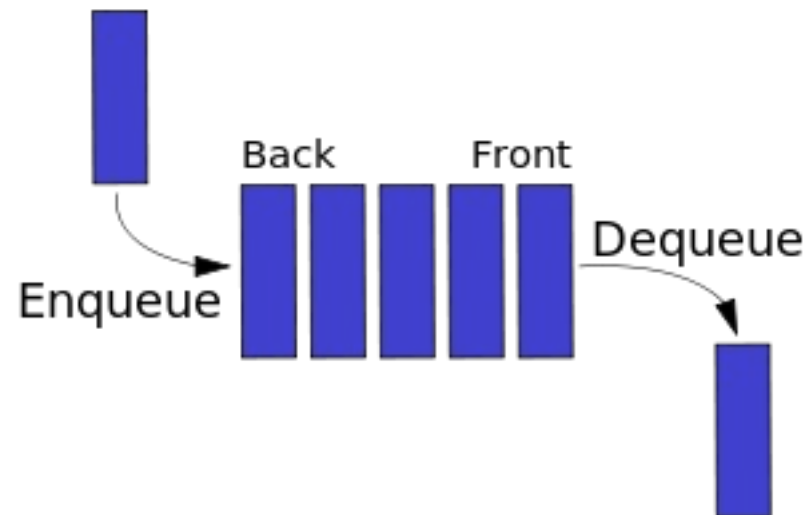


Queues

A Queue



The Abstract Data Type Queue

- A **queue** is a list from which items are deleted from one end (**front**) and into which items are inserted at the other end (**rear**, or **back**)
 - It is like line of people waiting to purchase tickets:
- **Queue** is referred to as a **first-in-first-out (FIFO)** data structure.
 - The first item inserted into a queue is the first item to leave
- Queues have many applications in computer systems:
 - Any application where a group of items is waiting to use a shared resource will use a queue. e.g.
 - jobs in a single processor computer
 - print spooling
 - information packets in computer networks.

ADT Queue Operations

- ***createQueue()***
 - Create an empty queue
- ***destroyQueue()***
 - Destroy a queue
- ***isEmpty():boolean***
 - Determine whether a queue is empty
- ***enqueue(in newItem:QueueItemType) throw QueueException***
 - Inserts a new item at the end of the queue (at the **rear** of the queue)
- ***dequeue() throw QueueException***
dequeue(out queueFront:QueueItemType) throw QueueException
 - Removes (and returns) the element at the **front** of the queue
 - Remove the item that was added earliest
- ***getFront(out queueFront:QueueItemType) throw QueueException***
 - Retrieve the item that was added earliest (without removing)

Some Queue Operations

Operation

x.createQueue()

x.enqueue(5)

x.enqueue(3)

x.enqueue(2)

x.dequeue()

x.enqueue(7)

x.dequeue(a)

x.getFront(b)

Queue after operation

an empty queue

front

↓

5

5 3

5 3 2

3 2

3 2 7

2 7 (a is 3)

2 7 (b is 2)

An Application -- Reading a String of Characters

- A queue can retain characters in the order in which they are typed

```
aQueue.createQueue()
while (not end of line) {
    Read a new character ch
    aQueue.enqueue(ch)
}
```

- Once the characters are in a queue, the system can process them as necessary

Recognizing Palindromes

- A palindrome
 - A string of characters that reads the same from left to right as it does from right to left
- Solution ideas?

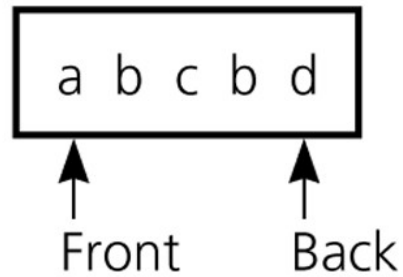
Recognizing Palindromes

- A palindrome
 - A string of characters that reads the same from left to right as it does from right to left
- To recognize a palindrome, a queue can be used in conjunction with a stack
 - A stack reverses the order of occurrences
 - A queue preserves the order of occurrences
- A nonrecursive recognition algorithm for palindromes
 - As you traverse the character string from left to right, insert each character into both a queue and a stack
 - Compare the characters at the front of the queue and the top of the stack

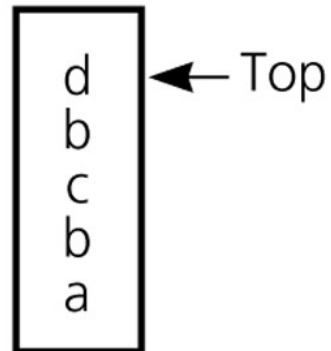
Recognizing Palindromes (cont.)

String: abcba

Queue:



Stack:



The results of inserting a string
into both a queue and a stack

Recognizing Palindromes -- Algorithm

```
isPal(in str:string) : boolean      // Determines whether str is a palindrome or not
    aQueue.createQueue();   aStack.createStack();
    len = length of str;
    for (i=1 through len) {
        nextChar = ith character of str;
        aQueue.enqueue(nextChar);
        aStack.push(nextChar);
    }
    charactersAreEqual = true;
    while (aQueue is not empty and charactersAreEqual) {
        aQueue.getFront(queueFront);
        aStack.getTop(stackTop);
        if (queueFront equals to stackTop) { aQueue.dequeue(); aStack.pop(); }
        else charactersAreEqual = false; }
    return charactersAreEqual;
```

Recognizing Palindromes -- Algorithm

```
bool isPal(char str[], int left, int right) {
```

A recursive one??????????

```
}
```

Recognizing Palindromes -- Algorithm

```
bool isPal(char str[], int left, int right) {
```

