

# Design, Modeling, and Analysis of Inductive Resonant Coupling Wireless Power Transfer for Micro Aerial Vehicles (MAVs)

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**Abstract**—This paper presents the design, modeling, analysis, and experimental validation of an inductive resonant wireless power transfer (WPT) system to power a micro aerial vehicle (MAV). Using WPT, in general, enables longer flight times, virtually eliminates the need for batteries, and minimizes down time for recharging or replacing batteries. The proposed WPT system consists of a transmit coil, which can either be fixed to ground or placed on a mobile platform, and a receive coil carried by the MAV. The details of the WPT circuit design are presented. A power-transfer model is developed for the two-coil system, where the model is used to select suitable coil geometries to maximize the power received by the MAV for hovering. Analysis, simulation, and experimental results are presented to demonstrate the effectiveness of the WPT circuitry. Finally, a wirelessly powered MAV that hovers above the transmit coil is demonstrated in a laboratory setting.

## I. INTRODUCTION

Recent advances in technology have enabled the development of high-performance MAVs which include fixed-wing aircraft, flapping-wing aircraft, coaxial helicopters, trirotor helicopters, and the ubiquitous quadrotor helicopters (quadcopters) [1]. These small vehicles are well suited for applications that include autonomous sensor networks for remotely detecting environmental hazards, surveillance, and search and rescue operations in areas that are dangerous to humans. One of the key challenges with MAV technology is short flight times because batteries offer a limited supply of energy. For example, the average battery life of a MAV falls between 10 and 20 minutes [2], where advances have pushed the flight time to around 30 minutes [3].

Wireless power transfer, for example through magnetic resonance coupling, is a potential method to deliver power to MAVs to address the limitations — such as short flight times — associated with carrying batteries. This method gives the MAV a constant source of power to operate, virtually eliminating the need for a battery and significantly extending flight times compared to state-of-the-art battery-operated technology. The advantages of wireless charging are that the MAV can remain operational and airborne, allowing it to be useful in complex and hostile environments where landing or recovering the MAV and changing out batteries is not practical, for example when operating around chemical spills/leaks and nuclear disaster sites. For example, the MAV can be contaminated and physical interaction with the vehicle

to change out batteries is not a safe option. Furthermore, it has been suggested that wirelessly powering a quadcopter could be useful to inspect transmission lines [4], although a working demonstration was never reported. If the charging coils are set up properly in an industrial facility, the MAV used for assembly-line inspection would never have to take an operational break to charge, but rather it could constantly fly through the “charging path” to continuously recharge.

The contribution of this paper is the detailed design, modeling, and analysis of an effective inductive resonant WPT system to specifically power a MAV and experimentally demonstrating hovering for an extended period of time. Compared to recent similar work which described the design of the power amplifier for inductive resonant coupling WPT [5], the detailed design, modeling, and analysis specific to MAV operation, to the best knowledge of the authors, has not been published. In this work, the WPT is designed through modeling to maximize the ratio of power received by the MAV to that of the power requirements for the MAV. Additionally, a sensing scheme is proposed in which the MAV can sense its location relative to the transmit coil and this information can be used to develop a feedback controller to position the MAV at the optimum location for maximum power received.

## II. RELATED WORKS

The area of wireless power transfer has recently attracted the attention of researchers, in particular research in magnetic resonance coupling wireless power transfer (MRC-WPT) [6]. For example, the optimal ratio of planar spiral coil sizes in a MRC-WPT system was examined in [7]. When comparing coil size and distance for efficiency, it was reported that at closer distances, transmit ( $T_x$ ) and receive ( $R_x$ ) coils of similar size have higher efficiency than coils of mismatched size, but as separation distances increase, the efficiency of a small  $R_x$  coil coupled with a larger  $T_x$  coil is better than similarly sized coils. Other work has been performed to compare different coil geometries, such as planar circular spiral coils, square helical coils, and circular solenoid coils to demonstrate the effects of coil shape on efficiency with change in load and separation distance [8]. The results indicate that power transfer through planar spiral coils generally decreases more quickly due to deviations in operating frequency, as opposed to coil shape. However, planar spiral coils perform similarly to other shapes when the operating frequency is close to the resonant frequency of the coils.

