

IFT2105 Devoir1

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1 Programme RÉPÉTER et TANQUE

a. Sommaire d'entiers

```
#SOMME D'ENTIERES

repetier r2 fois {
  inc(r5)
  r3 <- PREMIERK(r5)
  r1 = DIV(r1, r3)
  repetier r1 fois{
    inc(r4)
  }
}

r0 <- r4
```

b. FRACTRAN

```
#FRACTRAN:
#ON ASSUME QUE LES TABLEAUX SONT INDEXES A PARTIR DE 1 POUR TABLVAL

tant que r5 != r3{
  inc(r5)
  r6 <- TABLVAL(r1, x)
  r7 <- TABLVAL(r2, x)
  r8 <- PGCD(r6, r7)
  r6 <- DIV(r6, r8)
  r7 <- DIV(r7, r8)
  si EQ(MOD(MULT(r6, r4), r7), 0) {
    r3 <- DIV(MULT(r4, r6), r7)
    r5 <- 0
  }
}

r0 <- r4
```

2 Langage régulier

- a. $\Sigma = \{a, b\}$ et $L = \{w \in \Sigma^* \mid |w|_a = 2 \text{ ou } |w|_b = 3\}$

description textuelle:

$$M = \{Q, \Sigma, \delta, q_0, F\}$$

où

$$Q = \{ \langle a_i b_j \rangle \mid i = 0, 1, 2, 3; j = 0, 1, 2, 3, 4 \}$$

$$q_0 = \langle a_0 b_0 \rangle$$

$$F = \{ \langle a_i b_j \rangle \mid i = 2 \text{ ou } j = 3 \}$$

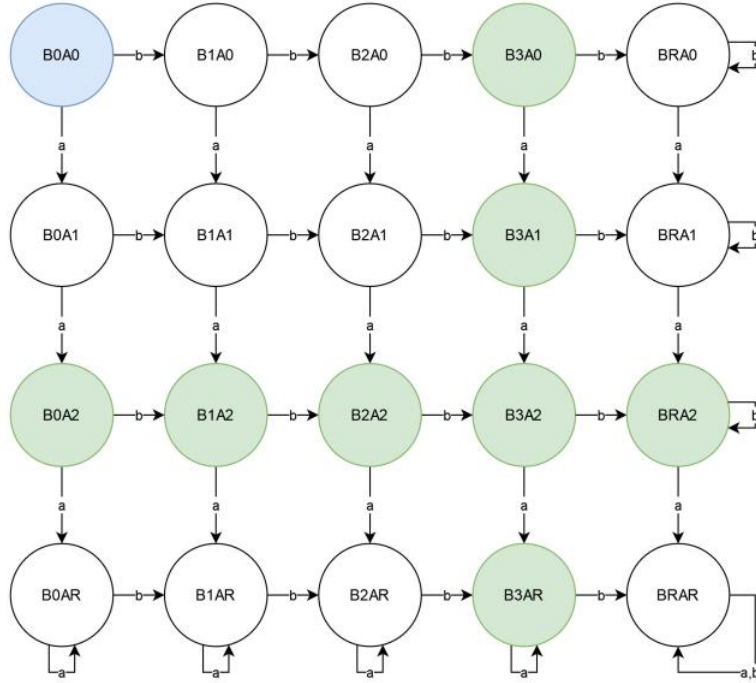
δ est donné par

$$\delta(\langle a_i b_j \rangle, a) = \langle a_{i+1} b_j \rangle, i = 0, 1, 2; \forall j;$$

$$\delta(\langle a_i b_j \rangle, b) = \langle a_i b_{j+1} \rangle, j = 0, 1, 2, 3; \forall i;$$

$$\delta(\langle a_i b_j \rangle, b) = \langle a_i b_j \rangle, i = 3; \forall j;$$

$$\delta(\langle a_i b_j \rangle, b) = \langle a_i b_j \rangle, j = 4; \forall i;$$



Bleu: État initial
Vert: État acceptant

Figure 1: solution 2.a

- b. $\Sigma = \{a, b\}$ et $L = \{w \in \Sigma^* \mid |w|_a \equiv |w|_b + 1 \pmod{3}\}$

Bleu: État initial
Vert: État acceptant

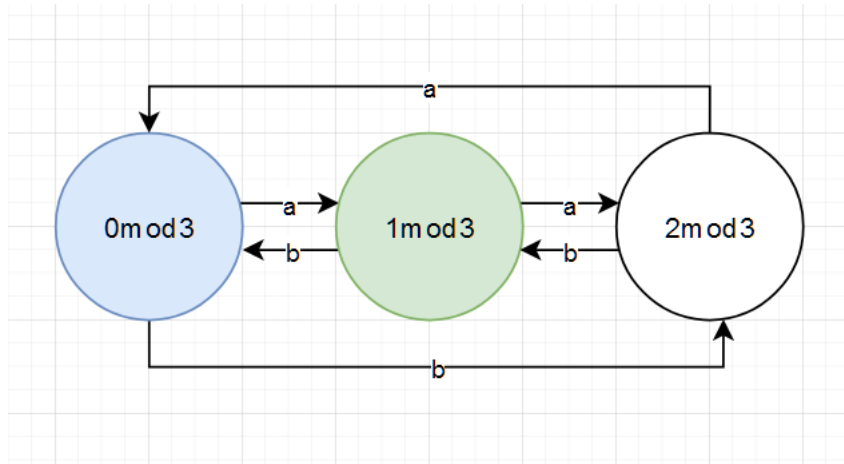


Figure 2: solution 2.b

- c. $\Sigma = \{0, 1\}$ et $L = \{w \in \Sigma^* \mid w^r \equiv 2 \pmod{5}\}$

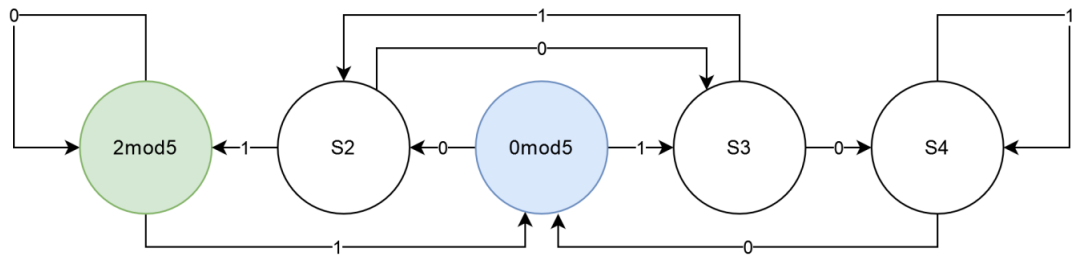


Figure 3: solution 2.c

Bleu: État initial
Vert: État acceptant