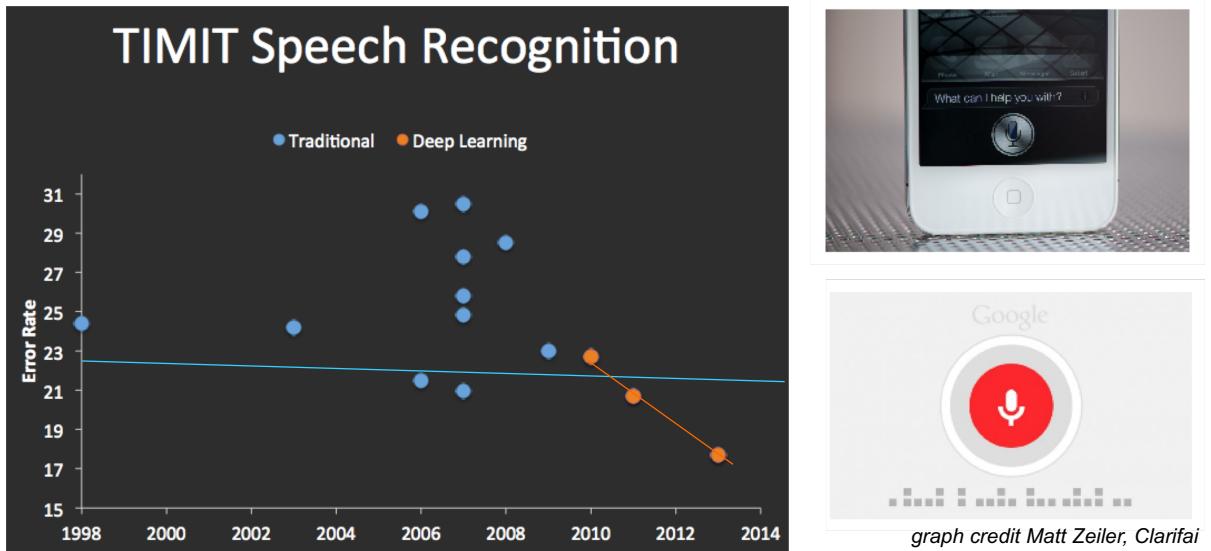
Karpathy & Fei-Fei, 2015; Donahue et al., 2015; Xu et al, 2015; many more

Visual QA Challenge

Stanislaw Antol, Aishwarya Agrawal, Jiasen Lu, Margaret Mitchell, Dhruv Batra, C. Lawrence Zitnick, Devi Parikh

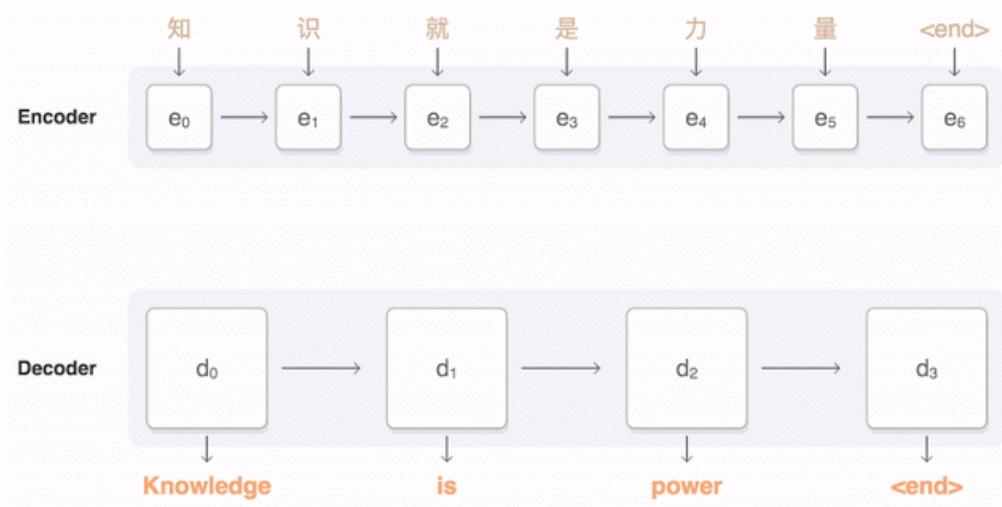
<p>What vegetable is on the plate? Neural Net: broccoli Ground Truth: broccoli</p>	<p>What color are the shoes on the person's feet ? Neural Net: brown Ground Truth: brown</p>	<p>How many school busses are there? Neural Net: 2 Ground Truth: 2</p>	<p>What sport is this? Neural Net: baseball Ground Truth: baseball</p>
<p>What is on top of the refrigerator? Neural Net: magnets Ground Truth: cereal</p>	<p>What uniform is she wearing? Neural Net: shorts Ground Truth: girl scout</p>	<p>What is the table number? Neural Net: 4 Ground Truth: 40</p>	<p>What are people sitting under in the back? Neural Net: bench Ground Truth: tent</p>

