Table 1: A performance comparison between the ϵ -constraint and BOBLB&B&C algorithms.

			ϵ -constraint	B&B		EPB B&C (ISC) (Λ)		Cut&Branch	
Instance	n	m	Time(s)	Time(s)	#Nodes	Time(s)	#Nodes	Time(s)	#Nodes
MDMKP_n10_m2_q1_0.25	10	2	2.84	1.61	107	0.95	1	0.47	1
MDMKP_n10_m2_q1_0.5	10	2	3.88	1.79	393	2.87	50	2.36	277
MDMKP_n10_m2_q1_0.75	10	2	3.01	1.67	259	2.46	16	2.22	107
MDMKP_n10_m2_q2_0.25	10	2	2.87	1.66	181	2.37	19	2.22	97
MDMKP_n10_m2_q2_0.5 MDMKP_n10_m2_q2_0.75	10 10	$\frac{2}{2}$	3.88 2.83	$1.7 \\ 1.64$	229 65	$2.76 \\ 1.84$	33 19	$2.3 \\ 2.19$	161 59
MDMKP n20 m2 q1 0.25	20	2	5.4	19.12	34877	3.45	159	4.84	2669
MDMKP_n20_m2_q1_0.5	20	2	8.05	94.6	139437	4.42	361	6.87	5207
MDMKP_n20_m2_q1_0.75	20	2	5.69	3.99	1903	3.76	155	4.28	1527
MDMKP_n20_m2_q2_0.25	20	2	6.77	6.27	10379	4.14	220	4.81	1859
MDMKP_n20_m2_q2_0.5	20	2	5.4	20.7	26139	7.38	781	10.29	8019
MDMKP_n20_m2_q2_0.75 MDMKP_n20_m4_q1_0.25	20 20	$\frac{2}{4}$	4.03 4.82	3.13 9.28	1751 13611	3.53 5.13	146 167	3.34 4.87	811 2701
MDMKP n20 m4 q1 0.5	20	4	5.62	19.3	23193	7.96	584	7.11	4317
MDMKP n20 m4 q1 0.75	20	4	5.46	8.25	10037	4.63	268	5.35	3563
MDMKP_n20_m4_q2_0.25	20	4	4.44	5.56	7043	3.78	149	3.89	1195
$MDMKP_n20_m4_q2_0.5$	20	4	5.77	30.73	29217	11.72	885	13.38	8253
MDMKP_n20_m4_q2_0.75	20	4	4.22	7.85	5611	4.34	111	4.51	1377
MDMKP_n20_m4_q4_0.25 MDMKP_n20_m4_q4_0.5	20 20	$\frac{4}{4}$	$5.89 \\ 6.57$	5.15 19.54	5011 18213	5.51 17.2	321 1339	4.62 16.63	3119 14891
MDMKP n20 m4 q4 0.75	20	4	4.98	3.36	2063	$\frac{17.2}{4.42}$	117	4.02	14091
MDMKP n30 m2 q1 0.25	30	2	9.31	3549.99	2553847	26.09	4667	75.23	35753
MDMKP_n30_m2_q1_0.5	30	$\overline{2}$	13.1	1953.31	793651	29.72	4968	267.25	124975
MDMKP_n30_m2_q1_0.75	30	2	7.26	175.81	108371	10.31	1457	52.82	27023
MDMKP_n30_m2_q2_0.25	30	2	12.92	536.24	333799	20.62	3257	139.97	80499
MDMKP_n30_m2_q2_0.5	30	2	10.12	1783.2	1062045	32.18	3656	206.32	132767
MDMKP_n30_m2_q2_0.75 MDMKP_n30_m4_q1_0.25	30 30	$\frac{2}{4}$	6.94 7.11	17.12 689.02	8905 468263	6.88 193.61	630 20998	9.65 156.9	$3991 \\ 78503$
MDMKP n30 m4 q1 0.5	30	4	9.05	TL	1000901	224.61	26285	807.25	312375
MDMKP_n30_m4_q1_0.75	30	4	5.84	330.69	141019	39.33	4206	51.8	19385
MDMKP_n30_m4_q2_0.25	30	4	9.15	766.61	746357	49.29	4742	87.3	43163
$MDMKP_n30_m4_q2_0.5$	30	4	5.54	3375.34	1960679	27.85	2522	63.33	30781
MDMKP_n30_m4_q2_0.75	30	4	7.7	284.83	122047	27.99	3351	76.12	29767
MDMKP_n30_m4_q4_0.25	30 30	$\frac{4}{4}$	7.14 11.14	$416.02 \\ 2342.68$	330739 830987	$36.69 \\ 322.95$	$3506 \\ 31212$	54.03 1210.58	$\begin{array}{c} 26635 \\ 402423 \end{array}$
MDMKP_n30_m4_q4_0.5 MDMKP_n30_m4_q4_0.75	30	4	6.13	166.88	155613	36.89	3061	66.36	50885
MDMKP n30 m6 q1 0.25	30	6	6.3	639.99	630457	55.78	5580	60.82	34173
MDMKP_n30_m6_q1_0.5	30	6	12.78	TL	982945	1295.86	171149	2444.64	845293
MDMKP_n30_m6_q1_0.75	30	6	7.33	414.99	210013	128.5	14832	213.44	104069