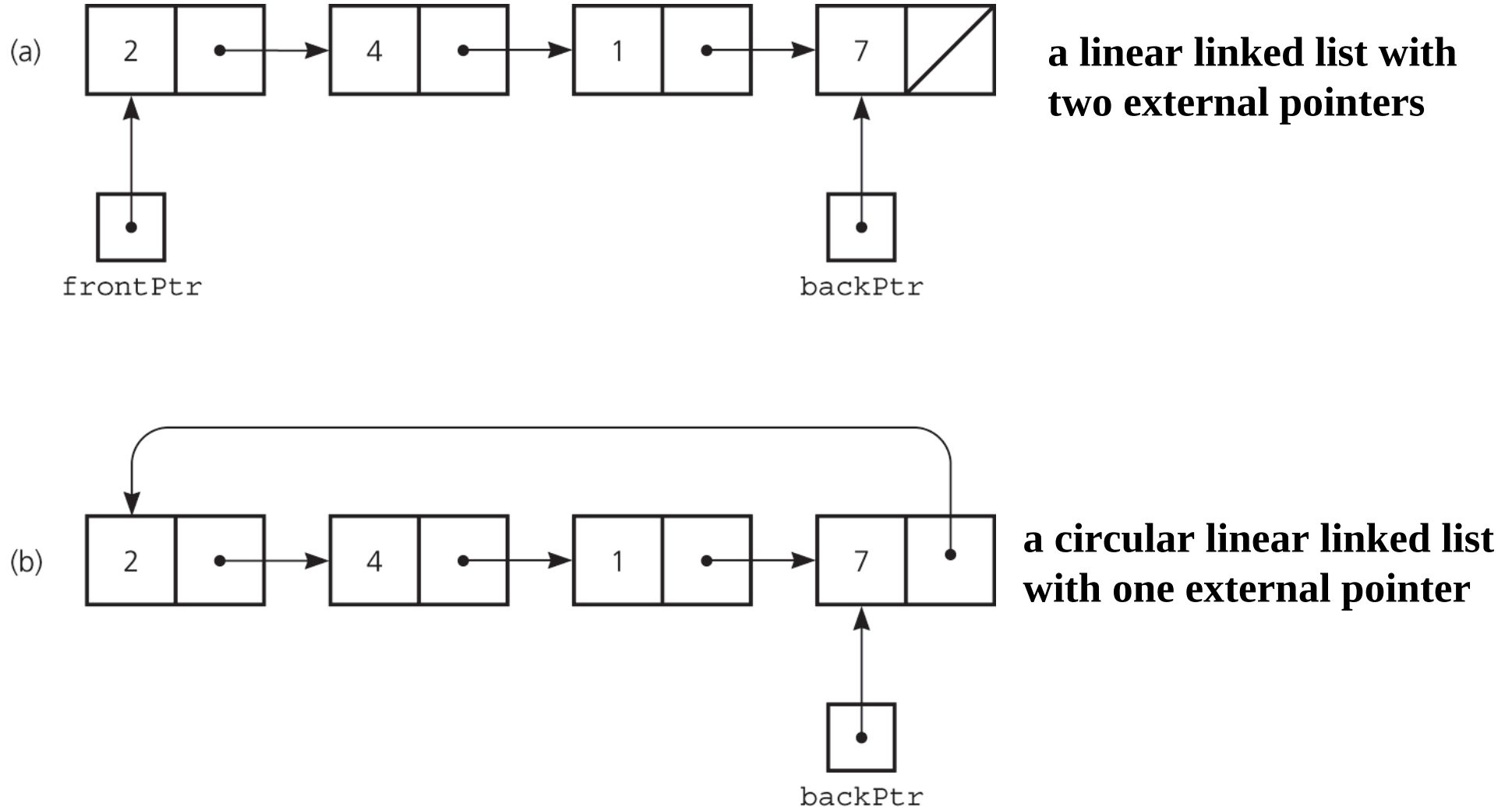
```
    //to be called from main as isPal("rotator", 0, 6);  
    if (left >= right) //Could I have used == instead?  
        return true;  
    if (str[left] == str[right])  
        return isPal(str, left+1, right-1);  
    return false;  
  
}
```

```
//idea: rotator is pal if otato is pal, if tat is pal, if a is pal
```

Implementations of the ADT Queue

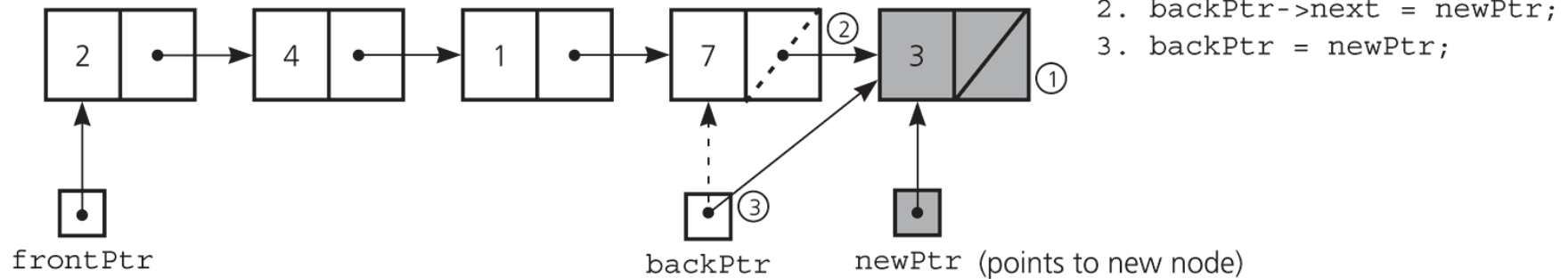
- Pointer-based implementations of queue
 - A linear linked list with two external references
 - A reference to the front
 - A reference to the back
 - A circular linked list with one external reference
 - A reference to the back
- Array-based implementations of queue
 - A naive array-based implementation of queue
 - A circular array-based implementation of queue