Speech Recognition



Machine Translation

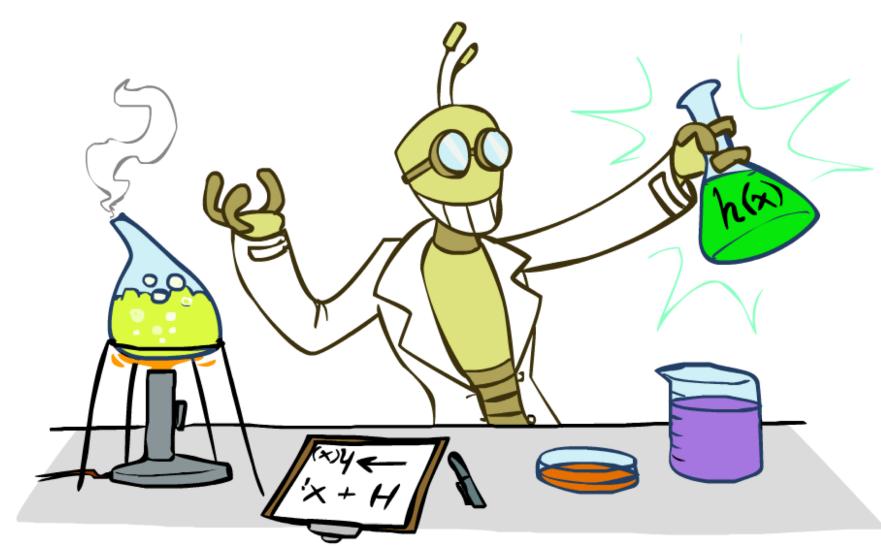
Google Neural Machine Translation (in production)



Today

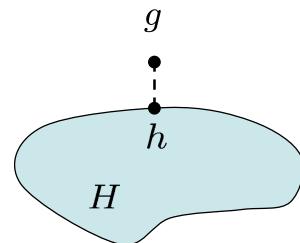
- Neural Nets -- wrap
- **Formalizing Learning**
 - Consistency
 - Simplicity
- Decision Trees
 - Expressiveness
 - Information Gain
 - Overfitting
- Clustering

Inductive Learning



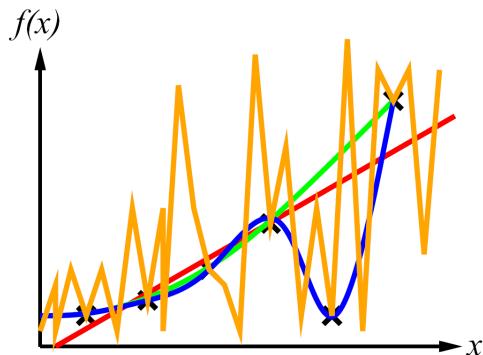
Inductive Learning (Science)

- Simplest form: learn a function from examples
 - A target function: g
 - Examples: input-output pairs $(x, g(x))$
 - E.g. x is an email and $g(x)$ is spam / ham
 - E.g. x is a house and $g(x)$ is its selling price
- Problem:
 - Given a hypothesis space H
 - Given a training set of examples x_i
 - Find a hypothesis $h(x)$ such that $h \sim g$
- Includes:
 - Classification (outputs = class labels)
 - Regression (outputs = real numbers)
- How do perceptron and naïve Bayes fit in? (H, h, g , etc.)



Inductive Learning

- Curve fitting (regression, function approximation):