The concept of resonant capacitive coupling wireless power transfer to charge and power an aerial vehicle was illustrated in a brochure by Solace Power Inc. [9]. However, this technol-

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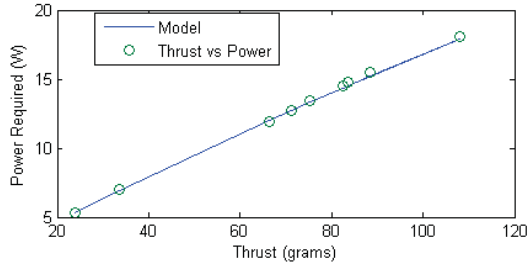


Fig. 3. The power-to-thrust relationship for the experimental MAV (Jianjian Technology Co., LTD model JJRC-H98), comparing measurements and model.

(with loaded weight of 115 g for the test) to a scale and using a DC power supply to power the MAV in place of the battery. As the throttle on the MAV was increased the change in scale measurement was recorded with the associated voltage and current. Figure 3 displays the experimentally measured power-to-thrust relationship for the MAV, along with a polynomial-fit of the data ( $R^2 = 0.9994$ ), given by

$$P = -0.0002t^2 + 0.1759t + 1.2212, \quad (2)$$

where  $P$  is the power consumed by the MAV in Watts and  $t$  is the thrust in grams which the MAV needs for hover.

Coil design parameters include wire diameter, number of coil turns, pitch, and coil diameter. The coil model must calculate receive coil mass to use with the thrust-to-power relationship given by Eq. (2). With the density of copper as  $8.96 \text{ g/cm}^3$ , the length of the coil  $l$ , self inductance  $L$ , AC resistance  $R_{AC}$ , mutual inductance  $M$ , and coupling coefficient  $k$  [7] are calculated using

$$l = \frac{1}{2}N\pi(D_o + D_i), \quad (3)$$

$$L = \frac{N^2(D_o - N(w + p))^2}{16D_o + 28N(w + p)} \times \frac{39.37}{10^6}, \quad (4)$$

$$R_{AC} = \sqrt{\frac{f\pi_o\mu_o}{\sigma}} \times \frac{N(D_o - N(w + p))}{w}, \quad (5)$$

$$M = \sum_{i=1}^{N_{Tx}} \sum_{j=1}^{N_{Rx}} \mu_o R_i R_j \times \int_0^\pi \frac{\cos(\Theta) d\Theta}{\sqrt{R_i^2 + R_j^2 + d^2 - 2R_i R_j \cos(\Theta)}}, \text{ and}$$

$$k = \frac{M}{\sqrt{L_i L_j}}, \quad (7)$$

where  $D_o$  is outside diameter of the coil,  $D_i$  is the inside diameter of the coil,  $N$  is the number of coil turns,  $w$  is the wire diameter,  $p$  is the pitch,  $f$  is the operating frequency (in this work 13.56 MHz),  $\sigma$  is conductivity of copper ( $59.6 \times 10^6 \frac{\text{S}}{\text{m}}$ ),  $\mu_o$  is the permeability of free space,  $d$  is the distance between the two coils, and  $r_i$  and  $r_j$  are radii of each turn for the  $T_x$  and  $R_x$  coils, respectively. In Eq. (6), coils are assumed to be coaxial and parallel-planar. When coils are not coaxial and parallel-planar mutual inductance between

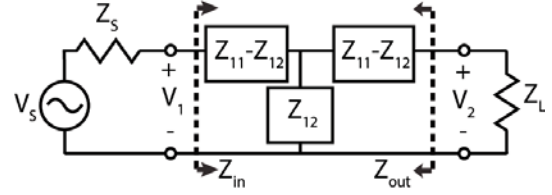


Fig. 4. The equivalent circuit model of a WPT system with a T-equivalent two-port network, where  $Z_{in}$  is the impedance seen by the RF power supply and  $Z_{out}$  is the impedance seen by the load. The T-network represents the two-port element formed by the coupled coils.

each turn is calculated using mutual inductance calculations outlined in [12] and methods from [13].