Pointer-based implementations of queue

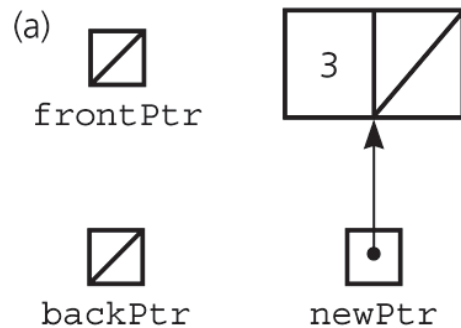


A linked list Implementation -- enqueue

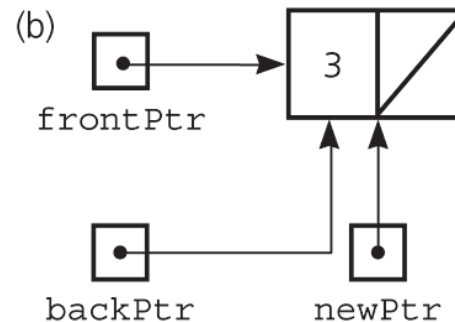
Inserting an item into a nonempty queue



Inserting an item into an empty queue



a) before insertion

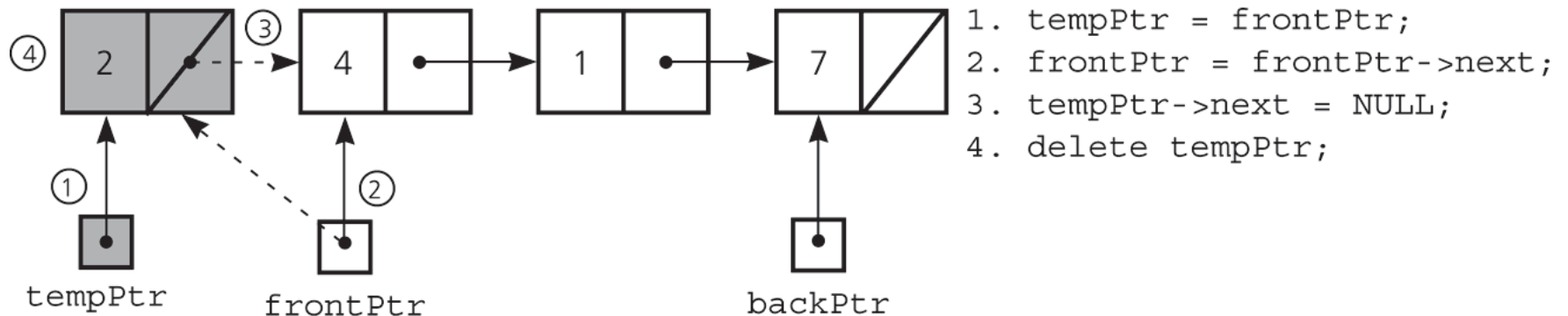


b) after insertion

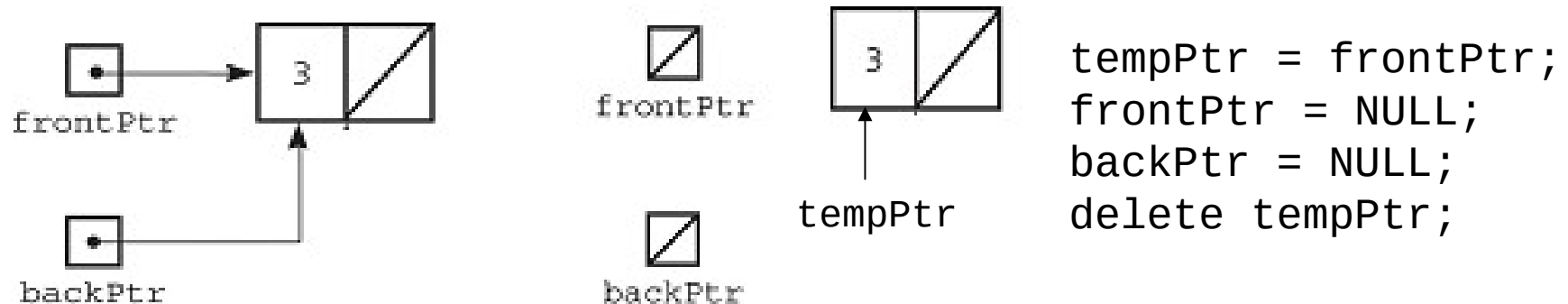
```
frontPtr = newPtr;  
backPtr = newPtr;
```

A Linked list Implementation -- dequeue

Deleting an item from a queue of more than one item



Deleting an item from a queue with one item



before deletion

after deletion

Linked List implementation- Queue Node Class

// QueueNode class for the nodes of the Queue

```
template <class Object>
class QueueNode
{
    public:
        QueueNode(const Object& e = Object(), QueueNode* n = NULL)
            : item(e), next(n) {}

        Object item;
        QueueNode* next;
};
```

A Linked list Implementation – Queue Class

```
#include "QueueException.h"
```

```
template <class T>;
```

```
class Queue {
```

```
public:
```

```
    Queue(); // default constructor
```

```
    Queue(const Queue& rhs); // copy constructor
```

```
    ~Queue(); // destructor
```

```
    Queue& operator=(const Queue & rhs); //assignment operator
```

```
    bool isEmpty() const; // Determines whether the queue is empty
```

```
    void enqueue(const T& newItem); // Inserts an item at the back of a queue
```

```
    void dequeue() throw(QueueException); // Dequeues the front of a queue
```

```
    // Retrieves and deletes the front of a queue.
```

```
    void dequeue(T& queueFront) throw(QueueException);
```

```
    // Retrieves the item at the front of a queue.
```

```
    void getFront(T& queueFront) const throw(QueueException);
```

```
private:
```

```
    QueueNode<T> *backPtr;
```

```
    QueueNode<T> *frontPtr;
```

```
}
```