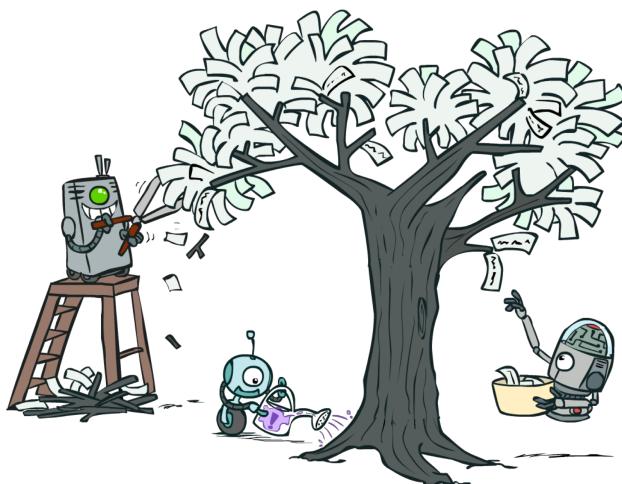


- Consistency vs. simplicity
- Ockham's razor

Consistency vs. Simplicity

- Fundamental tradeoff: bias vs. variance
- Usually algorithms prefer consistency by default (why?)
- Several ways to operationalize “simplicity”
 - Reduce the **hypothesis space**
 - Assume more: e.g. independence assumptions, as in naïve Bayes
 - Have fewer, better features / attributes: feature selection
 - Other structural limitations (decision lists vs trees)
 - **Regularization**
 - Smoothing: cautious use of small counts
 - Many other generalization parameters (pruning cutoffs today)
 - Hypothesis space stays big, but harder to get to the outskirts

Decision Trees



Reminder: Features

- Features, aka attributes
 - Sometimes: TYPE=French
 - Sometimes: $f_{\text{TYPE}=\text{French}}(x) = 1$

Example	Attributes											Target WillWait
	Alt	Bar	Fri	Hun	Pat	Price	Rain	Res	Type	Est		
X_1	T	F	F	T	Some	\$\$\$	F	T	French	0-10		T
X_2	T	F	F	T	Full	\$	F	F	Thai	30-60		F
X_3	F	T	F	F	Some	\$	F	F	Burger	0-10		T
X_4	T	F	T	T	Full	\$	F	F	Thai	10-30		T
X_5	T	F	T	F	Full	\$\$\$	F	T	French	>60		F
X_6	F	T	F	T	Some	\$\$	T	T	Italian	0-10		T
X_7	F	T	F	F	None	\$	T	F	Burger	0-10		F
X_8	F	F	F	T	Some	\$\$	T	T	Thai	0-10		T
X_9	F	T	T	F	Full	\$	T	F	Burger	>60		F
X_{10}	T	T	T	T	Full	\$\$\$	F	T	Italian	10-30		F
X_{11}	F	F	F	F	None	\$	F	F	Thai	0-10		F
X_{12}	T	T	T	T	Full	\$	F	F	Burger	30-60		T

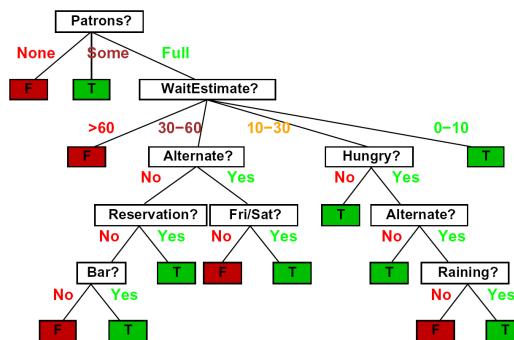
Decision Trees

- Compact representation of a function:

- Truth table
- Conditional probability table
- Regression values

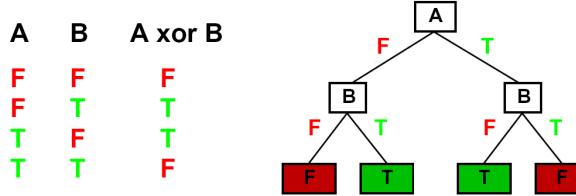
▪ True function

- Realizable: in H



Expressiveness of DTs

- Can express any function of the features



$$P(C|A, B)$$

- However, we hope for compact trees

Comparison: Perceptrons

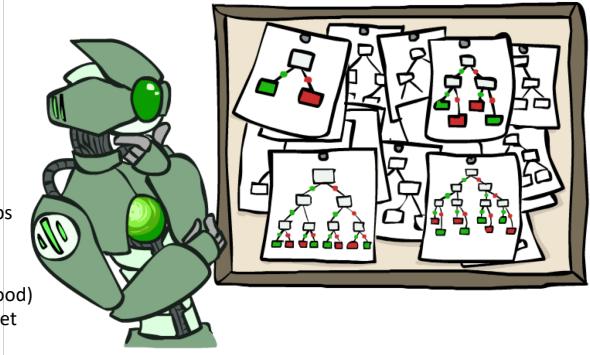
- What is the expressiveness of a perceptron over these features?