The transmit coil geometry is held constant when comparing receive coil geometries. Using the coil values found above, an impedance analysis of the system is performed to determine power delivery capabilities of each system as shown by

$$Z_{11} = R_1 + j\omega L_{T_x} + \frac{1}{j\omega C_{T_x}}, \quad (8)$$

$$Z_{22} = R_L + R_2 + j\omega L_{R_x} + \frac{1}{j\omega C_{R_x}}, \quad (9)$$

$$Z_{12} = Z_{21} = j\omega M, \text{ and} \quad (10)$$

$$Z_{in} = Z_{11} - \frac{Z_{12}^2}{Z_{22} + Z_L}. \quad (11)$$

The impedance of the WPT system,  $Z_{in}$ , as seen by the source is found using a T-equivalent two-port network as shown in Fig. 4. The T-equivalent two-port network is a representation of the simplified circuit used for modeling purposes.

By calculating the impedances throughout the WPT system, the current through the  $T_x$  coil is calculated with

$$I_1 = \frac{V_s Z_{22}}{Z_{11} Z_{22} + (\omega M)^2}, \quad (12)$$

and the current through the  $R_x$  coil is calculated with

$$I_2 = -\frac{jV_s(\omega M)}{Z_{11} Z_{22} + (\omega M)^2}. \quad (13)$$

The instantaneous power going into the  $T_x$  coil can then be calculated with

$$P_{in} = I_1^2 Z_{in}, \quad (14)$$

and the instantaneous power received at the load is calculated using

$$P_e = I_2^2 R_L. \quad (15)$$

Many coil geometries are tested with these equations to determine a suitable geometry for application with the selected MAV and a fixed  $T_x$  coil geometry of 200 mm outer diameter, 10mm pitch, 6 turns, and made of 14-AWG wire. The maximum transmit power is 100 W with a maximum limit of 2 A and 50 V, which is a similar output from the power supply used in this work.

As illustrated by the results in Fig. 5, the figure-of-merit,  $\Gamma$ , increases with increasing pitch and decreasing number of coil turns. Coils with two or fewer turns are shown here to be suitable, assuming a 1.29 mm wire diameter and 150-mm outer diameter. Figure 6 shows the relationship of the change in coil diameter and change in number of turns to the power



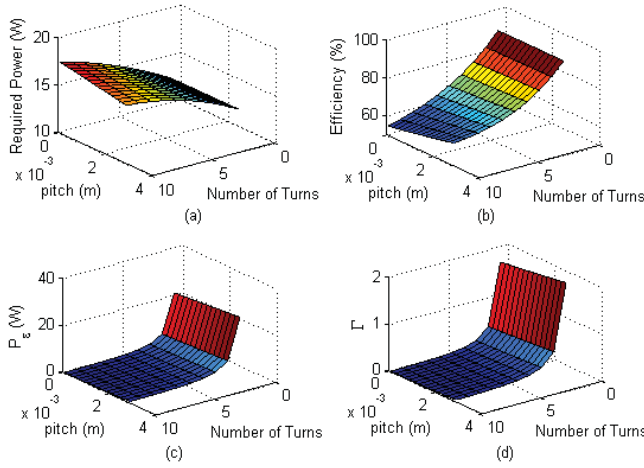


Fig. 5. Performance of the WPT system: (a) power required to lift the MAV, (b) efficiency of the WPT system, (c) power received at the load ( $P_e$ ), and (d) figure-of-merit  $\Gamma$ . In each plot the number of  $R_x$  coil turns and pitch were varied. As the results show, fewer turns with wider spacing between turns results in a greater  $\Gamma$ .

