

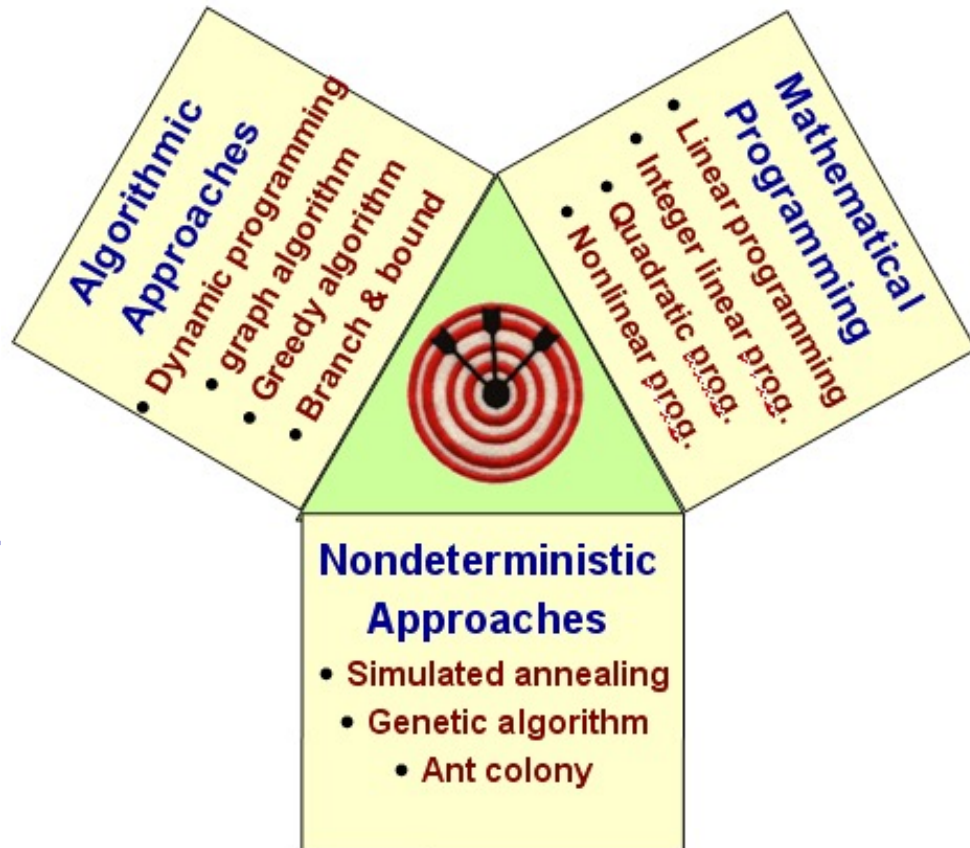
Unit 2: EDA Paradigms & Complexity

- Course contents:

- Computational Complexity
- EDA paradigms: Algorithms, Frameworks, Methodology

- Readings

- W&C&C: Chapter 4
- S&Y: Appendix A



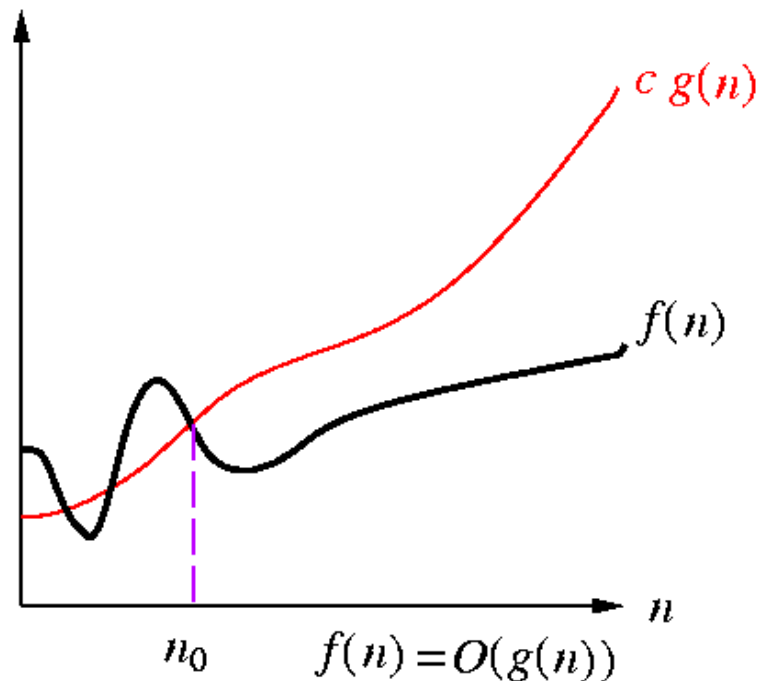
Why Does Complexity Matter?

- To characterize the efficiency/hardness of problem solving
- Have a better idea on how to come up with good algorithms
 - Algorithm: a well-defined procedure transforming some *input* to a desired *output* in **finite** computational resources in *time* and *space*.
- Runtime comparison: assume 1 BIPS (Billion Instructions Per Sec.), 1 instruction/operation.

Time	Big-Oh	$n = 10$	$n = 100$	$n = 10^4$	$n = 10^6$	$n = 10^8$
500	$O(1)$	$5 \cdot 10^{-7}$ sec	$5 \cdot 10^{-7}$ sec	$5 \cdot 10^{-7}$ sec	$5 \cdot 10^{-7}$ sec	$5 \cdot 10^{-7}$ sec
$3n$	$O(n)$	$3 \cdot 10^{-8}$ sec	$3 \cdot 10^{-7}$ sec	$3 \cdot 10^{-5}$ sec	0.003 sec	0.3 sec
$n \lg n$	$O(n \lg n)$	$3 \cdot 10^{-8}$ sec	$6 \cdot 10^{-7}$ sec	$1 \cdot 10^{-4}$ sec	0.018 sec	2.5 sec
n^2	$O(n^2)$	$1 \cdot 10^{-7}$ sec	$1 \cdot 10^{-5}$ sec	0.1 sec	16.7 min	116 days
n^3	$O(n^3)$	$1 \cdot 10^{-6}$ sec	0.001 sec	16.7 min	31.7 yr	∞
2^n	$O(2^n)$	$1 \cdot 10^{-6}$ sec	$4 \cdot 10^{11}$ cent.	∞	∞	∞
$n!$	$O(n!)$	0.003 sec	∞	∞	∞	∞

O: Upper Bounding Function

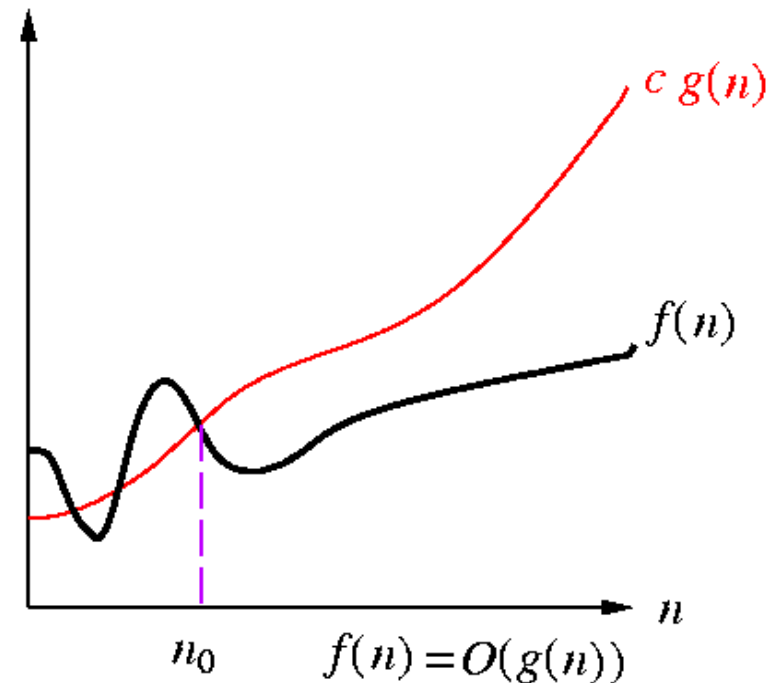
- **Def:** $f(n) = O(g(n))$ if $\exists c > 0$ and $n_0 > 0$ such that $0 \leq \mathbf{f(n)} \leq \mathbf{cg(n)}$ for all $n \geq n_0$.
 - Examples: $2n^2 + 3n = O(n^2)$, $2n^2 = O(n^3)$, $3n \lg n = O(n^2)$
- Intuition: $f(n)$ “ \leq ” $g(n)$ when we ignore constant multiples and small values of n .



Big-O Notation

- “An algorithm has worst-case running time $O(f(n))$ ”: there is a constant c s.t. for every n big enough, **every execution** on an input of size n takes **at most** $cf(n)$ time.
- Only the dominating term needs to be kept while constant coefficients are immaterial.

- e.g.,
 $0.3n^2 = O(n^2)$,
 $3n^2 + 152n + 1777 = O(n^2)$,
 $n^2 \lg n + 3n^2 = O(n^2 \lg n)$
- The following are correct but not used
 $3n^2 = O(n^2 \lg n)$
 $3n^2 = O(0.1n^2)$
 $3n^2 = O(n^2 + n)$

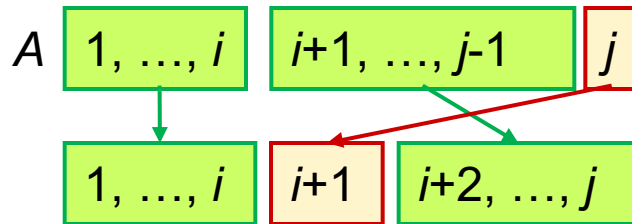


Computational Complexity

- **Computational complexity**: an abstract measure of the time and space necessary to execute an algorithm as function of its “**input size**”.
- Input size examples:
 - sort n words of bounded length $\Rightarrow n$
 - the input is the integer $n \Rightarrow \lg n$
 - the input is the graph $G(V, E) \Rightarrow |V|$ and $|E|$
- **Time complexity** is expressed in *elementary computational steps* (e.g., an addition, multiplication, pointer indirection).
- **Space Complexity** is expressed in *memory locations* (e.g. bits, bytes, words).

Example: Insertion Sort

- Idea:
 - Insert a number $A[j]$ into a sorted sequence with $j-1$ numbers
 - Result in a sorted sequence with j numbers



Time complexity?

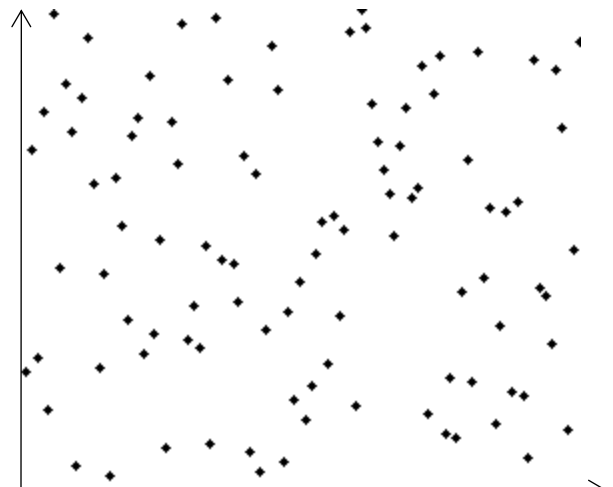
InsertionSort(A)

```
1. for  $j = 2$  to  $\text{length}[A]$  do
2.    $\text{key} = A[j]$ 
3.   // Insert  $A[j]$  into the sorted sequence  $A[1..j-1]$ 
4.    $i = j-1$ 
5.   while  $i > 0$  and  $A[i] > \text{key}$  do
6.      $A[i+1] = A[i]$ 
7.      $i = i-1$ 
8.    $A[i+1] = \text{key}$ 
```

$O(j^2)$

$O(j)$

value



index

http://en.wikipedia.org/wiki/Image:Insertion_sort_animation.gif

Amortized Analysis

- **Why Amortized Analysis?**
 - Find a tight bound of a sequence of data structure operations.
- No probability involved, guarantees the **average performance of each operation in the worst case**
- Three popular methods
 - Aggregate method
 - Accounting method
 - Potential method

Methods for Amortized Analysis

- **Aggregate** method
 - n operations take $T(n)$ time.
 - Average cost of an operation is $T(n)/n$ time.
- **Accounting** method
 - Charge each type of operation an amortized cost.
 - Store the overcharge of early operations as “prepaid credit” in “bank.”
 - Use the credit for later operations.
 - **Must guarantee nonnegative balance at all time**
- **Potential** method
 - View “prepaid credit” as “potential energy.”