Example	Attributes										Target WillWait
	Alt	Bar	Fri	Hun	Pat	Price	Rain	Res	Type	Est	
X_1	T	F	F	T	Some	\$\$\$	F	T	French	0-10	T
X_2	T	F	F	T	Full	\$	F	F	Thai	30-60	F

- For a perceptron, a feature's contribution is either positive or negative
 - If you want one feature's effect to depend on another, you have to add a new conjunction feature
 - E.g. adding "PATRONS=full \wedge WAIT = 60" allows a perceptron to model the interaction between the two atomic features
- DTs automatically conjoin features / attributes
 - Features can have different effects in different branches of the tree!
- Difference between modeling relative evidence weighting (NB) and complex evidence interaction (DTs)
 - Though if the interactions are too complex, may not find the DT greedily

Hypothesis Spaces

- How many distinct decision trees with n Boolean attributes?
 - = number of Boolean functions over n attributes
 - = number of distinct truth tables with 2^n rows
 - = $2^{(2^n)}$
 - E.g., with 6 Boolean attributes, there are 18,446,744,073,709,551,616 trees
- How many trees of depth 1 (decision stumps)?
 - = number of Boolean functions over 1 attribute
 - = number of truth tables with 2 rows, times n
 - = $4n$
 - E.g. with 6 Boolean attributes, there are 24 decision stumps
- More expressive hypothesis space:
 - Increases chance that target function can be expressed (good)
 - Increases number of hypotheses consistent with training set (bad, why?)
 - Means we can get better predictions (lower **bias**)
 - But we may get worse predictions (higher **variance**)



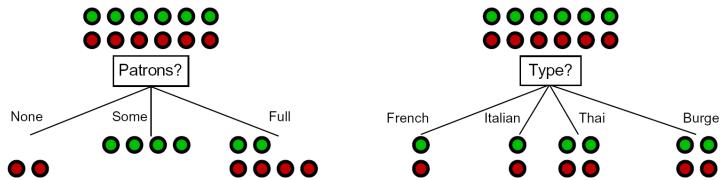
Decision Tree Learning

- Aim: find a small tree consistent with the training examples
- Idea: (recursively) choose “most significant” attribute as root of (sub)tree

```
function DTL(examples, attributes, default) returns a decision tree
    if examples is empty then return default
    else if all examples have the same classification then return the classification
    else if attributes is empty then return MODE(examples)
    else
        best ← CHOOSE-ATTRIBUTE(attributes, examples)
        tree ← a new decision tree with root test best
        for each value  $v_i$  of best do
            examples $_i$  ← {elements of examples with best =  $v_i$ }
            subtree ← DTL(examples $_i$ , attributes - best, MODE(examples))
            add a branch to tree with label  $v_i$  and subtree subtree
        return tree
```

Choosing an Attribute

- Idea: a good attribute splits the examples into subsets that are (ideally) “all positive” or “all negative”



- So: we need a measure of how “good” a split is, even if the results aren’t perfectly separated out

Entropy and Information

- Information answers questions**
 - The more uncertain about the answer initially, the more information in the answer
 - Scale: bits
 - Answer to Boolean question with prior $<1/2, 1/2>$?
 - Answer to 4-way question with prior $<1/4, 1/4, 1/4, 1/4>$?
 - Answer to 4-way question with prior $<0, 0, 0, 1>$?
 - Answer to 3-way question with prior $<1/2, 1/4, 1/4>$?
- A probability p is typical of:**
 - A uniform distribution of size $1/p$
 - A code of length $\log 1/p$

Entropy

- General answer: if prior is $\langle p_1, \dots, p_n \rangle$:

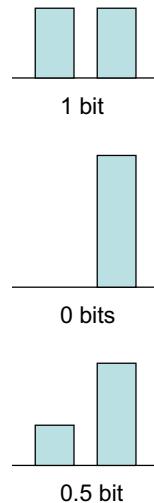
- Information is the expected code length

$$H(\langle p_1, \dots, p_n \rangle) = E_p \log_2 1/p_i$$

$$= \sum_{i=1}^n -p_i \log_2 p_i$$

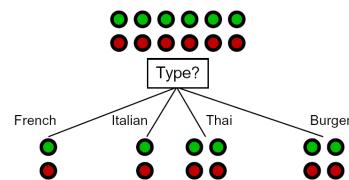
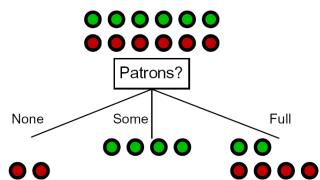
- Also called the **entropy of the distribution**

- More uniform = higher entropy
- More values = higher entropy
- More peaked = lower entropy
- Rare values almost “don’t count”



Information Gain

- Back to decision trees!
- For each split, compare entropy before and after
 - Difference is the **information gain**
 - Problem: there's more than one distribution after split!