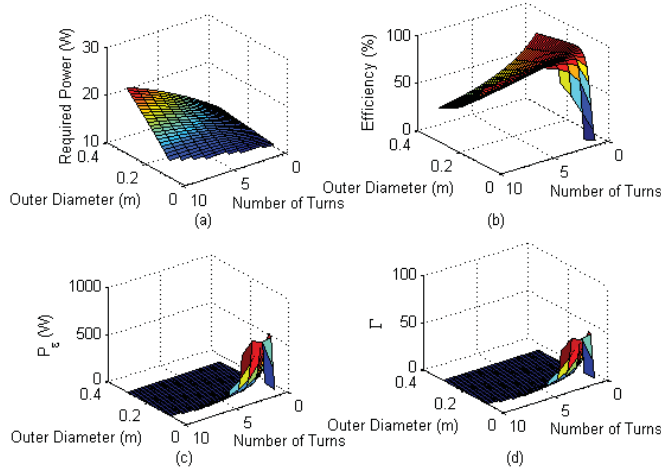


Fig. 6. An example of the relationship between number of  $R_x$  coil turns and  $R_x$  coil diameter: (a) power required to lift the MAV, (b) efficiency of the WPT system, (c)  $P_e$ , and (d)  $\Gamma$ , according to the modeling. As seen, the plot indicates that there is an optimal ridge to maximize the ratio of power transferred to power required.

figure of merit,  $\Gamma$ . The results show a ridge of optimal  $\Gamma$  based on the coil diameter and the number of turns. Figure 7, which shows the relationship between number of turns and wire diameter, indicates that a smaller wire diameter and fewer turns have a higher  $\Gamma$ . Based on the modeling results a suitable  $R_x$  coil is made with 1.29-mm diameter (16 AWG) wire, two coil turns, with an outer diameter of 130 mm and pitch of approximately 1 mm.

## V. POSITIONING SENSING AND CONTROL

The MAV's small size makes it extremely susceptible to drift [14], and accurate position control relative to the wireless power transmit coil is needed to ensure that optimum power is received by the MAV. To sense the relative displacement between the MAV and transmit coil during hover, a magnetic field sensor is designed and characterized.

It has been shown that for a circular shaped  $T_x$  coil

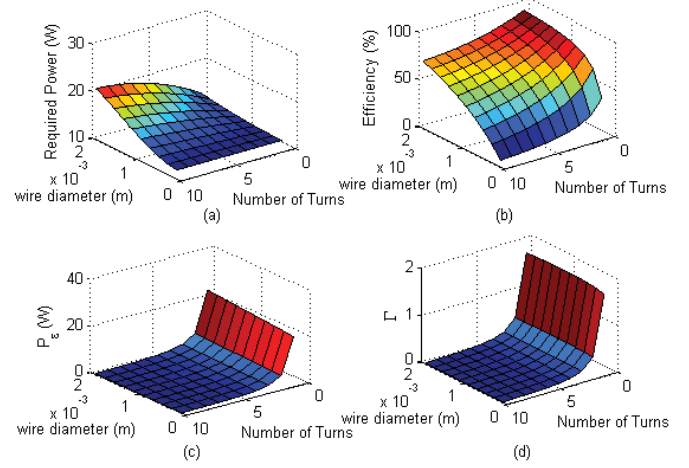


Fig. 7. An example of the effect on the  $\Gamma$  by the number of  $R_x$  coil turns and  $R_x$  wire diameter according to the modeling. The results shown here are (a) power required to lift the MAV, (b) efficiency of the WPT system, (c) power received at the load ( $P_e$ ), and (d)  $\Gamma$ . These results indicate that the  $\Gamma$  is maximized for small wire diameters and low number of turns.

the resulting magnetic field will be a symmetrically-shaped sphere [15]. The flux of the magnetic field is strongest at the center of the coil and decreases at a rate that can be modeled as a polynomial function [16]. Because of this rapid decline in flux and hence power, it is important to avoid  $T_x$  and  $R_x$  coil misalignment and keep the MAV hovering over the  $T_x$  coil. By mapping this magnetic field and through the placement of sensors on the MAV, closed-loop feedback control can be utilized to keep the MAV above the transmit coil.