Linked List Implementation – constructor, destructor, isEmpty

```
template<class T>
Queue<T>::Queue() : backPtr(NULL), frontPtr(NULL){} // default
               constructor

template<class T>
Queue<T>::~~Queue() { // destructor
    while (!isEmpty())
        dequeue(); // backPtr and frontPtr are NULL at this point
}

template<class T>
bool Queue<T>::isEmpty() const{
    return backPtr == NULL;
}
```

A Linked list Implementation – enqueue

```
template<class T>
void Queue<T>::enqueue(const T& newItem) {
```

```
    // create a new node
```

```
    QueueNode<T> *newPtr = new QueueNode;
```

```
    // set data portion of new node
```

```
    newPtr->item = newItem;
```

```
    newPtr->next = NULL;
```

```
    // insert the new node
```

```
    if (isEmpty())
```

```
        frontPtr = newPtr;
```

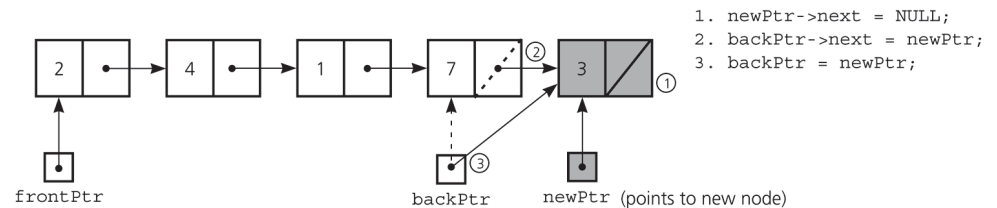
```
    else
```

```
        // insertion into nonempty queue
```

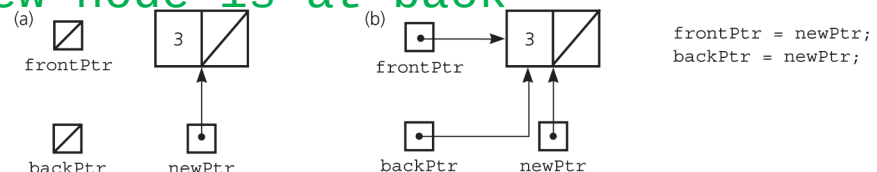
```
        backPtr->next = newPtr;
```

```
    backPtr = newPtr;    // new node is at back
```

```
}
```



```
    // insertion into empty queue
```



A Linked list Implementation – dequeue

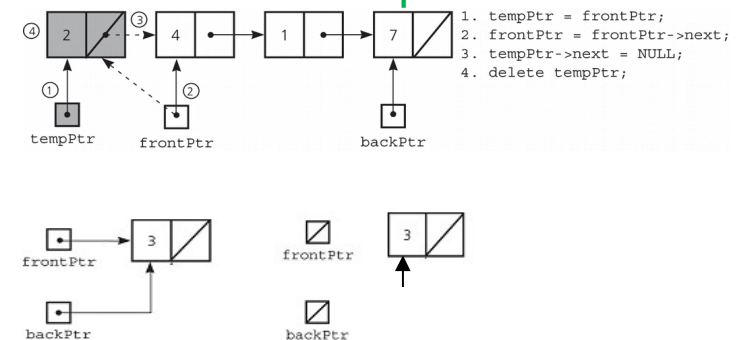
```

template<class T>
void Queue<T>::dequeue() throw(QueueException) {
    if (isEmpty())
        throw QueueException("QueueException: empty queue, cannot
dequeue");
    else {        // queue is not empty; remove front
        QueueNode<T> *tempPtr = frontPtr;
        if (frontPtr == backPtr) {
            frontPtr = NULL;
            backPtr = NULL;
        }
        else
            frontPtr = frontPtr->next;

        tempPtr->next = NULL;        // defensive strategy
        delete tempPtr;
    }
}

```

// one node in queue

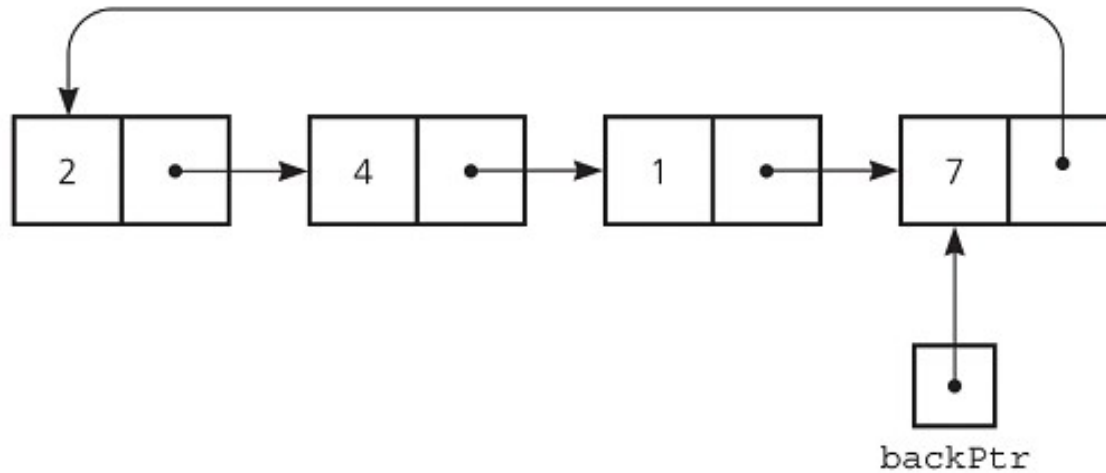


A Pointer-Based Implementation – dequeue, getFront

```
template<class T>
void Queue<T>::dequeue(T& queueFront) throw(QueueException) {
    if (isEmpty())
        throw QueueException("QueueException: empty queue, cannot
dequeue");
    else {        // queue is not empty; retrieve front
        queueFront = frontPtr->item;
        dequeue(); // delete front
    }
}

template<class T>
void Queue<T>::getFront(T& queueFront) const throw(QueueException) {
    if (isEmpty())
        throw QueueException("QueueException: empty queue, cannot
getFront");
    else        // queue is not empty; retrieve front
        queueFront = frontPtr->item;
}
```

A circular linked list with one external pointer



Queue Operations

constructor ?