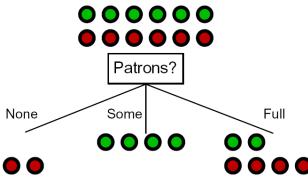


- Solution: use **expected entropy**, weighted by the number of examples



Next Step: Recurse

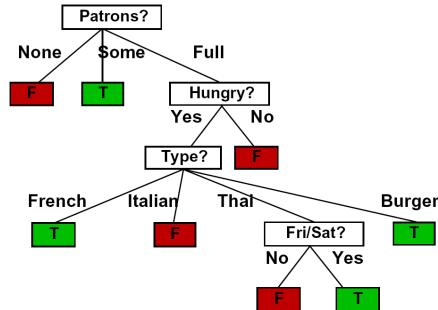
- Now we need to keep growing the tree!
- Two branches are done (why?)
- What to do under “full”?
 - See what examples are there...



Example	Attributes											Target
	Alt	Bar	Fri	Hun	Pat	Price	Rain	Res	Type	Est	WillWait	
X_1	T	F	F	T	Some	\$\$\$	F	T	French	0-10	T	
X_2	T	F	F	T	Full	\$	F	F	Thai	30-60	F	
X_3	F	T	F	F	Some	\$	F	F	Burger	0-10	T	
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X_9	F	T	T	F	Full	\$	T	F	Burger	>60	F	
X_{10}	T	T	T	T	Full	\$\$\$	F	T	Italian	10-30	F	
X_{11}	F	F	F	F	None	\$	F	F	Thai	0-10	F	
X_{12}	T	T	T	T	Full	\$	F	F	Burger	30-60	T	

Example: Learned Tree

- Decision tree learned from these 12 examples:



- Substantially simpler than “true” tree
 - A more complex hypothesis isn’t justified by data
- Also: it’s reasonable, but wrong

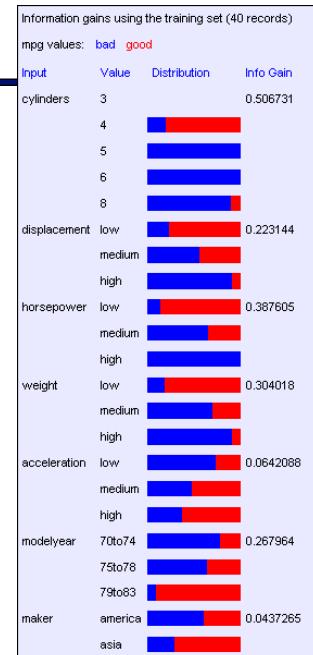
Example: Miles Per Gallon

40 Examples

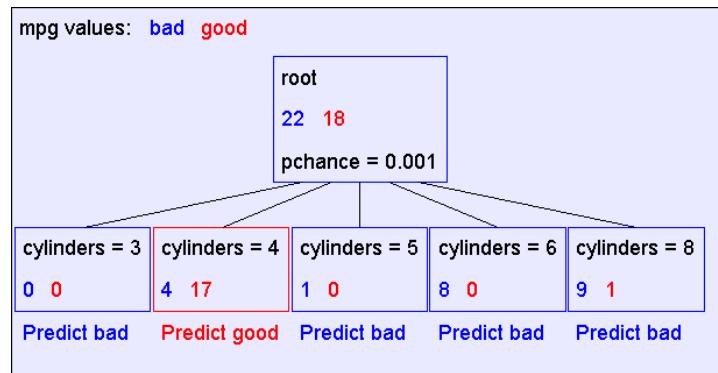
mpg	cylinders	displacement	horsepower	weight	acceleration	modelyear	maker
good	4	low	low	low	high	75to78	asia
bad	6	medium	medium	medium	medium	70to74	america
bad	4	medium	medium	medium	low	75to78	europe
bad	8	high	high	high	low	70to74	america
bad	6	medium	medium	medium	medium	70to74	america
bad	4	low	medium	low	medium	70to74	asia
bad	4	low	medium	low	low	70to74	asia
bad	8	high	high	high	low	75to78	america
:	:	:	:	:	:	:	:
:	:	:	:	:	:	:	:
:	:	:	:	:	:	:	:
bad	8	high	high	high	low	70to74	america
good	8	high	medium	high	high	79to83	america
bad	8	high	high	high	low	75to78	america
good	4	low	low	low	low	79to83	america
bad	6	medium	medium	medium	high	75to78	america
good	4	medium	low	low	low	79to83	america
good	4	low	low	medium	high	79to83	america
bad	8	high	high	high	low	70to74	america
good	4	low	medium	low	medium	75to78	europe
bad	5	medium	medium	medium	medium	75to78	europe