Aggregate Method: Stack and MULTIPOP

- n operations take $T(n)$ time \Rightarrow average cost of an operation is $T(n)/n$ time.
- Consider a sequence of n PUSH, POP, and MULTIPOP operations on an initially empty stack.
 - Worst-case analysis: a MULTIPOP operation takes $O(n)$.
 - Aggregate method: Any sequence of n PUSH, POP, MULTIPOP costs at most $O(n)$ time (**why?**) \Rightarrow amortized cost of an operation: $O(n)/n = O(1)$.

```
Multipop(S, k)
1. while not Stack-Empty(S) and  $k > 0$  do
2.   Pop(S)
3.    $k \leftarrow k-1$ 
```

top \rightarrow 23
17
6
39
10
47

(a)

top \rightarrow 10
47

(b)

(c)

Mark P.-| Multipop(S, 4) Multipop(S, 7)

因為一個堆疊S如果是空的，就不能執行pop了，也就是說可以pop或multi-pop的元素個數不會超過S中push進去的元素個數

$$\text{所以 } n_{pop} + n_{multi-pop} \leq n_{push}$$

假設 $T(n)$ 是執行 n 個操作的時間複雜度上限

$$T(n) = O(1) \times n_{push} + O(1) \times n_{pop} = O(n)$$

所以堆疊一個操作的平攤成本為 $O(n)/n = O(1)$

Accounting Method

記帳法(Accounting method) [編輯]

執行花費較低的operations時先存credit未雨綢繆, 供未來花費較高的operations使用

對每個操作定義一個合法的平攤成本(amortized cost) 假設 c_i 為第 i 個操作的actual cost, \hat{c}_i 為第 i 個操作的amortized cost

若 $c_i < \hat{c}_i$, 則 $\text{credit} = \hat{c}_i - c_i$, 我們把credit存起來(deposited), 未來可以提取(withdraw) 若 $c_i > \hat{c}_i$, 則提取credit

設定每個操作的平攤成本(amortized cost)後, 要做valid check確保credit不可以是0, 也就是說
$$\sum_{k=1}^n \hat{c}_i \geq \sum_{k=1}^n c_i$$

我們假設S.push(x), S.pop(), S.multi-pop(k)的amortized cost分別為2, 0, 0, 如下表所示

操作(operation)	actual cost c_i	amortized cost \hat{c}_i
S.push(x)	1	2
S.pop()	1	0
S.multi-pop(k)	$O(\min(S , k))$	0

credit = 2-1 = 1 --> 每次push都會存入\$1

只要存入的總credit > 0, 其餘operation就不用再有額外花費
因此這邊的pop的amortize cost = 0

看每個操作的amortize cost就是看每個操作取出的credit為多少-->每次pop都取出credit 1, 因此amortize cost 就是O(1)

Valid Check

$$\text{證明: } \sum_{k=1}^n \hat{c}_i \geq \sum_{k=1}^n c_i$$

proof:

push進入堆疊S的元素會存入credit \$1

pop(S), multi-pop(S, k) 會取出這些元素的credit \$1

因此每個操作的平攤成本是O(1)

Potential Method

- Represent the prepaid work as “potential” that can be released to pay for future operations.
 - Potential is associated with the whole data structure, not with specific items in the data structure. (cf. accounting method)
- The potential method:
 - D_0 : initial data structure
 - D_i : data structure after applying the i th operation to D_{i-1}
 - c_i : actual cost of the i th operation
 - Define the potential function $\Phi : D_i \rightarrow \mathbb{R}$.
 - Amortized cost \hat{c}_i , $\hat{c}_i = c_i + \Phi(D_i) - \Phi(D_{i-1})$.

$$\begin{aligned}\sum_{i=1}^n \hat{c}_i &= \sum_{i=1}^n (c_i + \Phi(D_i) - \Phi(D_{i-1})) \\ &= \sum_{i=1}^n c_i + \Phi(D_n) - \Phi(D_0)\end{aligned}$$

- Pick $\Phi(D_n) \geq \Phi(D_0)$ to make $\sum_{i=1}^n \hat{c}_i \geq \sum_{i=1}^n c_i$
- Often define $\Phi(D_0) = 0$ and then show that $\Phi(D_i) \geq 0$, $\forall i$.

Potential Method: Stack Operations

位能法(Potential method) [編輯]

定義一個位能函數(potential function) $\Phi(D)$ ，將資料結構D(例如: 堆疊)的狀態對應到一個實數

D_0 : 資料結構D的初始狀態

D_i : 資料結構D經過*i*個操作後的狀態

c_i : 第*i*個操作的actual cost

\hat{c}_i : 第*i*個操作的amortized cost

定義 $\hat{c}_i = c_i + \Phi(D_i) - \Phi(D_{i-1})$

$$\sum_{k=1}^n \hat{c}_i = \sum_{k=1}^n (c_i + \Phi(D_i) - \Phi(D_{i-1})) = \left(\sum_{k=1}^n c_i \right) + \Phi(D_n) - \Phi(D_0)$$

為了滿足
$$\sum_{k=1}^n \hat{c}_i \geq \sum_{k=1}^n c_i$$

我們定義 $\Phi(D_n) - \Phi(D_0) \geq 0$ ，通常令 $\Phi(D_0) = 0$ 和 $\Phi(D_n) \geq 0$

我們定義位能函數 $\Phi(D)$ 為執行 i 個操作後，堆疊內的元素個數

$\Phi(D_0) = 0$ ，因為堆疊一開始是空的

$\Phi(D_i) \geq 0$ ，因為堆疊的元素個數一定 ≥ 0

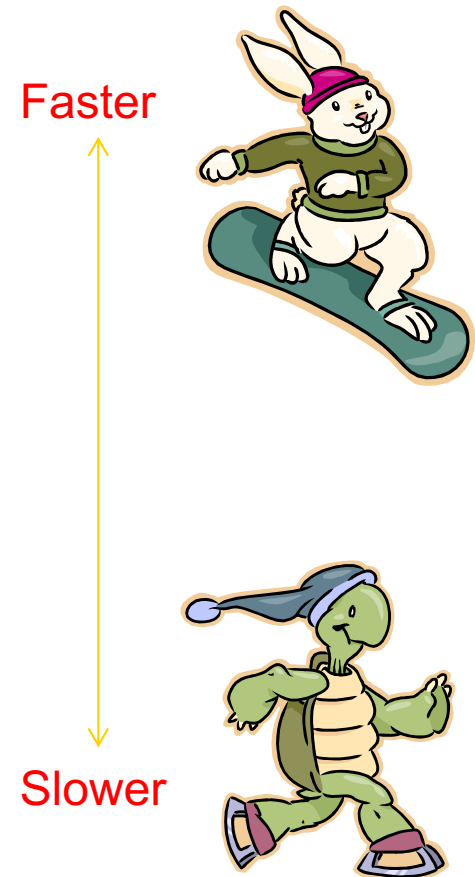
計算堆疊 S 每一個操作的平攤成本

操作(operation)	平攤成本(amortized cost) \hat{c}_i
S.push(x)	$\hat{c}_i = c_i + \Phi(D_i) - \Phi(D_{i-1}) = 1 + (S + 1) - S = 2$
S.pop()	$\hat{c}_i = c_i + \Phi(D_i) - \Phi(D_{i-1}) = 1 + (S - 1) - S = 0$
S.multi-pop(k)	$\hat{c}_i = c_i + \Phi(D_i) - \Phi(D_{i-1}) = k + (S - k) - S = k - k = 0$

總平攤成本 $\sum_{k=1}^n \hat{c}_i = 2 \times n_{push} = O(n)$ ，所以堆疊單一個操作的平攤成本是 $O(n)/n = O(1)$

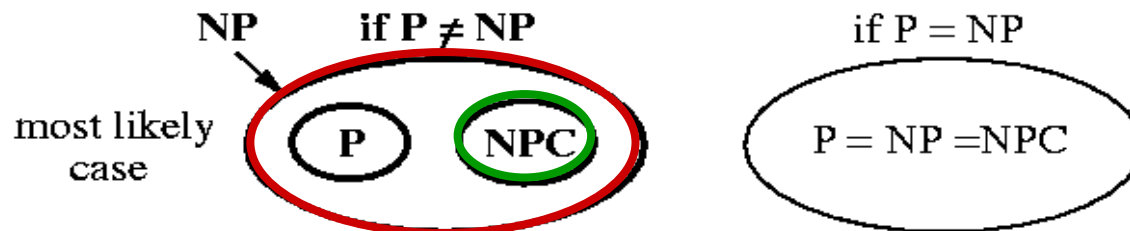
Asymptotic Functions

- Polynomial-time complexity: $O(n^k)$, where n is the **input size** and k is a constant.
- Example polynomial functions:
 - 999: constant
 - $\lg n$: logarithmic
 - \sqrt{n} : sublinear
 - n : linear
 - $n \lg n$: loglinear
 - n^2 : quadratic
 - n^3 : cubic
- Example non-polynomial functions
 - $2^n, 3^n$: exponential
 - $n!$: factorial



Complexity Classes

- **Class P**: class of problems that can be **solved** in polynomial time in the **size of input**.
 - Edmonds: Problems in P are considered **tractable**.
- **Class NP (Nondeterministic Polynomial)**: class of problems whose solutions can be **verified** in polynomial time in the size of input.
 - $P \subset NP$ or $P = NP$?
- **Class NP-complete (NPC)**: Any NPC problem can be solved in polynomial time \rightarrow all problems in NP can be solved in polynomial time (i.e., $P = NP$).