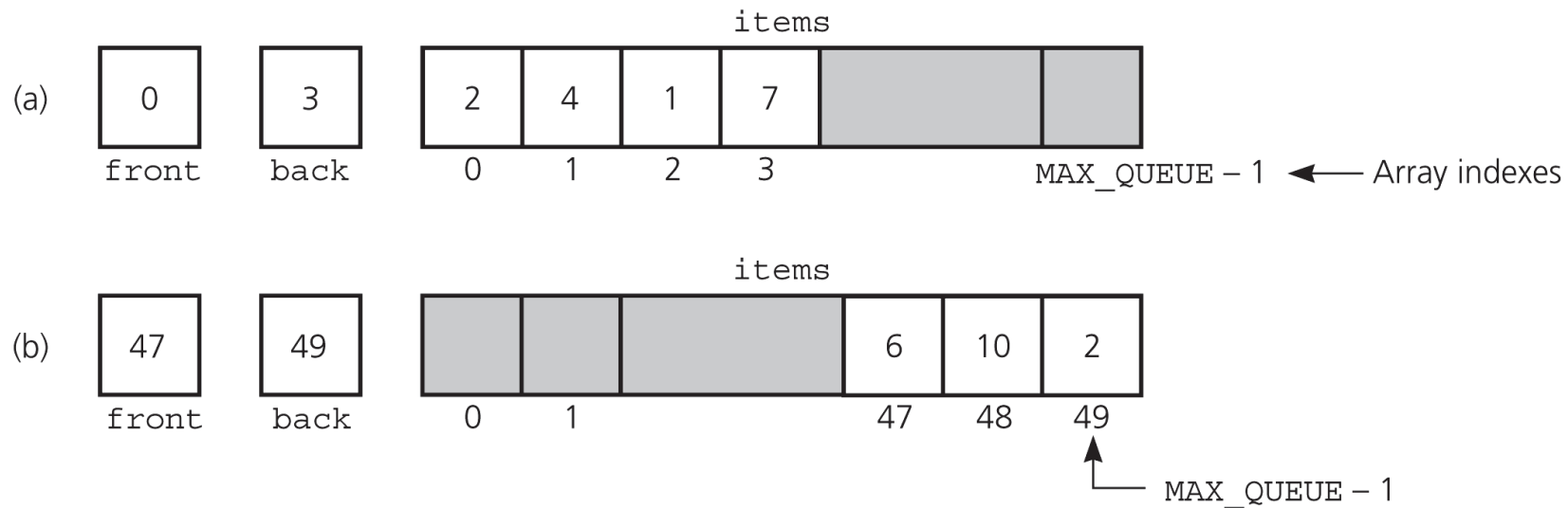
isEmpty ?

enqueue ?

dequeue ?

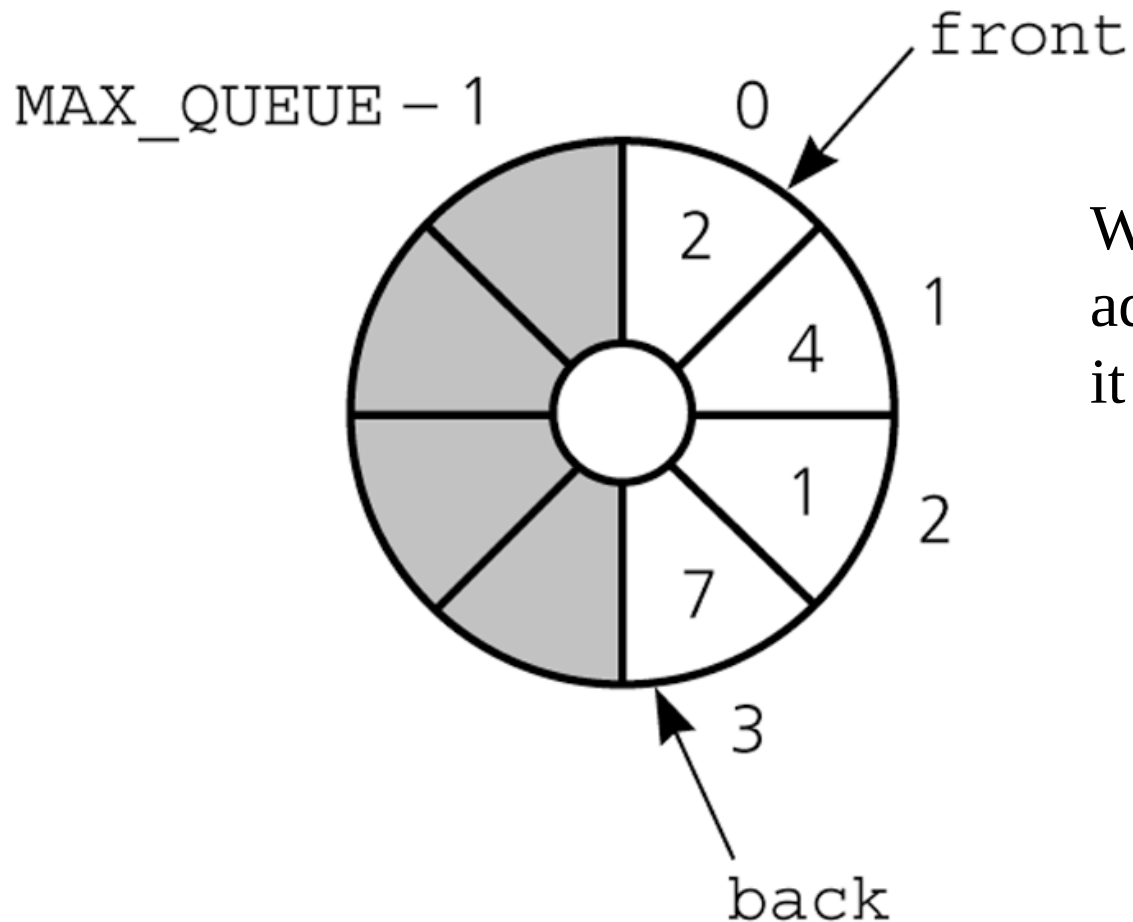
getFront ?

