# **GR** notes

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Conventions	

- 1. Greek index (e.g.  $\alpha, \beta, \mu, \nu$ ) take value from  $\{0, 1, 2, 3\}$ .
- 2. Events denoted by cursive capitals (e.g.  $\mathscr{A}, \mathscr{B}, \mathscr{E}$ ).
- 3.  $(x^0, x^1, x^2, x^3) \equiv (t, x, y, z) \equiv x^{\alpha}$
- 4. Latin index (e.g.i, j, k) take value from  $\{1, 2, 3\}$ .
- 5. New unit that speed of light c=1

## 1 Special Relativity

### 1.1 4-Dimensional Spacetime

#### **Definition 1.1.** Inertial coordinate

The coordinate system must satisfy three property to be consider inertial coordinat:

- 1. The distance between two points are independent of time.
- 2. The clocks at every points ticking off time coordinate t at same rate.
- 3. The geometry of space is always Euclidean (flat).

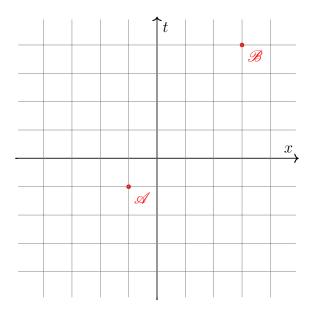


Figure 1: two events with coordinate (-1, -1, 0, 0) and (4, 3, 0, 0).

The event in 4-D spacetime is define by a set of coordinate (t, x, y, z). For simplicity, we assume those events have y = 0, z = 0 so that we can draw a 2D graph to represent them.

Analog to Euclidean geometry, just like the euclidean distance  $\Delta l^2 = \Delta x^2 + \Delta y^2 + \Delta z^2$ , we define the spacetime interval  $\Delta s^2 = -\Delta t^2 + \Delta x^2 + \Delta y^2 + \Delta z^2$ .

**Remark.** There are a lot different conventions to define the sign of interval, here we just use the popular one (-,+,+,+).

#### Example.

Interval for the two events in Figure 1 is  $\Delta s^2 = -\Delta t^2 + \Delta x^2 + \Delta y^2 + \Delta z^2 = -9$ .