Coping with a “Tough” Problem: **Trilogy I**



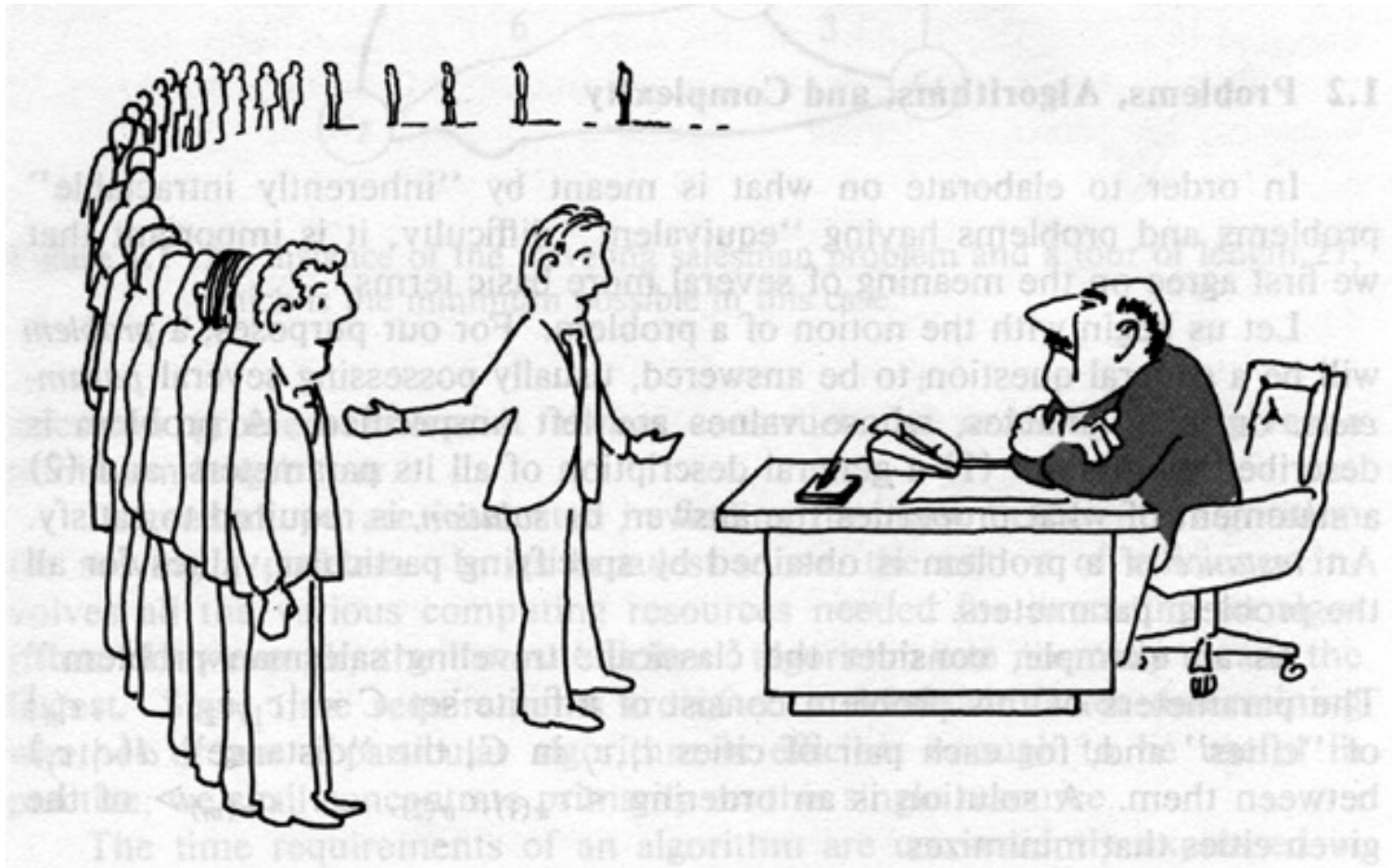
“I can’t find an efficient algorithm.
I guess I’m just too dumb.”

Coping with a “Tough” Problem: **Trilogy II**



“I can’t find an efficient algorithm,
because no such algorithm is possible!”

Coping with a “Tough” Problem: **Trilogy III**



“I can’t find an efficient algorithm,
but neither can all these famous people.”

Algorithmic Paradigms

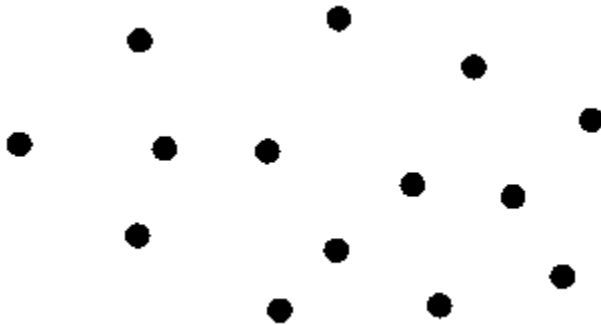
- **Exhaustive search**: Search the entire solution space
- **Branch and bound**: Search with pruning
- **Greedy**: Pick a locally optimal solution at each step
- **Dynamic programming**: if subproblems are **not independent**
- **Divide-and-conquer** (a.k.a. **hierarchical**): Divide a problem into subproblems (small and similar), solve subproblems, and then combine the solutions of subproblems
- **Mathematical programming**: Solve an objective function under constraints
- **Local search**: Move from solution to solution in the search space until a solution deemed optimal is found or a time bound is elapsed
- **Probabilistic**: Make some choices randomly (or pseudo-randomly)
- **Reduction**: Transform into a known and optimally solved problem

Algorithm Types

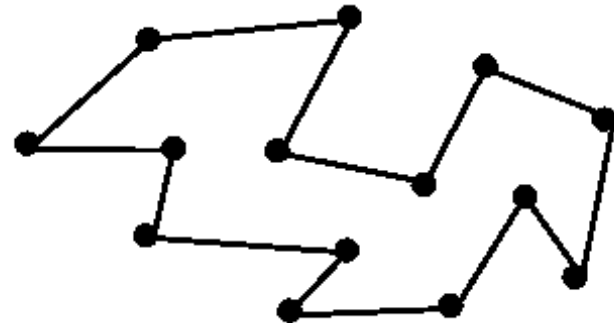
- Algorithms usually used for P problems
 - Exhaustive search
 - Branch and bound
 - Divide-and-conquer (a.k.a. hierarchical)
 - Dynamic programming
 - Mathematical programming
- Algorithms usually used for NP (but not P) problems
(strategy: not seeking an “optimal solution”, but a “good” one)
 - Approximation
 - Pseudo-polynomial time: polynomial form, but NOT to input size
 - Restriction: restrict the problem to a special case that is in P
 - Exhaustive search/branch and bound
 - Local search: simulated annealing, genetic algorithm, ant colony
 - Heuristics: greedy, ... etc

The Traveling Salesman Problem (TSP)

- **Instance:** a set of n cities, a distance between each pair of cities, and a bound B .
- **Question:** is there a route that starts and ends at a given city, visits every city exactly once, and has total distance $\leq B$?



A TSP instance



A TSP solution

NP vs. P

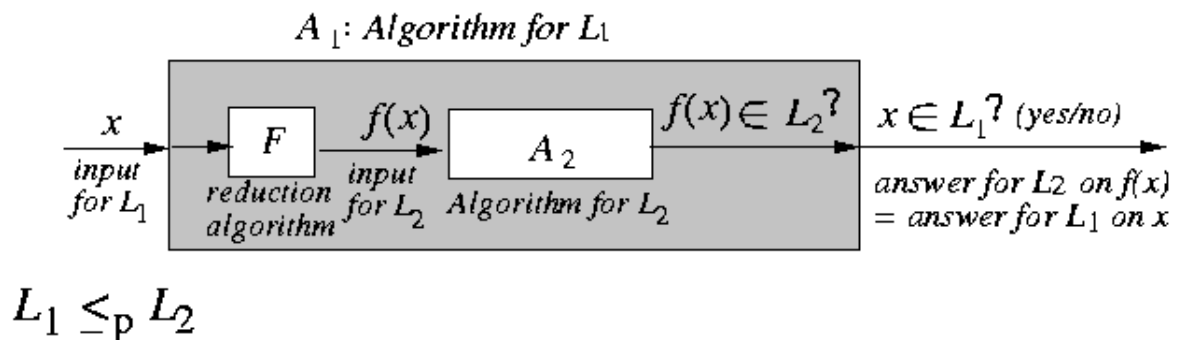
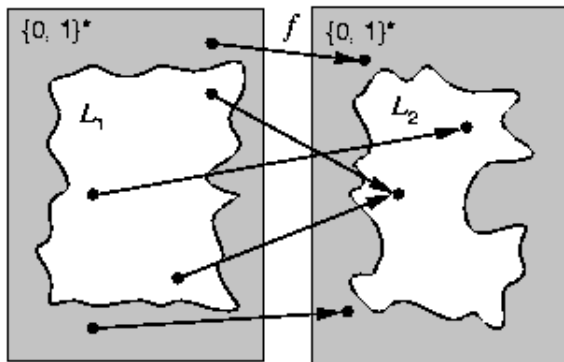
- TSP \in NP.
 - Need to **check** a solution (tour) in polynomial time.
 - Guess a tour.
 - Check if the tour visits every city exactly once, returns to the start, and total distance $\leq B$.
- TSP \in P?
 - Need to solve (find a tour) in polynomial time.
 - Still unknown if TSP \in P.

Decision Problems and NP-Completeness

- **Decision problems:** those having yes/no answers.
 - TSP: Given a set of cities, distance between each pair of cities, and a bound B , **is there a route** that starts and ends at a given city, visits every city exactly once, and has total distance at most B ?
- **Optimization problems:** those finding a legal configuration such that its cost is minimum (or maximum).
 - TSP: Given a set of cities and that distance between each pair of cities, **find the distance of a “minimum route”** that starts and ends at a given city and visits every city exactly once.
- Could apply binary search on decision problems to obtain solutions to optimization problems.
- NP-completeness is associated with decision problems.

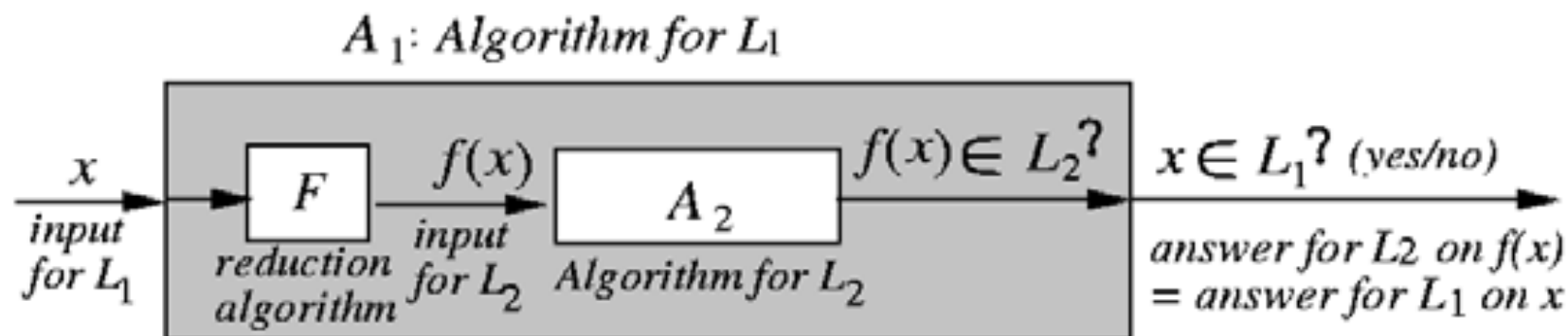
Polynomial-time Reduction

- **Motivation:** Let L_1 and L_2 be two decision problems.
Suppose algorithm A_2 can solve L_2 . Can we use A_2 to solve L_1 ?
- **Polynomial-time reduction f from L_1 to L_2 :** $L_1 \leq_p L_2$
 - f reduces input for L_1 into an input for L_2 s.t. the reduced input is a “yes” input for L_2 iff the original input is a “yes” input for L_1 .
 - $L_1 \leq_p L_2$ if \exists polynomial-time computable function $f: \{0, 1\}^* \rightarrow \{0, 1\}^*$ s.t. $x \in L_1$ iff $f(x) \in L_2$, $\forall x \in \{0, 1\}^*$.
 - L_2 is at least as hard as L_1 .
- f is computable in polynomial time.