Find the First Split

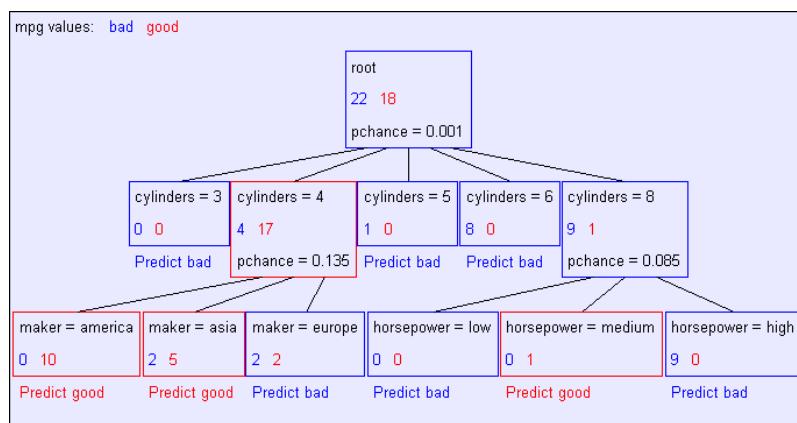
- Look at information gain for each attribute
- Note that each attribute is correlated with the target!
- What do we split on?