MDMKP_n30_m6_q3_0.25	30	6	12.1	239.2	207343	857.11	98061	177.18	123775
MDMKP_n30_m6_q3_0.5	30 30	6 6	14.47 4.73	TL	$\begin{array}{r} 1259961 \\ 99497 \end{array}$	$775.2 \\ 22.8$	84772 1798	766.6	282721 18855
MDMKP_n30_m6_q3_0.75 MDMKP_n30_m6_q6_0.25	30 30	6	4.73	168.85 98.74	92555	$\frac{22.8}{17.95}$	922	46.63 25.41	14069
MDMKP_n30_m6_q6_0.5	30	6	6.95	772.88	771663	152.54	12261	128.91	82117
MDMKP_n30_m6_q6_0.75	30	6	4.49	81.99	46695	30.77	2059	29.18	18939
MDMKP_n40_m2_q1_0.25	40	2	14.21	TL	824379	189.06	24130	2010.25	528517
MDMKP_n40_m2_q1_0.5	40	2	13.89	TL	447465	277.73	34614	2491.88	826361
MDMKP_n40_m2_q1_0.75	40	2	6.65	619.68	225357	18.56	2585	139.29	53659
MDMKP_n40_m2_q2_0.25 MDMKP_n40_m2_q2_0.5	40 40	$\frac{2}{2}$	12.23 16.28	${ m TL}$ ${ m TL}$	$\frac{1102005}{542459}$	52.34 270.67	6653 32775	892.83 3121.58	$425449 \\ 1305391$
MDMKP n40 m2 q2 0.75	40	2	12.22	2385.94	631379	66.34	9201	260.35	113349
MDMKP_n40_m4_q1_0.25	40	4	7.21	TL	973269	123.89	12500	718.87	273853
$MDMKP_n40_m4_q1_0.5$	40	4	13.34	TL	352819	1100.93	128201	TL	648775
MDMKP_n40_m4_q1_0.75	40	4	14.17	TL	553077	382.48	44739	1670.45	356459
MDMKP_n40_m4_q2_0.25 MDMKP_n40_m4_q2_0.5	40	4	13.69	$_{ m TL}$	889325	811.88	85129 228404	TL	684493 317645
MDMKP_n40_m4_q2_0.5 MDMKP n40 m4 q2 0.75	40 40	$\frac{4}{4}$	18.51 19.17	$rac{ ext{TL}}{ ext{TL}}$	331119 791437	2027.7 2024.87	228404 237418	$\frac{\text{TL}}{3397.21}$	317645 940493
MDMKP n40 m4 q4 0.25	40	4	13.86	$^{ m TL}$	740819	824.85	75434	2826.89	771221
MDMKP_n40_m4_q4_0.5	40	4	30.4	TL	363581	TL	369249	$^{2020.00}$	369333
MDMKP_n40_m4_q4_0.75	40	4	9.79	TL	801357	172.02	17562	1101.94	331739
MDMKP_n40_m6_q1_0.25	40	6	10.76	TL	925841	1162.29	131823	2377.05	771507
MDMKP_n40_m6_q1_0.5	40	6	15.95	TL	294625	TL	385164	TL	355783
MDMKP_n40_m6_q1_0.75 MDMKP_n40_m6_q3_0.25	40 40	6 6	6.98 29.7	$_{ m TL}$	742787 706235	362.69 TL	39374 339800	828.74 TL	268147 644075
MDMKP_n40_m6_q3_0.25 MDMKP_n40_m6_q3_0.5	40	6	44.46	$^{ m TL}$	273251	$^{ m TL}$	390183	$^{ m TL}$	264585
MDMKP_n40_m6_q3_0.75	40	6	9.44	$^{ m TL}$	681439	560.5	55006	519.99	116475
MDMKP_n40_m6_q6_0.25	40	6	14.96	TL	1002671	1059.64	93326	3521.03	1282609
$MDMKP_n40_m6_q6_0.5$	40	6	34.22	TL	243335	TL	304486	TL	245411
MDMKP_n40_m6_q6_0.75	40	6	11.45	3026.65	642001	638.08	62329	1328.78	321287
MDMKP_n40_m8_q1_0.25	40	8 8	7.48	TL	1264237	490.63	43376	1088.6	318309
MDMKP_n40_m8_q1_0.5	40	ð	8.11	TL	339329	1455.44	145310	1980.82	391221

MDMKP_n40_m8_q1_0.75	40	8	7.23	TL	599887	616.96	65588	891.9	207127
MDMKP_n40_m8_q4_0.25	40	8	18.61	TL	1177239	2674.74	244723	1581.75	534277
MDMKP_n40_m8_q4_0.5	40	8	22.39	TL	301637	TL	312311	TL	295315
MDMKP_n40_m8_q4_0.75	40	8	10.01	TL	734301	694.89	58426	938.92	232515
MDMKP_n40_m8_q8_0.25	40	8	34.77	2617.5	1272087	2335.17	176194	1514.59	600343
MDMKP_n40_m8_q8_0.5	40	8	60.86	TL	273349	TL	297080	TL	253041