A Naive Array-Based Implementation of Queue

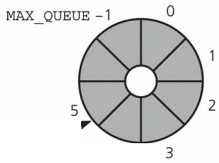


- Rightward drift can cause the queue to appear full even though the queue contains few entries.
- We may shift the elements to left in order to compensate for rightward drift, but shifting is expensive
- **Solution:** A circular array eliminates rightward drift.

A Circular Array-Based Implementation



When either **front** or **back** advances past **MAX_QUEUE - 1** it wraps around to 0.



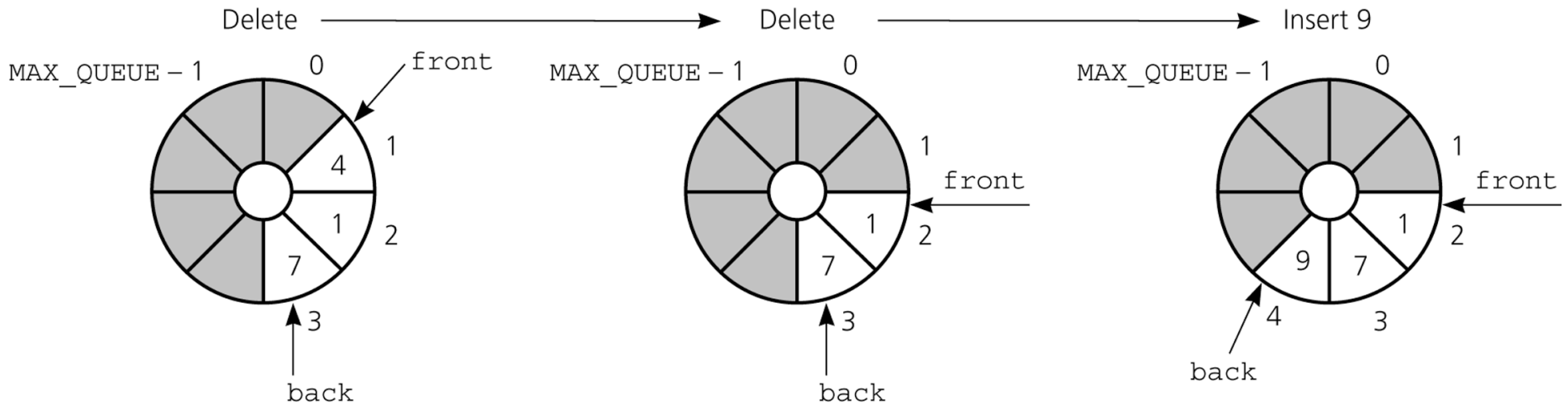
The effect of some operations of the queue

Initialize: $\text{front} = 0$; $\text{back} = \text{MAX_QUEUE} - 1$;

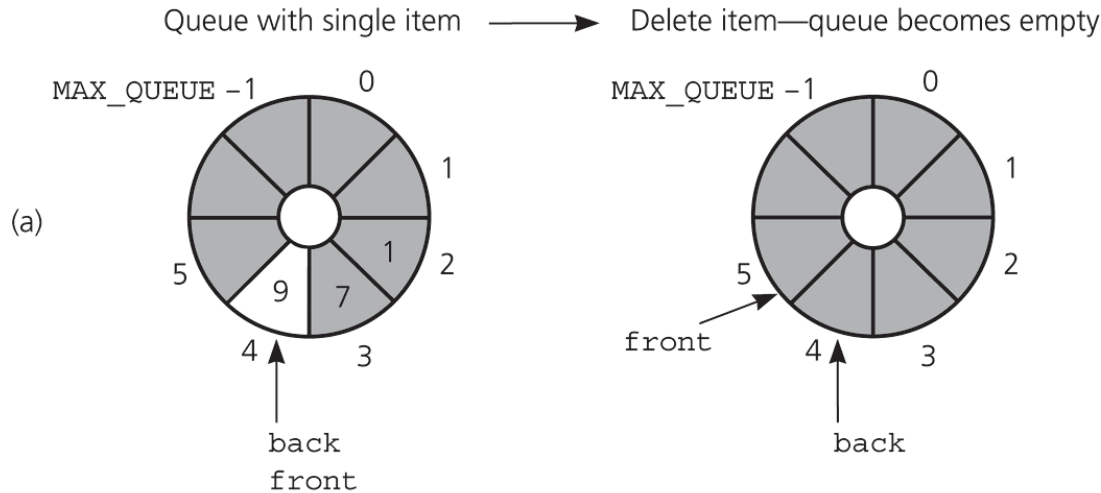
Insertion: $\text{back} = (\text{back} + 1) \% \text{MAX_QUEUE}$;
 $\text{items}[\text{back}] = \text{newItem}$;

NOT ENOUGH

Deletion: $\text{front} = (\text{front} + 1) \% \text{MAX_QUEUE}$;



