

# R documentation

of all in ‘man’

May 9, 2018

## R topics documented:

bsplineBasis . . . . .	1
CubicPowerBasisSpline . . . . .	2
natural_cubic_splines . . . . .	3
natural_cubic_splines.eval_basis . . . . .	4
natural_cubic_splines.predict . . . . .	4
natural_cubic_splines.train . . . . .	5
place_knots . . . . .	6

<b>Index</b>	<b>7</b>
--------------	----------

---

bsplineBasis	<i>Regression using B-spline basis</i>
--------------	--

---

## Description

This function provides nonparametric regressions using B-splines. The B-splines are defined following the recursive formulas due to de Boor. Only univariate input can be used.

## Usage

```
bsplineBasis(x, y, x_test, order = 4, innerknots)
```

## Arguments

x	The input vector of training dataset.
y	The output vector of training dataset.
x_test	The input values at which evaluations are required.
order	The order of B-spline functions. The default is order=4 for cubic B-splines.
innerknots	The internal knots that define the spline.

**Value**

A list with the following components:

beta	The coefficients of nonparametric regression.
basis	The B-spline basis matrix of dimension $c(\text{length}(x), \text{df})$ . $\text{df} = \text{length}(\text{innerknots}) + \text{order}$ .
f	The evaluated output at $x\_test$ .

**Examples**

```
x<-seq(0, 1, 0.001)
y <- x^3 * 3 - x^2 * 2 + x + exp(1)+rnorm(length(x),0,0.1)
plot(x,y)

innerknots <- c(0.1,0.2,0.3,0.4,0.5,0.6,0.7,0.8,0.9)
order<-4
x_test<-seq(0, 1, 0.01)

b_fit<-bspline(x,y,x_test,order,innerknots)

plot(x_test,b_fit$f)
lines(x_test,x_test^3 * 3 - x_test^2 * 2 + x_test + exp(1),col="red")

plot(x,rep(0,length(x)),type="l",ylim=c(0,1))
for (i in 1: (j+order)){
  lines(x,b_fit$basis[,i])
}
```

---

CubicPowerBasisSpline *Regression using cubic spline*

---

**Description**

This function provides regressions using cubic splines. The cubic splines are defined as  $h_1 = 1, h_2 = x, h_3 = x^2, h_4 = x^3, h_5 = (x-k_1)^3+, h_6 = (x-k_2)^3+, \dots$ , where  $k_1, k_2$  and  $k_n$  are  $n$  knots, '+' denotes the positive part.

**Usage**

```
CubicPowerBasisSpline(x, y, x_test, innerknots)
```

**Arguments**

x	The input vector of training dataset.
y	The output vector of training dataset.
x_test	The input values at which evaluations are required.
innerknots	The internal knots that define the spline.

**Details**

Only univariate input can be used.

**Value**

A list with the following components:

beta	The coefficients of nonparametric regression.
basis	The cubic spline basis matrix of dimension $c(\text{length}(x), \text{NumKnots}+4)$
f	The evaluated output at $x_{\text{test}}$ .

**Examples**

```
n <- 100
t <- seq(0,2*pi,length.out = 100)
a <- 3
b <- 2
c.unif <- runif(n)
amp <- 2
set.seed(1)
y1 <- a*sin(b*t)+c.unif*amp # uniform error
innerknots <- 2*pi*c(1/4,2/4,3/4)
solution <- CubicPowerBasisSpline(t,y1,t,innerknots)
y.hat <- solution$f
plot(t, y1, t="l")
lines(t, y.hat, col=4)
```

---

natural\_cubic\_splines    *Regression using natural cubic splines*

---

**Description**

This function provides regressions using natural cubic splines with truncated power basis functions. Only univariate input can be used.

**Usage**

```
natural_cubic_splines(x_train, y_train, x_test, df = NULL, knots = NULL)
```

**Arguments**

x_train	The input vector of training dataset.
y_train	The output vector of training dataset.
x_test	The input values at which evaluations are required.
df	The degree of freedom specified by user, number of knots will be equal to df.
knots	Knots location in terms of quantiles of $x_{\text{train}}$ , optional, default will be evenly spaced quantiles based on number of knots.

**Value**

y\_pred                      A vector of dimension  $\text{length}(x)$  The prediction vector evaluated at  $x_{\text{test}}$  values

**Examples**

```

x_train <- seq(0, 1, 0.001)
y_train <- x^3 * 3 - x^2 * 2 + x + exp(1) + rnorm(length(x), 0, 0.1)
plot(x, y)
df <- 10
x_test <- seq(0, 1, 0.01)
y_pred <- natural_cubic_splines(x, y, x_test, df)
plot(x_test, y_pred)
lines(x_test, x_test^3 * 3 - x_test^2 * 2 + x_test + exp(1), col="red")

```

---

natural\_cubic\_splines.eval\_basis

*Evaluate basis functions at each x and return the evaluated basis matrix N*

---

**Description**

Evaluate basis functions at each x and return the evaluated basis matrix N

**Usage**

```
natural_cubic_splines.eval_basis(x, knots, nknots)
```

**Arguments**

x	Predictor variable vector
knots	Knots location in terms of quantiles of x_train, optional, default will be evenly spaced quantiles based on number of knots
nknots	Number of knots used in training.

**Value**

Basis matrix evaluated at each x value

---

natural\_cubic\_splines.predict

*Prediction based on trained regression model*

---

**Description**

Prediction based on trained regression model

**Usage**

```
natural_cubic_splines.predict(x_test, betas, knots, nknots)
```

**Arguments**

x_test	The input values at which evaluations are required.
betas	Least square fit parameters obtained from training.
knots	Knots location in terms of quantiles of x_train, optional, default will be evenly spaced quantiles based on number of knots
nknots	Number of knots used in training.

**Value**

y_pred	A vector of dimension length(x)The prediction vector evaluated at x_test values
--------	---

---

natural\_cubic\_splines.train

*Generate an evaluated basis matrix for natural cubic splines*

---

**Description**

Generate an evaluated basis matrix for natural cubic splines

**Usage**

```
natural_cubic_splines.train(x_train, y_train, df = NULL, knots = NULL,
  intercept = FALSE)
```

**Arguments**

x_train	The input vector of training dataset.
y_train	The output vector of training dataset.
df	The degree of freedom specified by user, number of knots will be equal to df.
knots	Knots location in terms of quantiles of x_train, optional, default will be evenly spaced quantiles based on number of knots
intercept	Default false, do not change.

**Value**

A list of following components:

```
knots
N
betas
```

**Examples**

```
x_train <- seq(0, 1, 0.001)
y_train <- x^3 * 3 - x^2 * 2 + x + exp(1) + rnorm(length(x), 0, 0.1)
plot(x, y)
df <- 10
x_test <- seq(0, 1, 0.01)
train_result <- natural_cubic_splines.train(x, y, df)
print(train_result$betas)
print(train_result$N[1:5, 1:5])
```

---

place_knots	<i>Find evenly spaced out knots by quantile</i>
-------------	---

---

**Description**

Find evenly spaced out knots by quantile

**Usage**

```
place_knots(nknots, x)
```

**Arguments**

nknots	Number of knots to be located.
x	Data vector on which knots are placed.

**Value**

A named vector with knot quantiles and values

# Index

`bsplineBasis`, [1](#)

`CubicPowerBasisSpline`, [2](#)

`natural_cubic_splines`, [3](#)

`natural_cubic_splines.eval_basis`, [4](#)

`natural_cubic_splines.predict`, [4](#)

`natural_cubic_splines.train`, [5](#)

`place_knots`, [6](#)