The magnetic field sensor is an induction coil sensor consisting of a 10-turn solenoid coil made of 39-AWG copper wire with a 10-mm diameter, as shown in the inset in Fig. 8. Magnetic flux from the  $T_x$  coil induces an EMF voltage according to Faraday's Law

$$\epsilon = N \times \frac{d\Phi}{dt}, \quad (16)$$

where the EMF voltage,  $\epsilon$ , is directly proportional to the change in flux,  $\Phi$ , which corresponds with position of the sensor in the magnetic field and the number of turns,  $N$ , on the sensor loop. The most magnetic flux, and consequently the highest sensor voltage, will pass through the sensor coil when it is directly centered above the  $T_x$  coil. Through experimental measurements at 11.5 cm above the transmit coil, the output voltage of the sensor as a function of radial distance from the center of the coil is shown in Fig. 8. Thus, at a given vertical distance,  $z$ , the displacement of the sensor coil in the  $x/y$  plane can be empirically modeled by

$$e_s(H)|_z = a_2 H^2 + a_1 H + a_0, \quad (17)$$

where  $H$  is the radial distance from the center of the  $T_x$  coil to the sensor and  $e_s|_z$  is the EMF sensor voltage at a given vertical distance  $z$ . Using Eq. (17), the horizontal radial distance of the sensor on the MAV relative to the center of the  $T_x$  coil can be approximated and used for position estimation. A design is proposed where four sensors can be placed on the MAV. Three sensors are placed in a triangular configuration each located 60 mm from the center of the MAV.

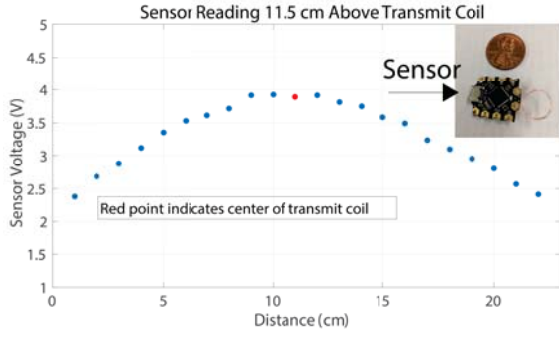


Fig. 8. The magnetic position sensor (inset) and a plot of the sensor readings as a function of radial distance from the center of the transmit coil measured at 11.5 cm above the coil. The center of the  $T_x$  coil is located at 11 cm.

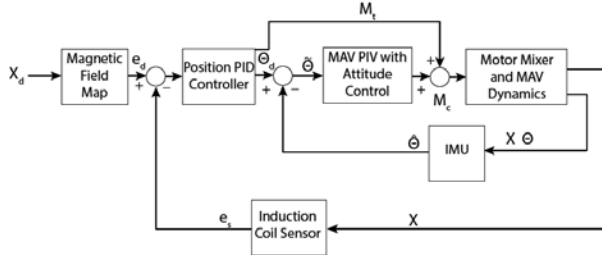


Fig. 9. The block diagram of the control system enabling the MAV to hover in place above the transmit coil of the WPT using the custom-designed magnetic position sensor.

The fourth sensor can be placed in the center of the MAV. The three sensors in the triangular configuration can be used to approximate the gradient of the magnetic field.