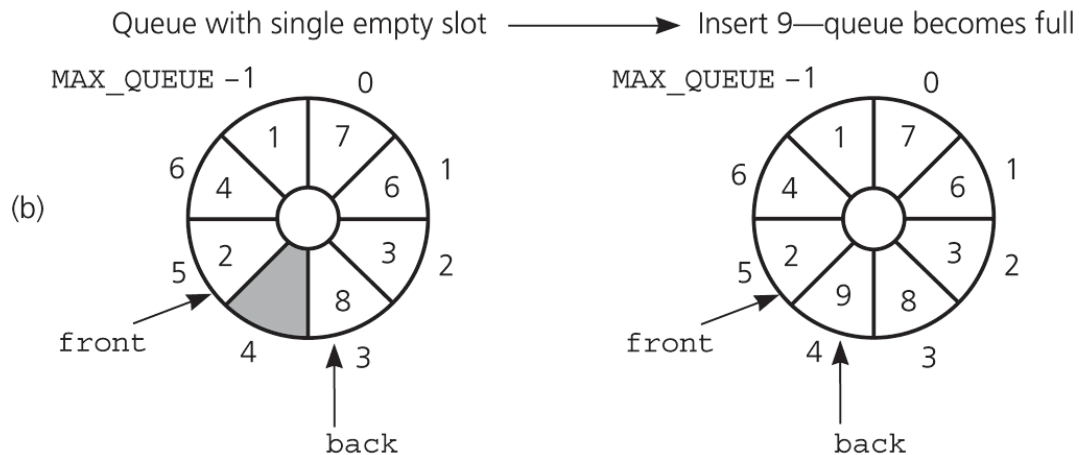
Problem: Q Empty or Full



front and **back** cannot be used to distinguish between *queue-full* and *queue-empty* conditions.

? Empty

$(back+1)\%MAX_QUEUE == front$



? Full

$(back+1)\%MAX_QUEUE == front$

So, we need extra mechanism to distinguish between *queue-full* and *queue-empty* conditions.

Solutions for Queue-Empty/Queue-Full Problem

1. Using a counter to keep the number items in the queue.
 - Initialize count to 0 during creation; Increment count by 1 during insertion; Decrement count by 1 during deletion.
 - $\text{count}=0 \rightarrow \text{empty}$; $\text{count}=\text{MAX_QUEUE} \rightarrow \text{full}$
2. Using isFull flag to distinguish between the full and empty conditions.
 - When the queue becomes full, set isFullFlag to true; When the queue is not full set isFull flag to false;
3. Using an extra array location (and leaving at least one empty location in the queue).
 - Declare $\text{MAX_QUEUE}+1$ locations for the array items, but only use MAX_QUEUE of them. We do not use one of the array locations.
 - *Full*: $\text{front} \text{ equals to } (\text{back}+1)\%(\text{MAX_QUEUE}+1)$
 - *Empty*: $\text{front} \text{ equals to } \text{back}$

Using a counter

- To initialize the queue, set
 - front to 0
 - back to MAX_QUEUE-1
 - count to 0
- Inserting into a queue

```
back = (back+1) % MAX_QUEUE;
items[back] = newItem;
++count;
```
- Deleting from a queue

```
front = (front+1) % MAX_QUEUE;
--count;
```
- Full: `count == MAX_QUEUE`
- Empty: `count == 0`

Array-Based Implementation Using a counter – Header File

```
#include "QueueException.h"
const int MAX_QUEUE = maximum-size-of-queue;

template <class T>
class Queue {
public:
    Queue(); // default constructor
    bool isEmpty() const;
    void enqueue(const T& newItem) throw(QueueException);
    void dequeue() throw(QueueException);
    void dequeue(T& queueFront) throw(QueueException);
    void getFront(T& queueFront) const throw(QueueException);
private:
    T items[MAX_QUEUE];
    int front;
    int back;
    int count;
};
```

Array-Based Implementation Using a counter – constructor, isEmpty

```
template<class T>
Queue<T>::Queue():front(0), back(MAX_QUEUE-1), count(0) {}
```

```
template<class T>
bool Queue<T>::isEmpty() const
{
    return count == 0;
}
```

Array-Based Implementation Using a counter - enqueue

```
template<class T>
void Queue<T>::enqueue(const T& newItem)
    throw(QueueException) {
    if (count == MAX_QUEUE)
        throw QueueException("QueueException: queue full on
enqueue");
    else {    // queue is not full; insert item
        back = (back+1) % MAX_QUEUE;
        items[back] = newItem;
        ++count;
    }
}
```


Array-Based Implementation Using a counter – dequeue

```
template<class T>
void Queue<T>::dequeue() throw(QueueException) {
    if (isEmpty())
        throw QueueException("QueueException: empty queue, cannot
dequeue");
    else { // queue is not empty; remove front
        front = (front+1) % MAX_QUEUE;
        --count;
    }
}

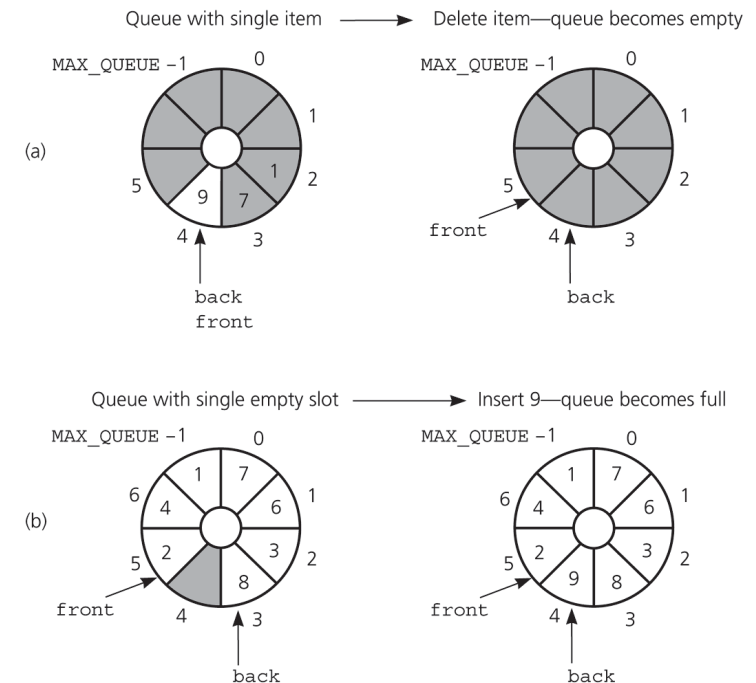
void Queue::dequeue(T& queueFront) throw(QueueException) {
    if (isEmpty())
        throw QueueException("QueueException: empty queue, cannot
dequeue");
    else { // queue is not empty; retrieve and remove front
        queueFront = items[front];
        front = (front+1) % MAX_QUEUE;
        --count;
    }
}
```