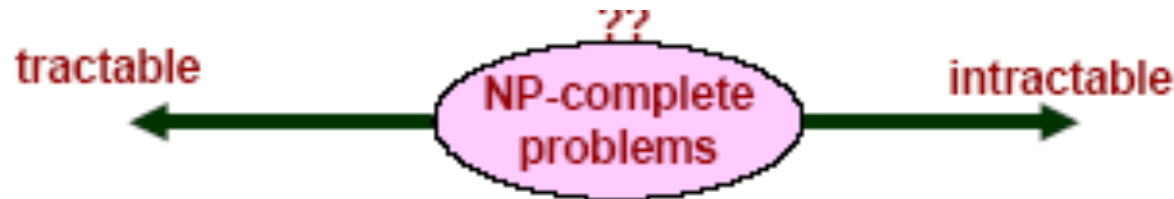
Significance of Reduction

- Significance of $L1 \leq_p L2$:
 - \exists polynomial-time algorithm for $L2 \Rightarrow \exists$ polynomial-time algorithm for $L1$ ($L2 \in P \Rightarrow L1 \in P$).
 - polynomial-time algorithm for $L1 \Rightarrow$ polynomial-time algorithm for $L2$ ($L1 \notin P \Rightarrow L2 \notin P$).
- \leq_p is transitive, i.e., $L1 \leq_p L2$ and $L2 \leq_p L3 \Rightarrow L1 \leq_p L3$.



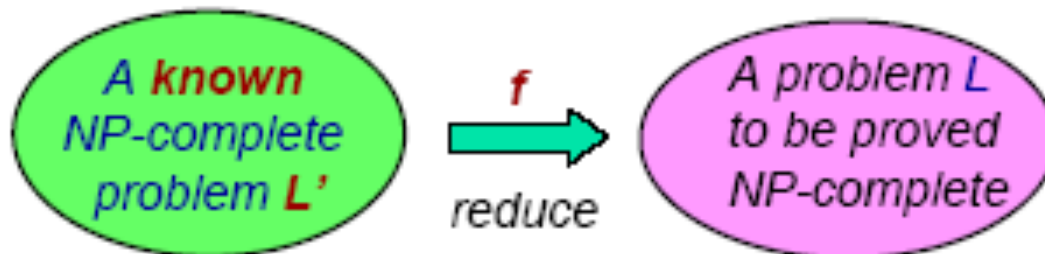
NP-Completeness

- **NP-completeness: worst-case** analyses for **decision** problems.
- A **decision** problem L is **NP-complete (NPC)** if
 1. $L \in \text{NP}$, and
 2. $L' \leq_p L$ for every $L' \in \text{NP}$.
- **NP-hard:** If L satisfies property 2, but not necessarily property 1, we say that L is **NP-hard**.
- Suppose $L \in \text{NPC}$.
 - If $L \in P$, then there exists a polynomial-time algorithm for every $L' \in \text{NP}$ (i.e., $P = \text{NP}$).
 - If $L \notin P$, then there exists no polynomial-time algorithm for any $L' \in \text{NPC}$ (i.e., $P \neq \text{NP}$).



Proving NP-Completeness

- **Five steps for proving that L is NP-complete:**
 1. Prove $L \in \text{NP}$. (easy)
 2. Select a known NP-complete problem L' .
 3. Construct a reduction f transforming **every** instance of L' to an instance of L .
 4. Prove that $x \in L'$ iff $f(x) \in L$ for all $x \in \{0, 1\}^*$.
 5. Prove that f is a polynomial-time transformation.

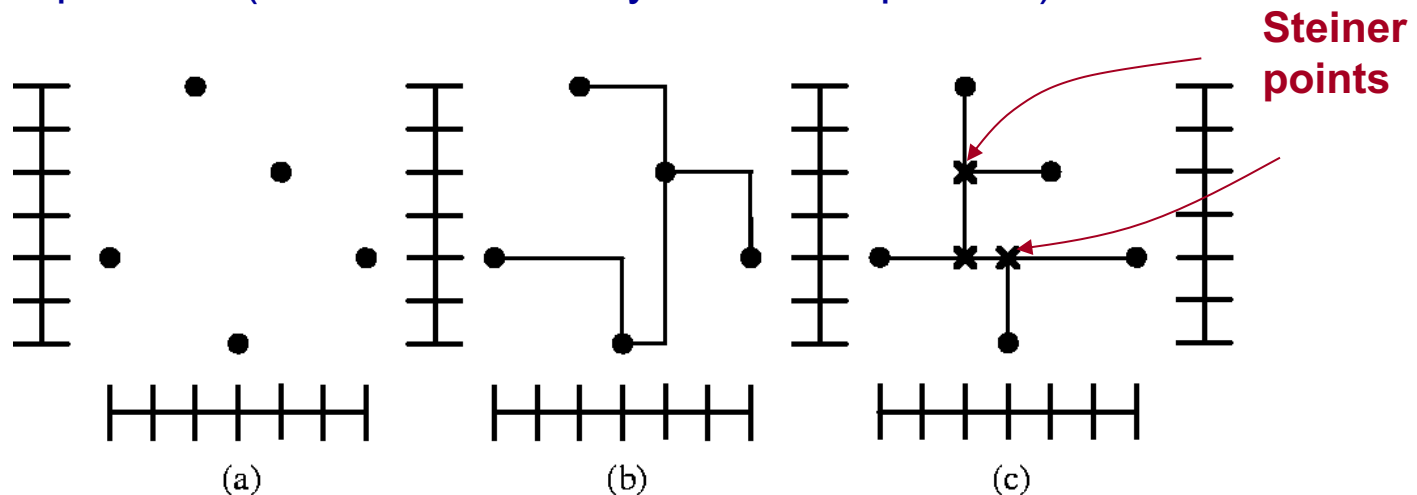


Coping with NP-hard Problems

- **Exhaustive search/Branch and bound**
 - Is feasible only when the problem size is small.
- **Approximation algorithms**
 - Guarantee to be a fixed percentage away from the optimum.
 - E.g., MST for the minimum Steiner tree problem.
- **Pseudo-polynomial time algorithms**
 - Has the form of a polynomial function for the complexity, but is not to the problem size.
 - E.g., $O(nW)$ for the 0-1 knapsack problem. (W : maximum weight)
- **Restriction**
 - Work on some subset of the original problem.
 - E.g., the maximum independent set problem in circle graphs.
- **Heuristics**: No guarantee of performance.

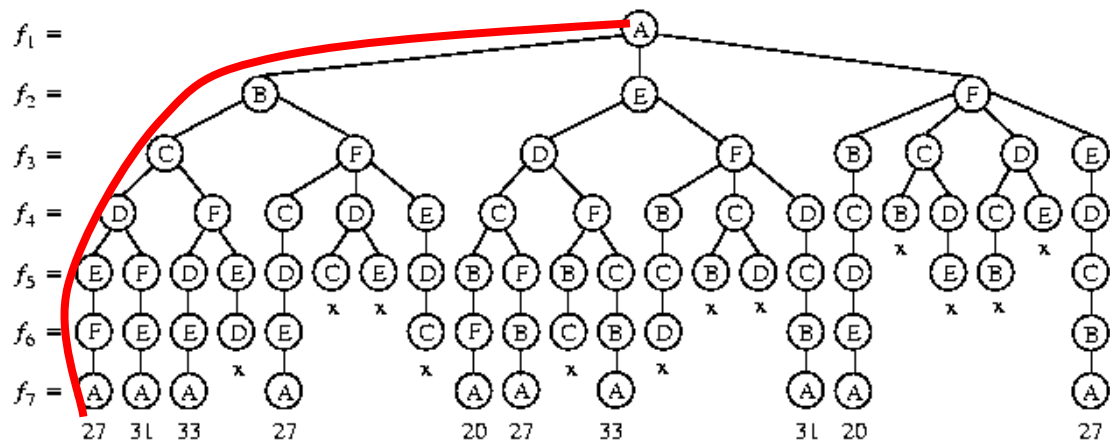
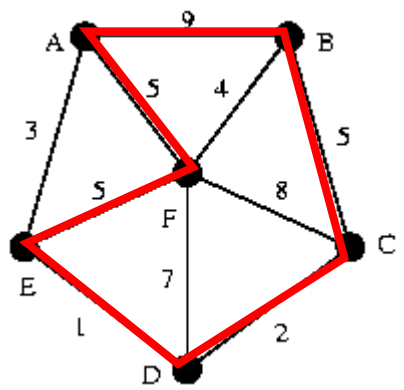
Spanning Tree vs. Steiner Tree

- **Manhattan distance:** If two points (nodes) are located at coordinates (x_1, y_1) and (x_2, y_2) , the Manhattan distance between them is given by $d_{12} = |x_1 - x_2| + |y_1 - y_2|$ (a.k.a. λ -1 metric)
- **Rectilinear spanning tree:** a spanning tree that connects its nodes using Manhattan paths (Fig. (b) below).
- **Steiner tree:** a tree that connects its nodes, and additional points (**Steiner points**) are permitted to be used for the connections.
- The minimum rectilinear spanning tree problem is in P, while the minimum rectilinear Steiner tree (Fig. (c)) problem is NP-complete.
 - The spanning tree algorithm can be an *approximation* for the Steiner tree problem (at most 50% away from the optimum).