Using the sensor output, a feedback controller as illustrated in Fig. 9 can be used to control the position of the MAV to hover at an optimum location relative to the transmit coil. This effort is mapped by the controller into a vector  $\Theta_d = [\phi_d, \theta_d, \psi_d]$ , which contains the Euler angles of roll, pitch and yaw, respectively, and a motor output proportional to the thrust  $M_t$ . The vector  $\Theta$  is compared in negative feedback loop with  $\hat{\Theta}$ , the estimate of the Euler angles from the MAV's IMU. The resulting vector is passed into the MAV's internal attitude controller. The output of the attitude controller is then summed with  $M_t$  to form inputs to the individual motors. It is noted that this controller will keep the MAV hovering above the  $T_x$  coil but it will not be able to control the yaw or horizontal orientation of the MAV relative to the  $T_x$  coil. Additional sensors are required to measure and control the yaw motion. However, since the received power of the MAV is not dependent on its horizontal orientation, the controller will keep the MAV in a position to receive the required power.

## VI. EXPERIMENTAL RESULTS AND DISCUSSION

This section demonstrates WPT to the experimental MAV system described above in Section III. The  $T_x$  coil is made of seven turns and 5-mm pitch with 190 mm outer diameter using 14-AWG copper wire. The  $R_x$  coil is made of a 200 mm diameter, single turn loop using 20-AWG magnet wire. The  $R_x$  coil, rectifier, and DC-DC converter have a mass of 22 g and the MAV consumes approximately 14.7 W to hover with the additional mass of the coil and electronics. The power input to the WPT system was approximately 40 W, with 36%

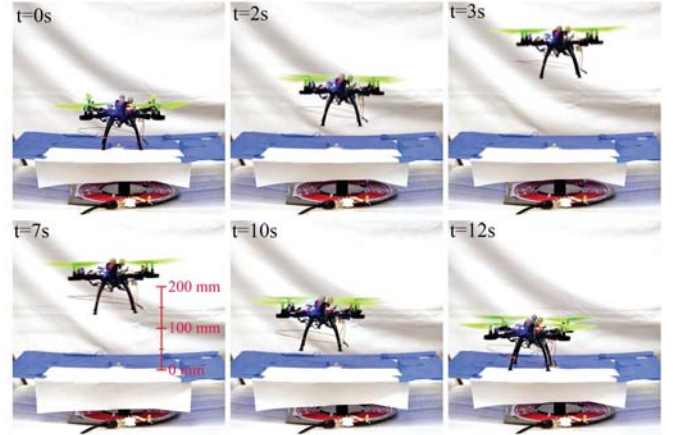


Fig. 10. A working demonstration of the MAV as it hovers using the WPT system, where the MAV is resting on a platform suspended above the  $T_x$  coil by 80 mm and the MAV hovering receiving power and taking off of the platform, and hovering approximately 120 mm above the  $T_x$  coil.

TABLE I

THEORETICAL AND EXPERIMENTAL VALUES OF A 13.7-CM COIL WITH 1-MM PITCH, 2 TURNS, AND 1.29-MM DIAMETER WIRE

	Theoretical	Experimental	% deviation
$L_{R_x}$ ( $\mu$ H)	1.19	1.40	16.2
$C_{R_x}$ (pF)	115.7	93.0	21.5
$N_{R_x}$	2	2	0
pitch (mm)	1	1	0
$D_o$ (mm)	137	137	0
Coil Sep. (mm)	100	100	0
$f_o$ (MHz)	13.56	13.24	2.4
$P_e$ (W)	16.91	15.2	10.65
$P_{in}$ (W)	18.07	18	0.39
$R_L$ ( $\Omega$ )	12.5	12.5	0

efficiency.

Figure 10 shows still frames of the MAV as it takes off and hovers from a platform suspended above the transmit coil. The platform is 80 mm from the  $T_x$  coil and the MAV hovers for an extended period of time approximately 120 mm from the  $T_x$  coil. For this demonstration the MAV's position is controlled through a motion capture system (OptiTrack). Three IR markers were placed on the MAV, enabling the motion capture system to track the MAV's position. The MAV's position was compared in a negative feedback loop with the desired position, and the resulting error was fed into a PID position control loop through a custom built ROS program designed for the Crazyflie 2.0 flight controller allowing the MAV to hover above the  $T_x$  coil.