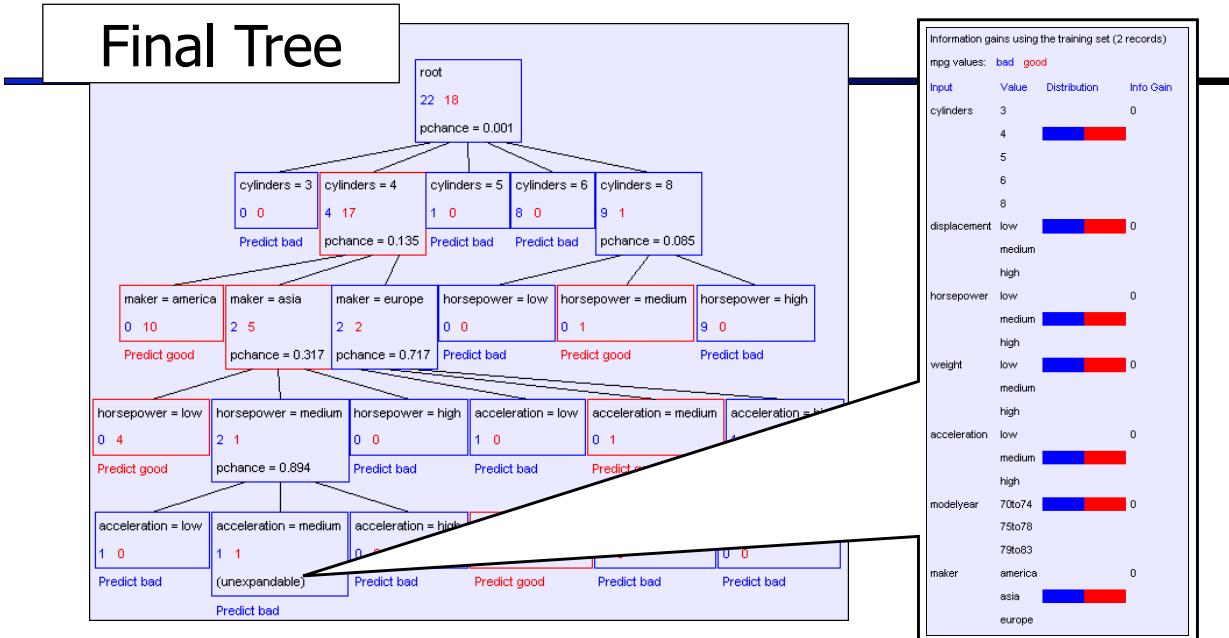
Result: Decision Stump



Second Level



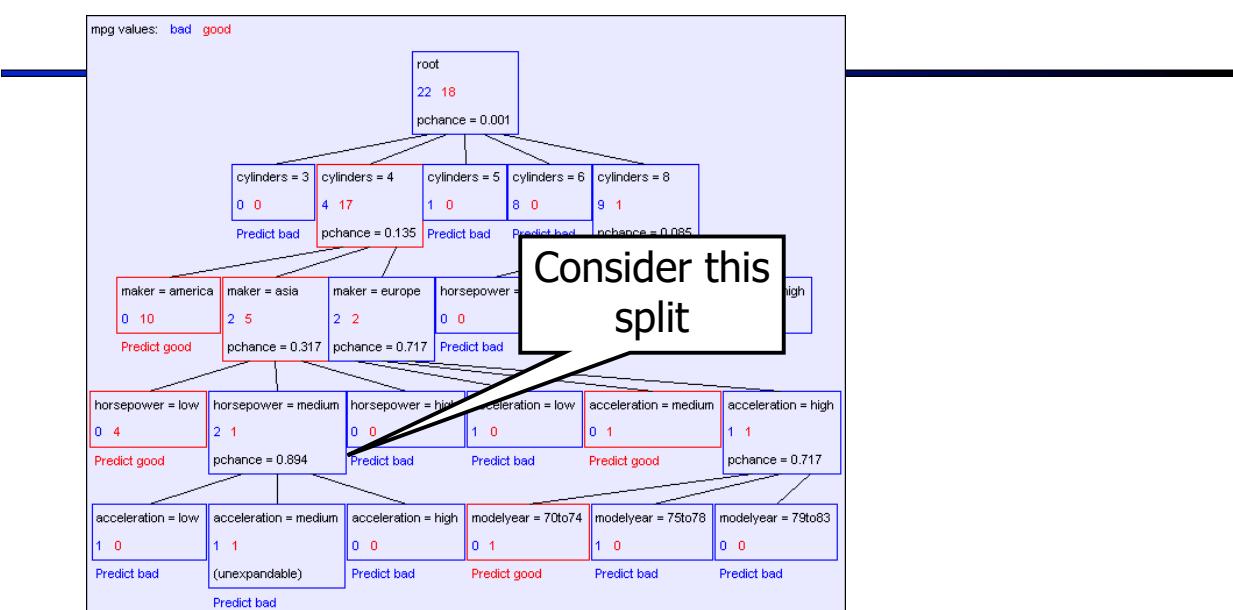
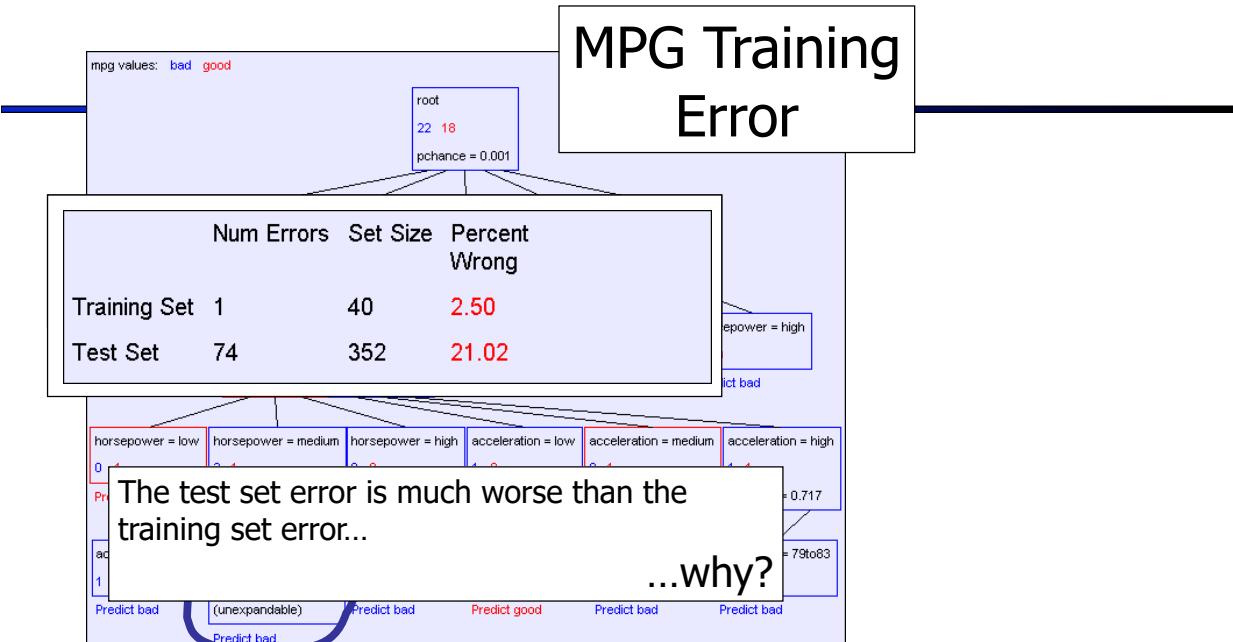
Final Tree



Reminder: Overfitting

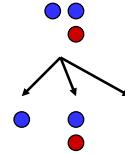
- **Overfitting:**
 - When you stop modeling the patterns in the training data (which generalize)
 - And start modeling the noise (which doesn't)

- **We had this before:**
 - Naïve Bayes: needed to smooth
 - Perceptron: early stopping