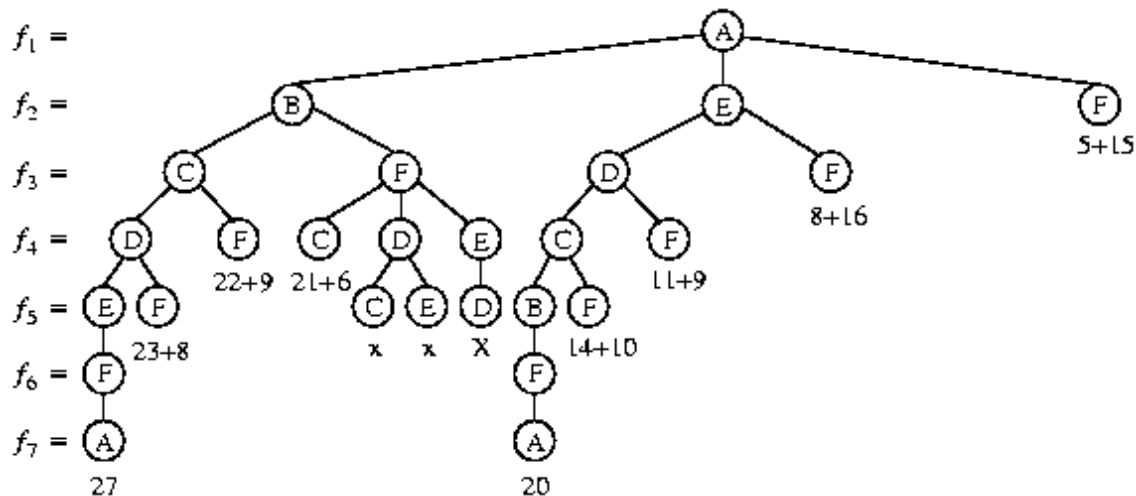


Exhaustive Search vs. Branch and Bound

- TSP example



Backtracking/exhaustive search



Branch and bound

Divide-and-Conquer

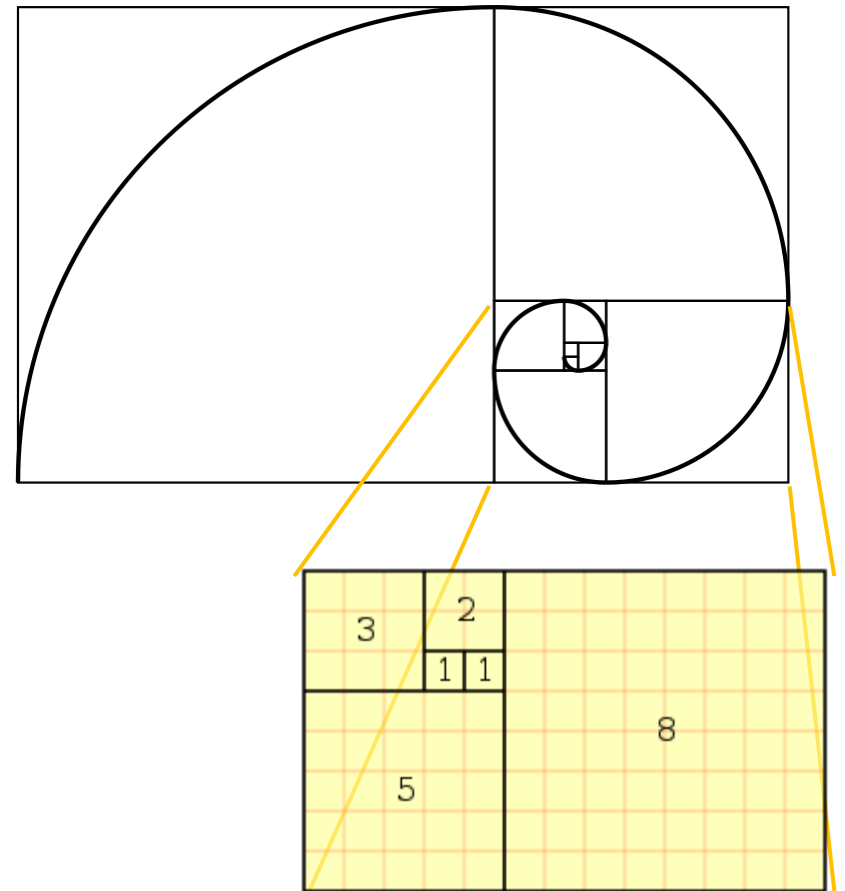
- Divide and conquer:
 - (Divide) Recursively break down a problem into two or more sub-problems of the same (or related) type
 - (Conquer) Until these become simple enough to be solved directly
 - (Combine) The solutions to the sub-problems are then combined to give a solution to the original problem
- Correctness: proved by mathematical induction
- Complexity: determined by solving recurrence relations

Example: Fibonacci Sequence

- Recurrence relation: $F_n = F_{n-1} + F_{n-2}$, $F_0=0$, $F_1=1$
 - e.g., 0, 1, 1, 2, 3, 5, 8, ...
- Direct implementation:
 - Recursion!

fib(n)

1. **if** $n = 0$ **return** 0
2. **if** $n = 1$ **return** 1
3. **return** fib($n - 1$) + fib($n - 2$)



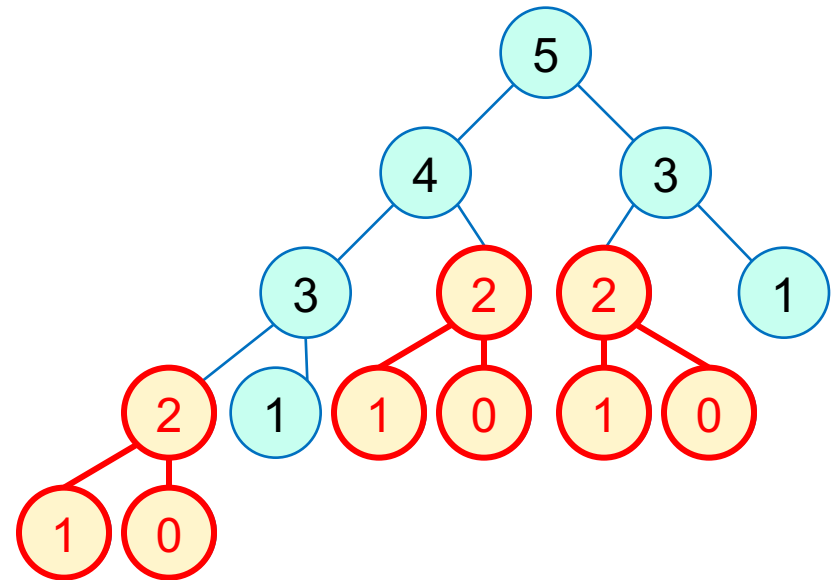
What's Wrong?

$\text{fib}(n)$

1. **if** $n == 0$ **return** 0
2. **if** $n == 1$ **return** 1
3. **return** $\text{fib}(n - 1) + \text{fib}(n - 2)$

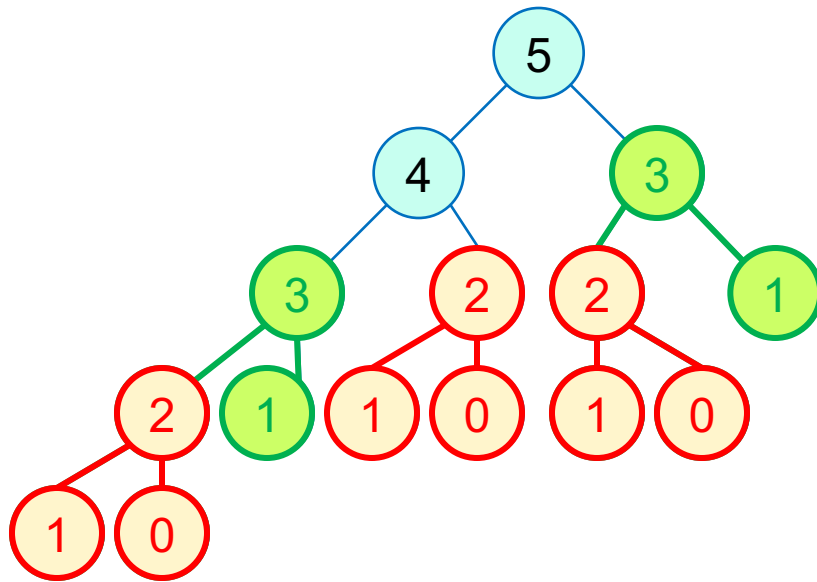
- What if we call $\text{fib}(5)$?

- $\text{fib}(5)$
- $\text{fib}(4) + \text{fib}(3)$
- $(\text{fib}(3) + \text{fib}(2)) + (\text{fib}(2) + \text{fib}(1))$
- $((\text{fib}(2) + \text{fib}(1)) + (\text{fib}(1) + \text{fib}(0))) + ((\text{fib}(1) + \text{fib}(0)) + \text{fib}(1))$
- $((((\text{fib}(1) + \text{fib}(0)) + \text{fib}(1)) + (\text{fib}(1) + \text{fib}(0))) + ((\text{fib}(1) + \text{fib}(0)) + \text{fib}(1)))$
- A call tree that calls the function on the same value many different times
 - $\text{fib}(2)$ was calculated **three** times from scratch
 - Impractical for large n



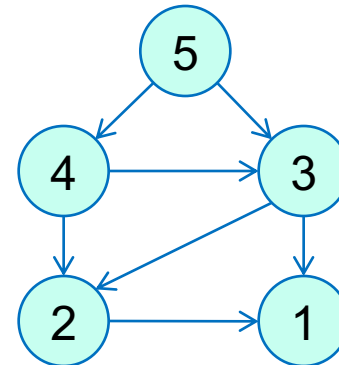
Too Many Redundant Calls!

Recursion



True dependency

- How to remove redundancy?
 - Prevent repeated calculation



Dynamic Programming

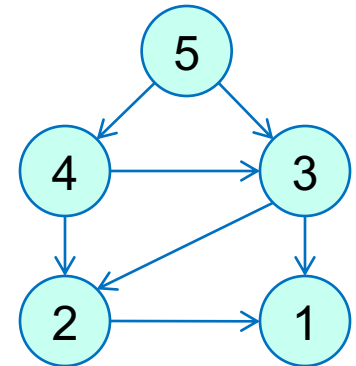
- Store the values in a table
 - Check the table before a recursive call
 - Top-down!
 - The control flow is almost the same as the original one

`fib(n)`

1. Initialize $f[0..n]$ with -1 // -1: unfilled
2. $f[0] = 0$; $f[1] = 1$
3. `fibonacci(n, f)`

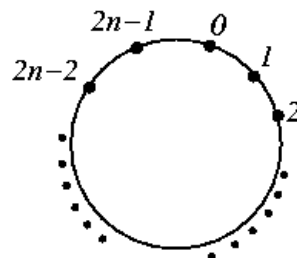
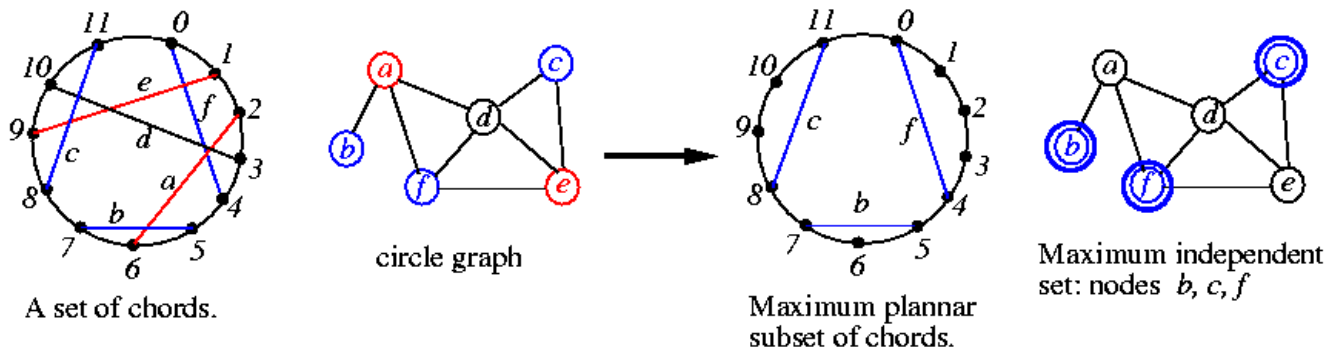
`fibonacci(n, f)`

1. **If** $f[n] == -1$ **then**
2. $f[n] = \text{fibonacci}(n - 1, f) + \text{fibonacci}(n - 2, f)$
3. **return** $f[n]$ // if $f[n]$ already exists, directly return

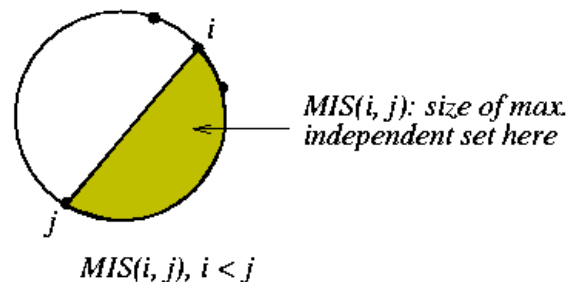


Maximum Independent Set (MIS) in Circle Graphs

- MIS in general is NP-complete
- Problem: Given a set of chords, find a maximum planar subset of chords.
 - Label the vertices on the circle 0 to $2n-1$.
 - Compute $MIS(i, j)$: size of MIS between vertices i and j , $i < j$.
 - $MIS(0, 2n-1)$ is efficiently solvable by dynamic programming.