To further validate the model, two  $R_x$  coils were constructed and tested using a resistive load. The power conditioning electronics and impedance matching tuning were removed from the system to more closely replicate the modeling approach discussed in this work. The summary of the results are found in Tables I and II.

The results shown in the tables indicate that the model is able to reasonably estimate inductance values for coils. In the model, resonating capacitor values are calculated based on the desired resonant frequency and neglect self capacitance of the coil. However, experimentally the self capacitance of the coils has an increasing effect on resonant frequency as

TABLE II

THEORETICAL AND EXPERIMENTAL VALUES OF A 15.3-CM COIL WITH  
2-MM PITCH, 4 TURNS, AND 1.29-MM DIAMETER WIRE

	Theoretical	Experimental	% deviation
$L_{R_x}$ ( $\mu$ H)	4.4	4.6	4.4
$C_{R_x}$ (pF)	31.5	24.3	25.8
$N_{R_x}$	4	4	0
pitch (mm)	2	2	0
$D_o$ (mm)	153	153	0
Coil Sep. (mm)	100	100	0
$f_o$ (MHz)	13.56	13.27	2.2
$P_e$ (W)	15.33	9	52.5
$P_{in}$ (W)	16.0	16	0
$R_L$ ( $\Omega$ )	12.5	12.5	0

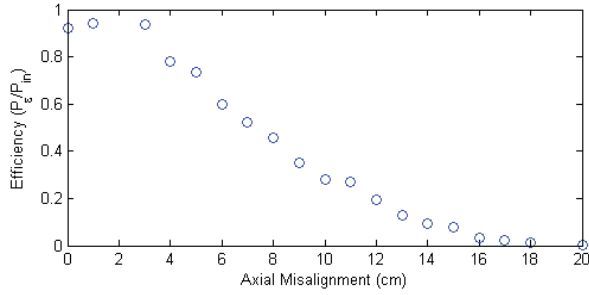


Fig. 11. Plot of how power efficiency at the load through the WPT system is affected by distance from axial alignment between  $T_x$  and  $R_x$  coils. Because the  $R_x$  coil is smaller than the  $T_x$  coil the plot has a small plateau around axial alignment, which indicates that there is approximately a 4-cm radius for which the MAV could move horizontally and still receive sufficient power.

number of coil turns and coil inductance increases. Therefore, experimentally, capacitor values are selected to tune the resonant frequency coil close to the operating frequency. The power delivered to the load matched well for the first  $R_x$  coil but had a larger error with the second  $R_x$  coil. In the case of the 4-turn  $R_x$  coil, if the measured inductance and resonant frequency are used to calculate the capacitance, and the theoretical inductance and calculated capacitance used in the model, then the theoretical  $P_e$  is calculated to be 11.9 W, which results in a percent deviation from experimental of 27.8%.

To determine the sensitivity of the WPT to the MAV's location, the  $R_x$  coil is terminated by a 12.5- $\Omega$  resistor and power efficiency is mapped as the  $R_x$  coil moves from axial alignment with the  $T_x$  coil. No impedance tuning circuits were used for this test. The results of the mapping are shown in Fig. 11. This demonstrates the margin of error that the control system has, which is used to position the MAV to where it can receive enough power.

## VII. CONCLUSIONS

This paper described the design, modeling, analysis, and experimental demonstration of an inductive resonant WPT system sufficient for a MAV to hover. Using a two-coil WPT model, the geometry for the  $T_x$  and  $R_x$  coil was chosen based on simulated performances. The model was validated through experimental results and a proof-of-concept was demonstrated by successfully powering a MAV, enabling it to hover. Additionally, a sensing and control system that would allow the MAV to remain within the WPT charging path was proposed. Future work will focus on validating the

proposed control system based on the WPT field, investigating different coil materials as well as additional coil geometries (i.e., square, solenoid, etc.), and the use of multiple  $R_x$  coils on the MAV.

## VIII. ACKNOWLEDGMENTS

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