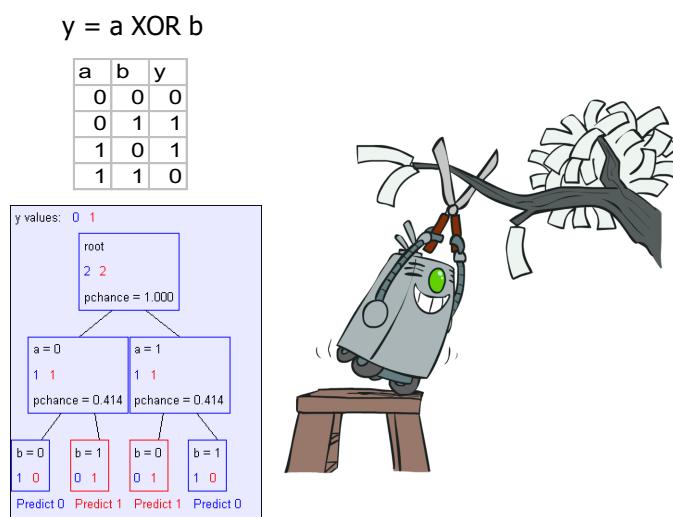
Significance of a Split

- Starting with:
 - Three cars with 4 cylinders, from Asia, with medium HP
 - 2 bad MPG
 - 1 good MPG
- What do we expect from a three-way split?
 - Maybe each example in its own subset?
 - Maybe just what we saw in the last slide?
- Probably shouldn't split if the counts are so small they could be due to chance
- A chi-squared test can tell us how likely it is that deviations from a perfect split are due to chance*
- Each split will have a significance value, p_{CHANCE}



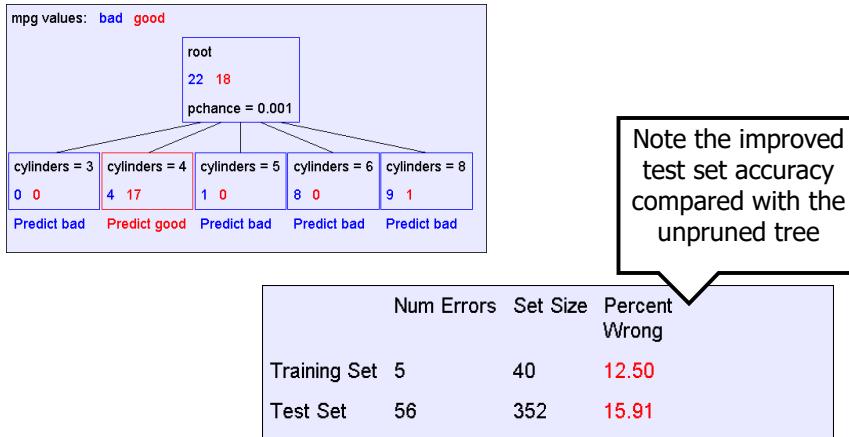
Keeping it General

- Pruning:
 - Build the full decision tree
 - Begin at the bottom of the tree
 - Delete splits in which $p_{CHANCE} > \text{Max}P_{CHANCE}$
 - Continue working upward until there are no more prunable nodes
 - Note: some chance nodes may not get pruned because they were “redeemed” later



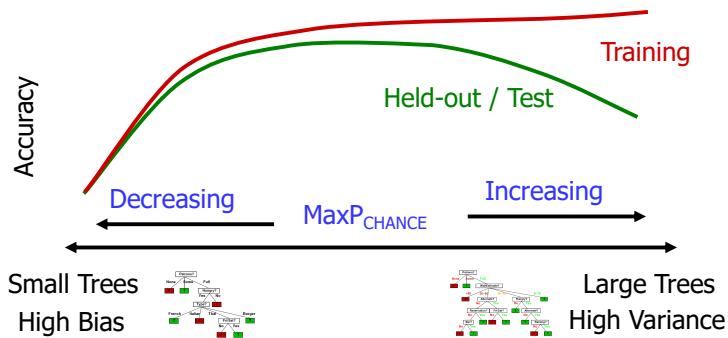
Pruning example

- With $\text{MaxP}_{\text{CHANCE}} = 0.1$:



Regularization

- $\text{MaxP}_{\text{CHANCE}}$ is a regularization parameter
- Generally, set it using held-out data (as usual)



Two Ways of Controlling Overfitting

- Limit the hypothesis space
 - E.g. limit the max depth of trees
 - Easier to analyze
- Regularize the hypothesis selection
 - E.g. chance cutoff
 - Disprefer most of the hypotheses unless data is clear
 - Usually done in practice

Next Lecture: Applications!