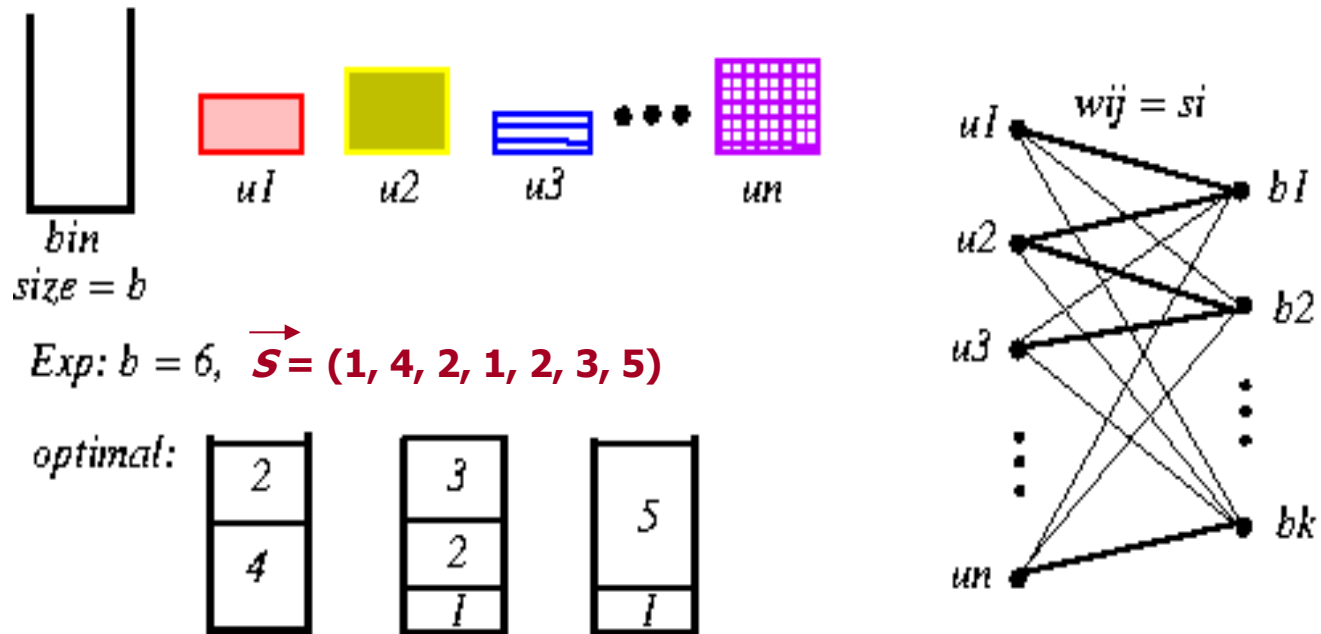


¹ Vertices on the circle

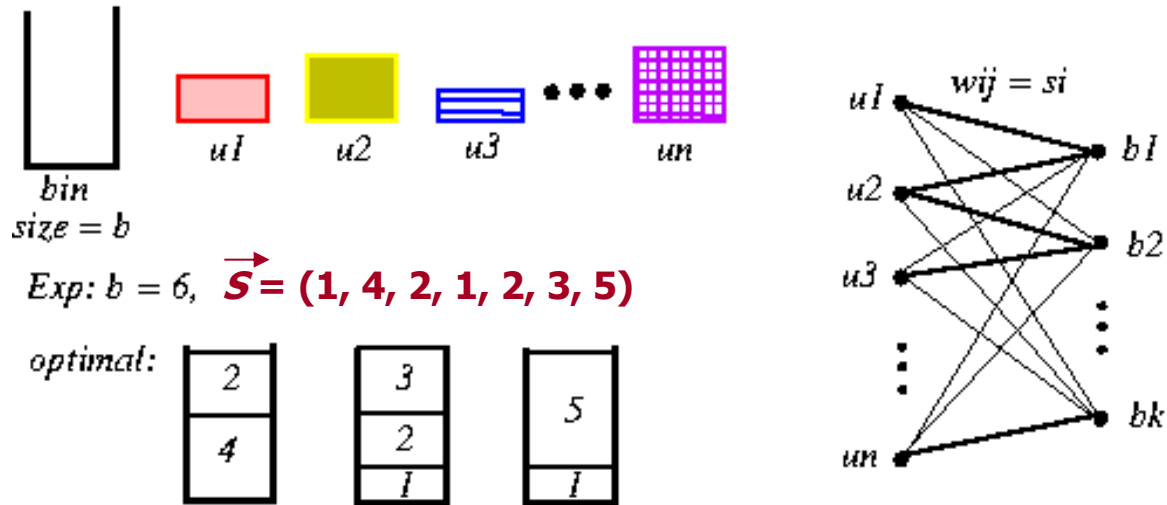


Example: Bin Packing

- **The Bin-Packing Problem Π** : Items $U = \{u_1, u_2, \dots, u_n\}$, where u_i is of an integer size s_i ; set B of bins, each with capacity b .
- **Goal**: Pack all items, minimizing # of bins used. (**NP-hard!**)



Algorithms for Bin Packing



- Greedy approximation alg.: First-Fit Decreasing (FFD)
 - $FFD(\Pi) \leq 11OPT(\Pi)/9 + 4$
- Dynamic Programming? Hierarchical Approach? Genetic Algorithm? ...
- Mathematical Programming: Use **integer linear programming (ILP)** to find a solution using $|B|$ bins, then search for the smallest feasible $|B|$.

ILP Formulation for Bin Packing

- 0-1 variable: $x_{ij}=1$ if item u_i is placed in bin b_j , 0 otherwise.

$$\max \sum_{(i,j) \in E} w_{ij} x_{ij}$$

subject to

objective function

constraints

$$\sum_{i \in U} w_{ij} x_{ij} \leq b_j, \forall j \in B \quad /* \text{capacity constraint} */ \quad (1)$$
$$\sum_{j \in B} x_{ij} = 1, \forall i \in U \quad /* \text{assignment constraint} */ \quad (2)$$
$$\sum_{ij} x_{ij} = n \quad /* \text{completeness constraint} */ \quad (3)$$
$$x_{ij} \in \{0, 1\} \quad /* 0, 1 \text{ constraint} */ \quad (4)$$

- Step 1:** Set $|B|$ to the lower bound of the # of bins.
- Step 2:** Use the ILP to find a feasible solution.
- Step 3:** If the solution exists, the # of bins required is $|B|$. Then exit.
- Step 4:** Otherwise, set $|B| \leftarrow |B| + 1$. Goto Step 2.

Machine Learning for EDA

Problem types solved with Machine Learning

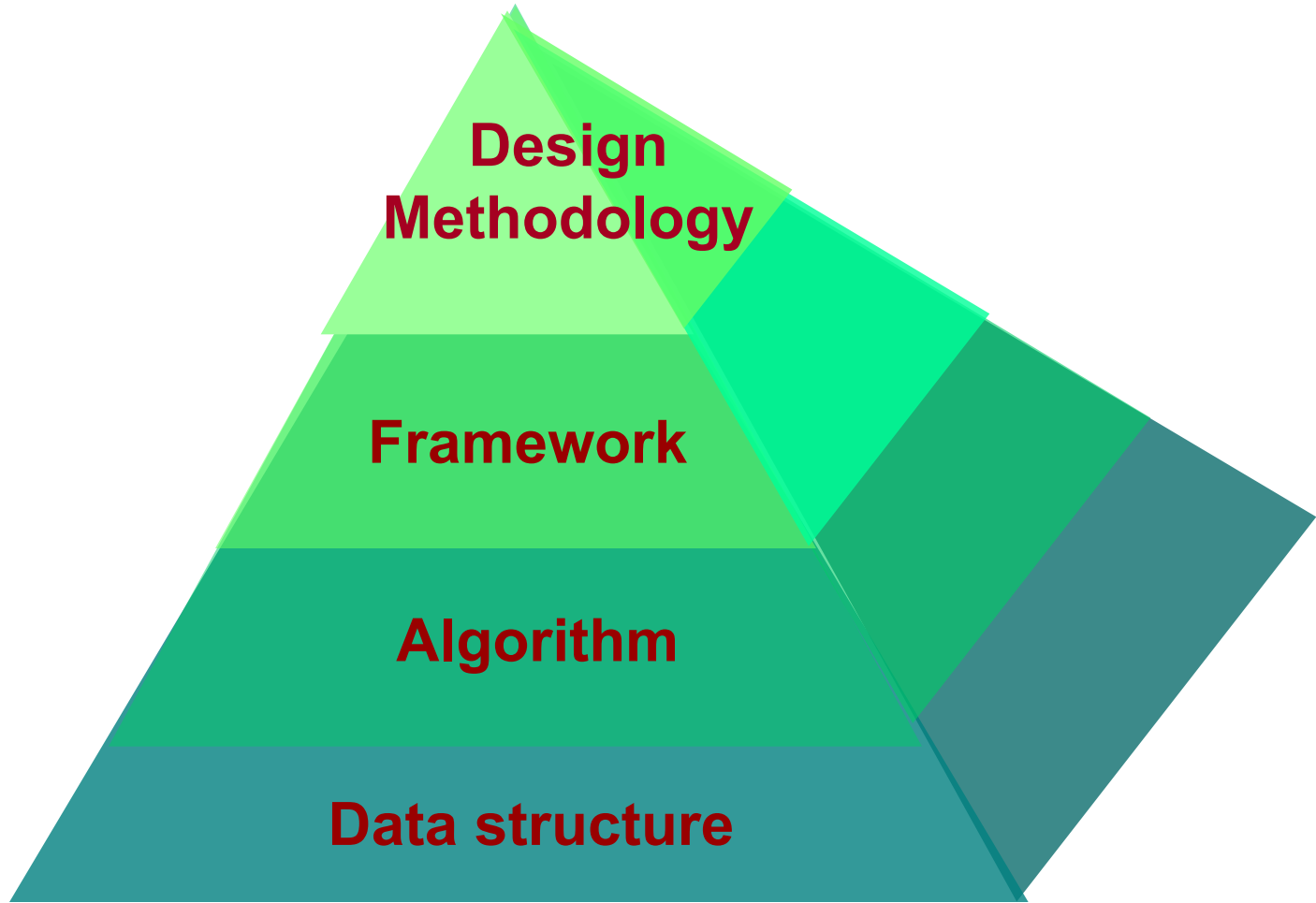
- Classification
- Regression
- Dimensionality reduction
- Structured prediction
- Anomaly detection

Past ML applications in EDA literature

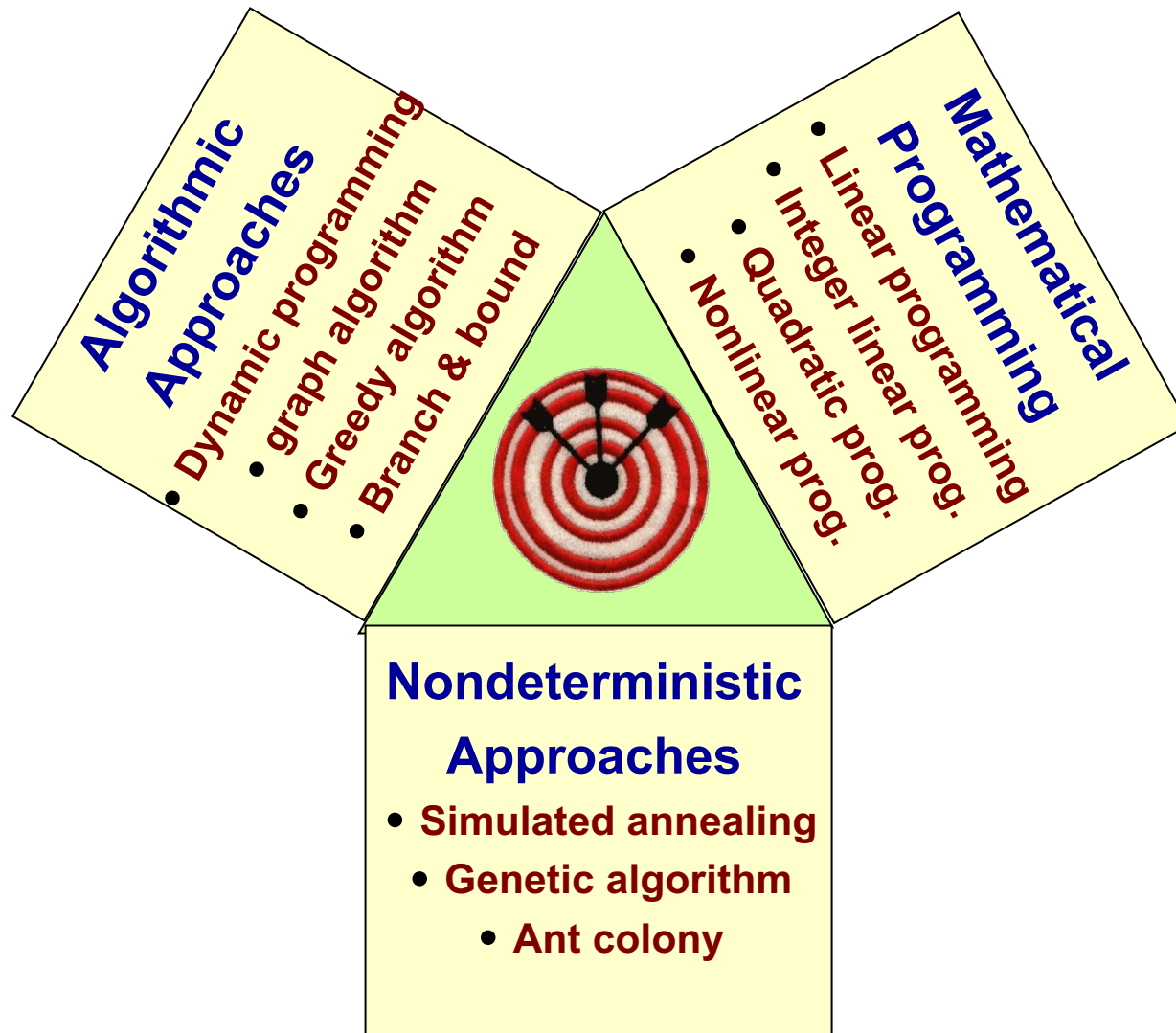
- Yield modeling (anomaly detection, classification)
- Lithography hotspot detection (classification)
- Identification of datapath-regularity (classification)
- Noise and process-variation modeling (regression)
- Performance modeling for analog circuits (regression)
- Design- and implementation-space exploration (regression)