Array-Based Implementation Using a counter – getFront

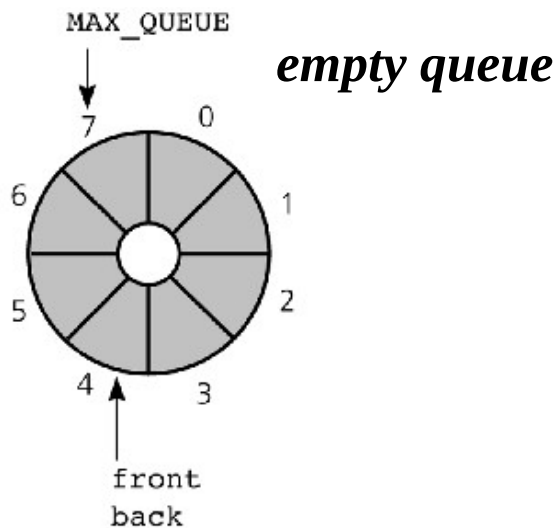
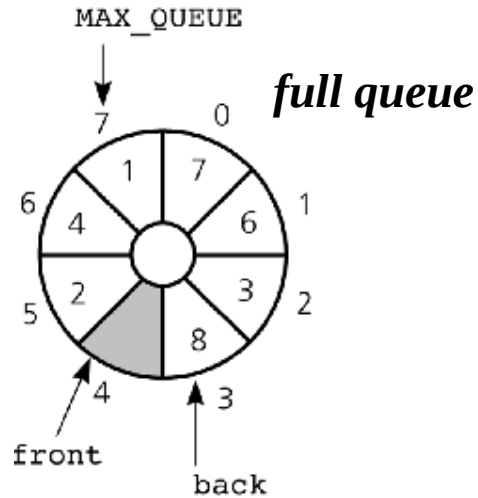
```
template <class T>
void Queue<T>::getFront(T& queueFront) const throw(QueueException)
{
    if (isEmpty())
        throw QueueException("QueueException: empty queue, cannot
getFront");
    else
        // queue is not empty; retrieve front
        queueFront = items[front];
}
```

Using isFull flag

- To initialize the queue, set
 $\text{front} = 0; \text{ back} = \text{MAX_QUEUE} - 1; \text{ isFull} = \text{false};$
- Inserting into a queue
 $\text{back} = (\text{back} + 1) \% \text{MAX_QUEUE}; \text{ items}[\text{back}] = \text{newItem};$
 $\text{if } ((\text{back} + 1) \% \text{MAX_QUEUE} == \text{front}) \text{ isFull} = \text{true};$
- Deleting from a queue
 $\text{front} = (\text{front} + 1) \% \text{MAX_QUEUE};$
 $\text{isFull} = \text{false};$
- Full: $\text{isFull} == \text{true}$
- Empty: $\text{isFull} == \text{false}$
 $\&\& ((\text{back} + 1) \% \text{MAX_QUEUE} == \text{front})$



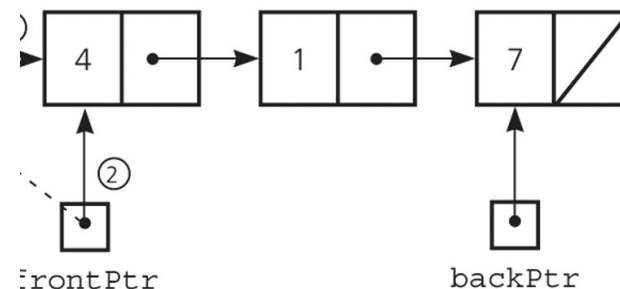
Using an extra array location



- To initialize the queue, allocate $(MAX_QUEUE+1)$ locations
 $front=0; \quad back=0;$
- **front** holds the index of the location before the front of the queue.
- Inserting into a queue (if queue is not full)
 $back = (back+1) \% (MAX_QUEUE+1);$
 $items[back] = newItem;$
- Deleting from a queue (if queue is not empty)
 $front = (front+1) \% (MAX_QUEUE+1);$
- Full:
 $(back+1)\%(MAX_QUEUE+1) == front$
- Empty:
 $front == back$

An Implementation That Uses the ADT List Class

- If the item in `first()` of a list `aList` represents the front of the queue, the following implementations can be used
 - *dequeue()*
`aList.remove(aList.first()->element)`
 - *getFront(queueFront)*
`aList.first()->element`
- If the item at the end of the list represents the back of the queue, the following implementations can be used
 - *enqueue(newItem)*
`aList.insert(newItem, aList.lastNode())`
- Simple to implement, but inefficient.



Comparing Implementations

- Fixed size versus dynamic size
 - A statically allocated array
 - Prevents the `enqueue` operation from adding an item to the queue if the array is full
 - A resizable array or a reference-based implementation
 - Does not impose this restriction on the `enqueue` operation
- Pointer-based implementations
 - A linked list implementation
 - More efficient; no size limit
 - The ADT list implementation
 - Simpler to write; inefficient

A Summary of ADTs

- ADTs: List, Stack, Queue.
- Stacks and Queues
 - Only the end positions can be accessed
- Lists
 - All positions can be accessed
- Stacks and queues are very similar
 - Operations of stacks and queues can be paired off as
 - `createStack` and `createQueue`
 - `Stack isEmpty` and `queue isEmpty`
 - `push` and `enqueue`
 - `pop` and `dequeue`
 - `Stack getTop` and `queue getFront`
- ADT list operations generalize stack and queue operations
 - `insert`, `remove`, `first()`