ML in PD: modeling, prediction, correlation, ...

Pyramid for Solving an EDA Problem



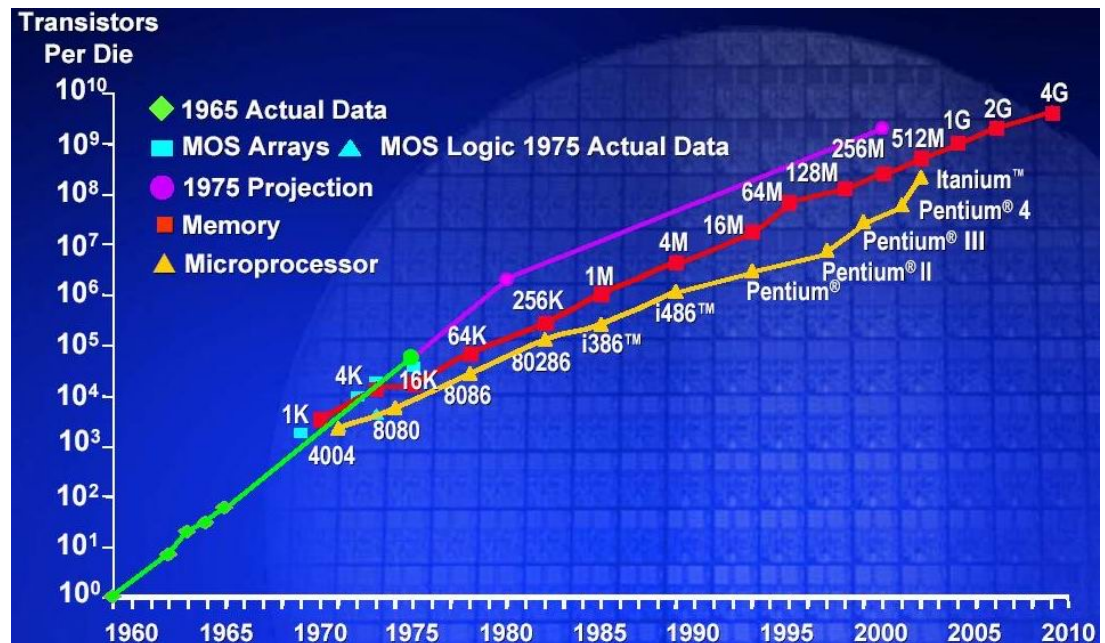
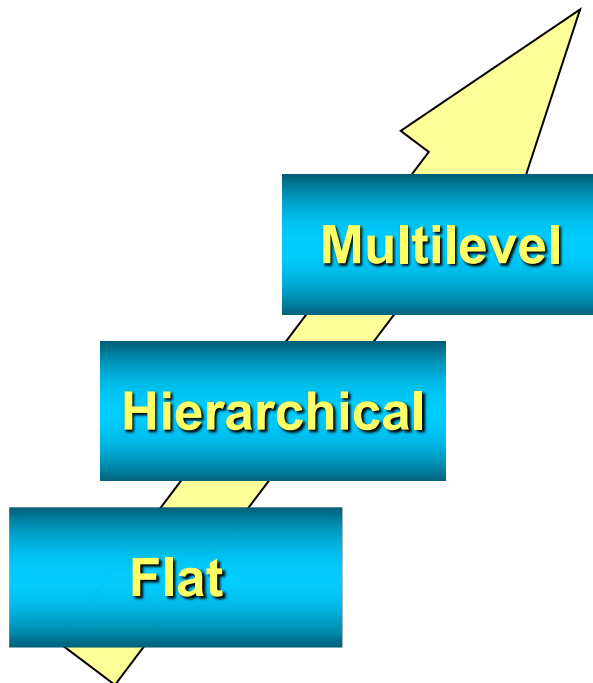
Classifications of Popular EDA Algorithms



Framework Evolution

- Billions of transistors may be fabricated in a single chip for nanometer technology.
- Need frameworks for very large-scale designs.
- Framework evolution for EDA tools:

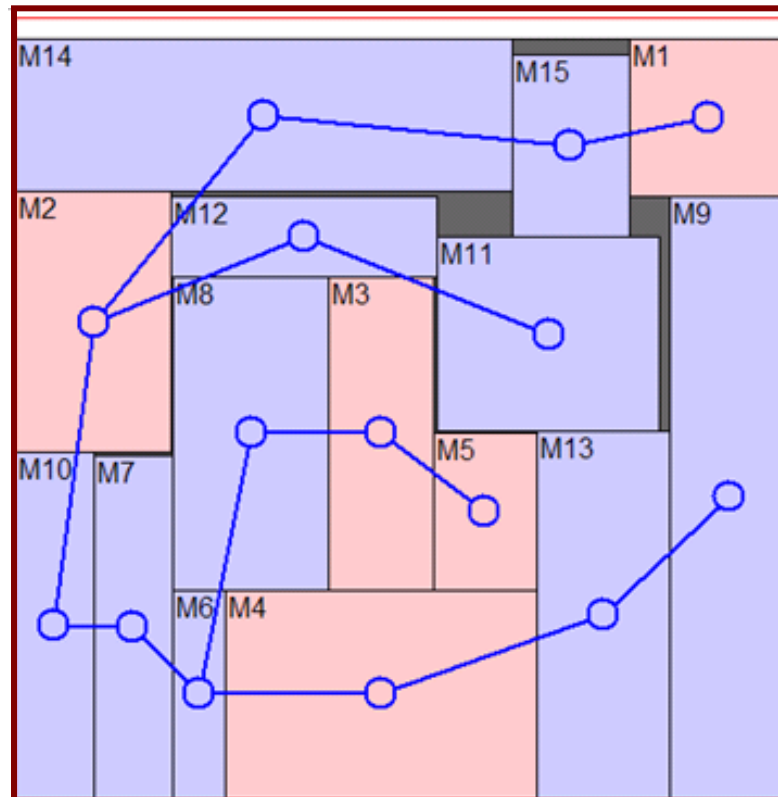
Flat → Hierarchical → Multilevel



Source: Intel (ISSCC-03)

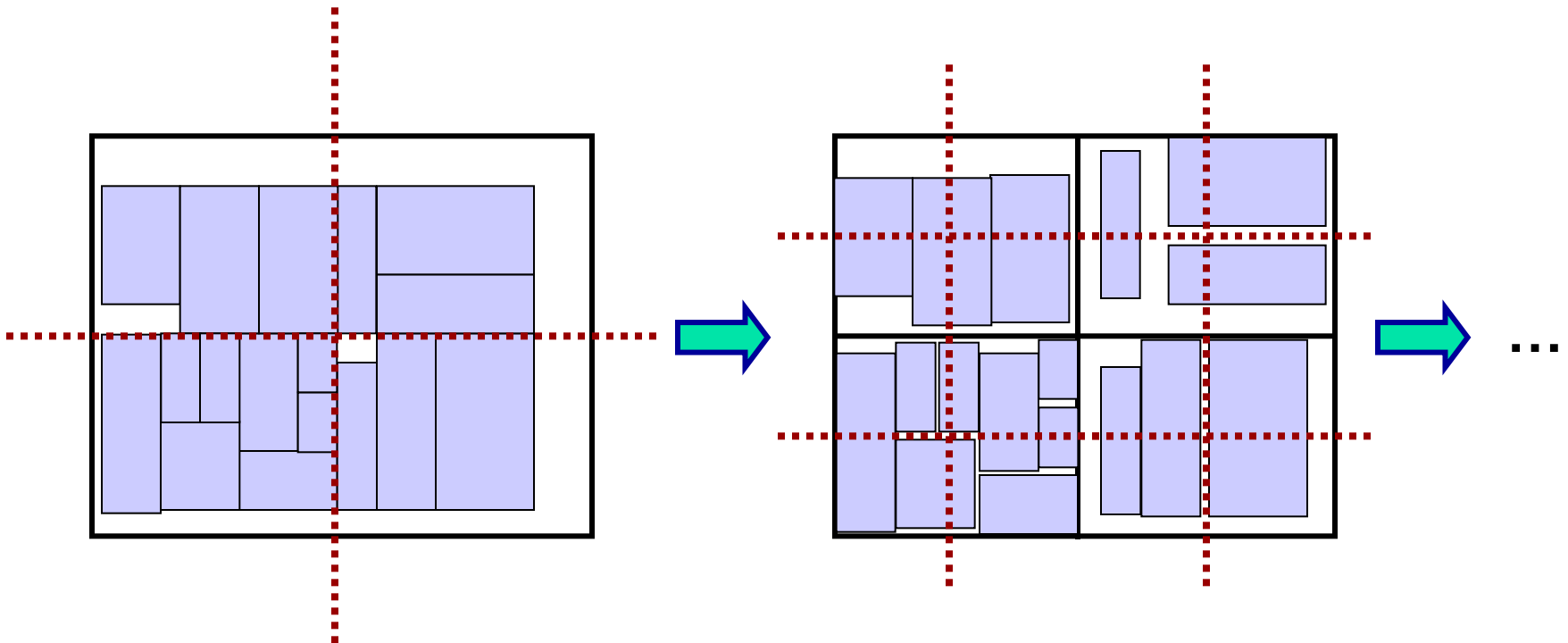
Flat Framework for 2D Bin Packing (Floorplanning)

- Process the circuit components in the whole chip
- Limitation: Good for small-scale designs, but hard to handle larger problems directly



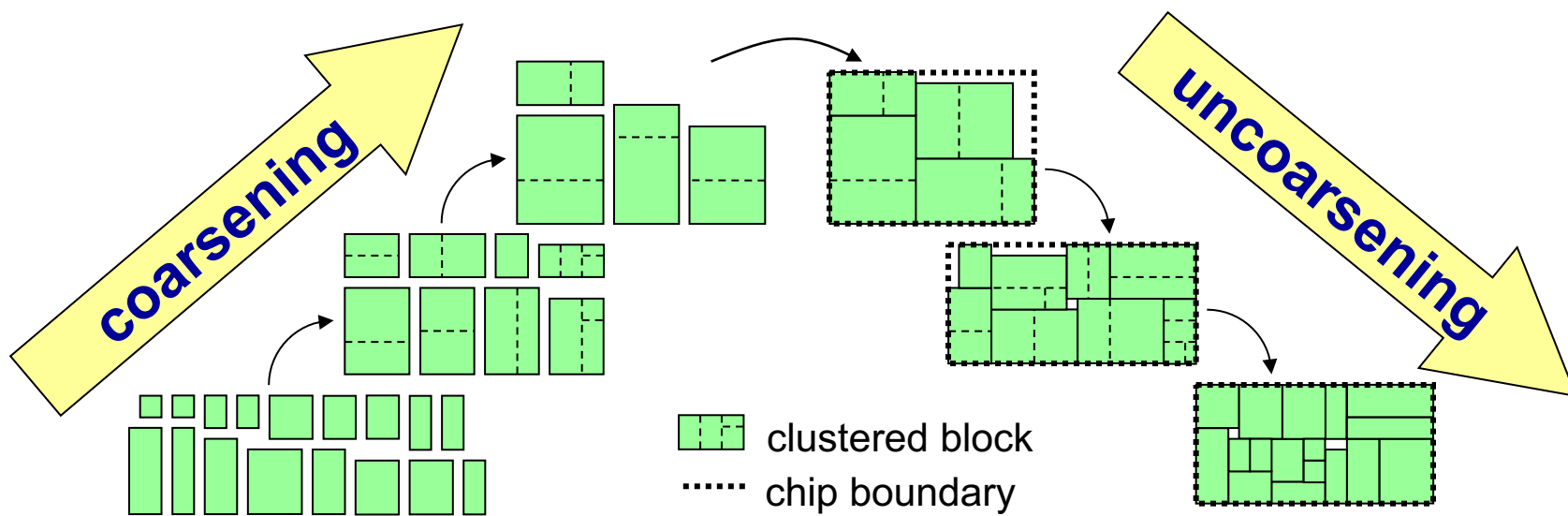
Hierarchical Framework

- The hierarchical approach recursively divides a circuit region into a set of subregions and **solve those subproblems *independently***.
- Good for scalability for large-scale design, but lack the global information for the interaction among subregions.

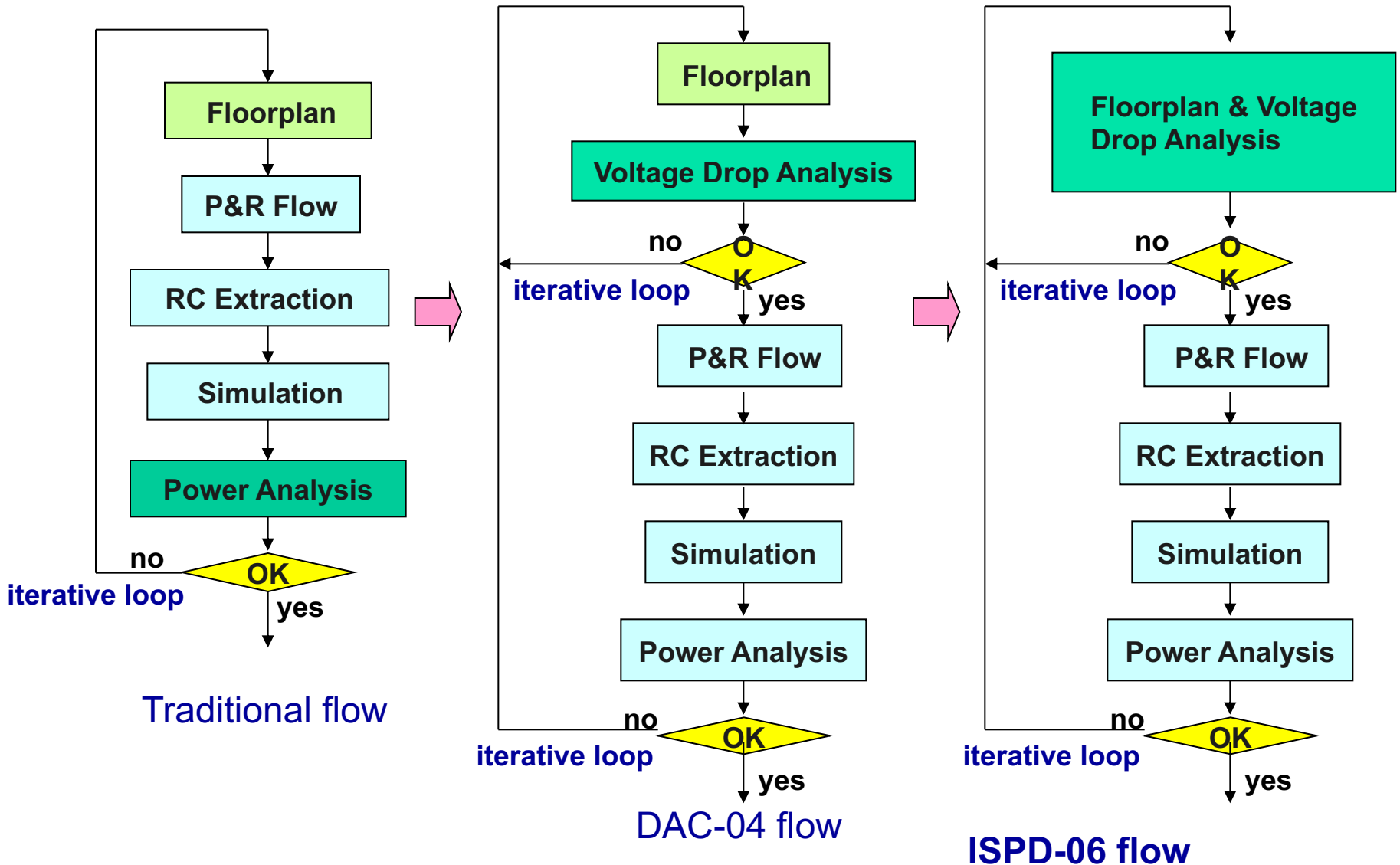


Multilevel Floorplanning

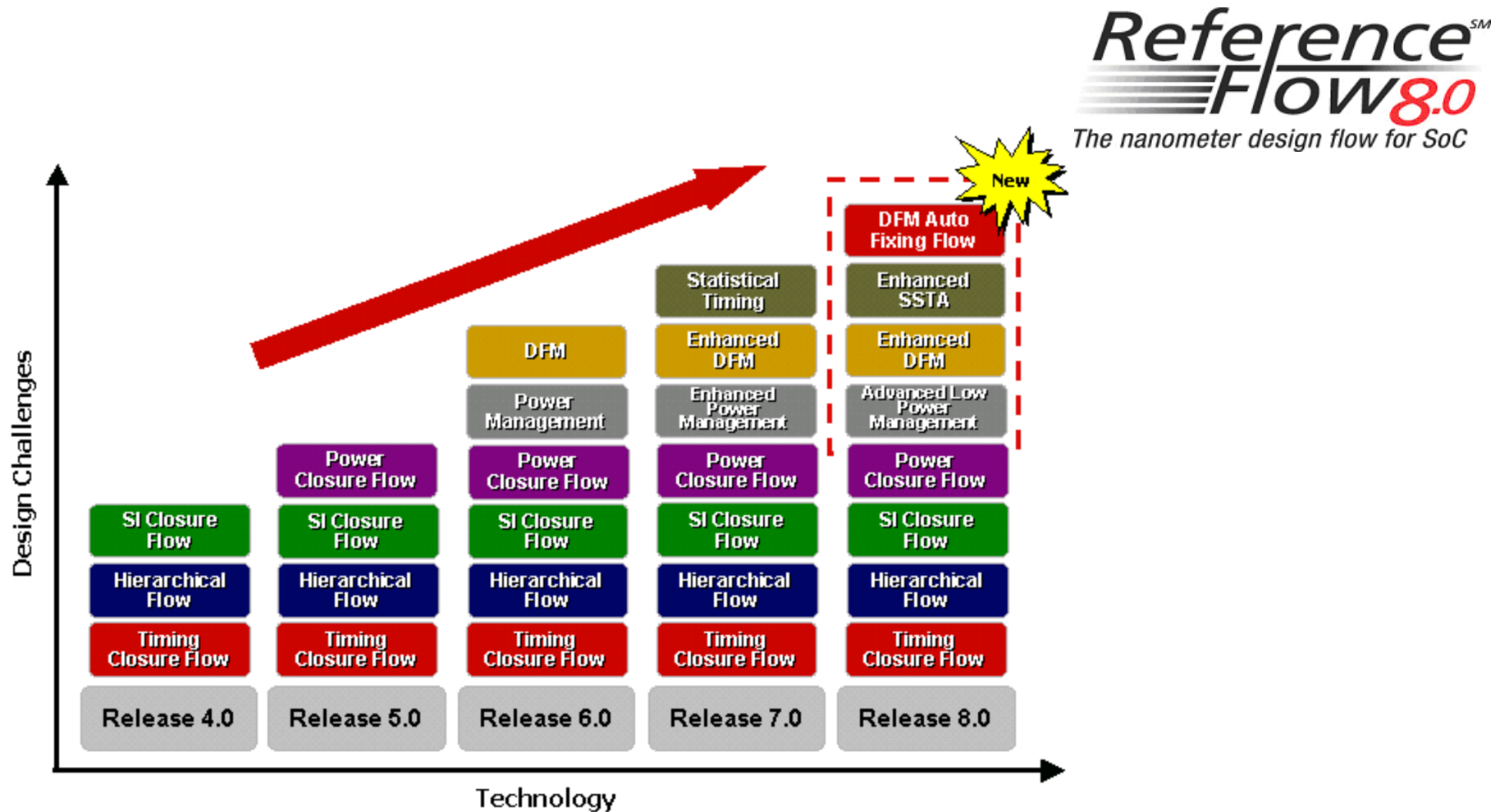
- Bottom-up Coarsening (clustering): Iteratively groups a set of circuit components and collects global information.
- Top-down Uncoarsening (declustering): Iteratively ungroups clustered components and refines the solution.
- Good for scalability and quality trade-off



Design Methodology Evolution



TSMC Reference Flow



Physical Design Related Conferences/Journals

- Important Conferences:
 - **ACM/IEEE Design Automation Conference (DAC)**
 - **IEEE/ACM Int'l Conference on Computer-Aided Design (ICCAD)**
 - **ACM Int'l Symposium on Physical Design (ISPD)**
 - ACM/IEEE Asia and South Pacific Design Automation Conf. (ASP-DAC)
 - ACM/IEEE Design, Automation, and Test in Europe (DATE)
 - IEEE Int'l Conference on Computer Design (ICCD)
 - IEEE Int'l Symposium on Circuits and Systems (ISCAS)
 - IEEE-TSA VLSI Design, Automation and Test (VLSI-DAT)
 - Many more, e.g., GLSVLSI, ISLPED, ISQED, SOCC, VLSI, VLSI Design/CAD Symposium/Taiwan
- Important Journals:
 - **IEEE Transactions on Computer-Aided Design (TCAD)**
 - **ACM Transactions on Design Automation of Electronic Systems (TODAES)**
 - **IEEE Transactions on VLSI Systems (TVLSI)**
 - **IEEE Transactions on Computers (TC)**
 - INTEGRATION: The VLSI Journal
 - IEE Proceedings