Table 1: A performance comparison between the ϵ -constraint and BOBLB&B&C algorithms.

			ϵ -constraint	B&B		EPB B&C (ISC) ($ \Lambda $)		Cut&Branch	
Instance	n	m	Time(s)	Time(s)	#Nodes	Time(s)	#Nodes	Time(s)	#Nodes
KP_p-3_n-100_ins-1.dat	100	1	24.54	TL	117493	705.62	52074	TL	114271
KP_p-3_n-100_ins-10.dat	100	1	28.74	$_{ m TL}$	125371	2292.23	159657	TL	137589
KP_p-3_n-100_ins-2.dat KP_p-3_n-100_ins-3.dat	100 100	1 1	21.19 24.71	$_{ m TL}$	$\frac{142583}{118553}$	671.96 883.31	48269 59841	$_{ m TL}$	$\frac{149391}{113895}$
KP p-3 n-100 ins-4.dat	100	1	47.22	$^{ m TL}$	114125	3423.36	226243	TL	100097
KP_p-3_n-100_ins-5.dat	100	1	37.27	TL	108747	2527.95	174890	TL	100771
KP_p-3_n-100_ins-6.dat	100	1	29.53	$_{ m TL}$	124825	1459.95	97854	TL	117529
KP_p-3_n-100_ins-7.dat KP p-3 n-100 ins-8.dat	100 100	1 1	19.83 30.67	$_{ m TL}$	$173589 \\ 122739$	$650.37 \\ 2077.82$	43955	${ m TL}$	177197
KP_p-3_n-100_ins-8.dat KP_p-3_n-100_ins-9.dat	100	1	28.43	$^{ m TL}$	121213	935.28	$\frac{144664}{67502}$	$^{ m TL}_{ m TL}$	$\frac{134497}{144919}$
KP_p-3_n-10_ins-1.dat	10	1	3.27	1.51	169	0.06	21	2.43	57
KP_p-3_n-10_ins-10.dat	10	1	3.5	1.44	177	0.09	28	2.95	111
KP_p-3_n-10_ins-2.dat	10	1	3.88	1.6	751	0.19	51	2.77	423
KP_p-3_n-10_ins-3.dat KP_p-3_n-10_ins-4.dat	10 10	1 1	$3.28 \\ 3.27$	1.54 1.49	473 129	$0.0 \\ 0.05$	1 15	$0.4 \\ 2.64$	$\begin{array}{c} 1 \\ 73 \end{array}$
KP p-3 n-10 ins-5.dat	10	1	3.95	1.45	443	0.03 0.14	42	3.02	277
KP_p-3_n-10_ins-6.dat	10	1	3.64	1.47	265	0.06	19	2.56	123
$KP_p-3_n-10_ins-7.dat$	10	1	3.43	1.6	609	0.06	21	2.47	139
KP_p-3_n-10_ins-8.dat	10	1	3.56	1.53	251	0.12	33	2.61	131
KP_p-3_n-10_ins-9.dat KP p-3 n-20 ins-1.dat	10 20	1 1	3.43 4.09	1.56 11.9	461 21121	$0.08 \\ 0.63$	24 126	$2.56 \\ 4.46$	87 3077
KP p-3 n-20 ins-10.dat	20	1	3.88	12.9	12595	0.62	120	4.26	1467
KP_p-3_n-20_ins-2.dat	20	1	4.21	8.52	5949	0.61	122	4.43	737
$KP_p-3_n-20_ins-3.dat$	20	1	4.32	3.63	2955	0.69	127	3.94	889
KP_p-3_n-20_ins-4.dat	20	1	3.98	5.71	9127	0.5	87	3.62	983
KP_p-3_n-20_ins-5.dat KP_p-3_n-20_ins-6.dat	20 20	1 1	5.0 3.83	15.61 16.33	10837 19097	$1.39 \\ 0.67$	$302 \\ 102$	$7.78 \\ 3.57$	3043 1183
KP_p-3_n-20_ins-7.dat	20	1	4.53	5.51	3509	0.8	163	4.82	1405
KP_p-3_n-20_ins-8.dat	20	1	4.25	9.9	18793	0.59	92	4.24	1669
$KP_p-3_n-20_ins-9.dat$	20	1	4.5	13.48	12373	0.74	165	4.74	1405
KP_p-3_n-30_ins-1.dat	30	1	5.09	88.01	81077	3.75	577	14.01	11523
KP_p-3_n-30_ins-10.dat KP p-3 n-30 ins-2.dat	30 30	1 1	4.86 4.86	52.31 171.71	37209 138815	$2.79 \\ 2.17$	$427 \\ 342$	7.34 12.96	$2853 \\ 5657$
KP p-3 n-30 ins-3.dat	30	1	5.39	160.4	104753	3.52	512	23.7	11155
KP_p-3_n-30_ins-4.dat	30	1	4.42	56.58	98343	1.56	247	7.77	6403
KP_p-3_n-30_ins-5.dat	30	1	5.35	54.53	45701	3.0	462	10.79	6053
KP_p-3_n-30_ins-6.dat	30	1	4.99	174.26	88373	2.57	398	12.03	4143
KP_p-3_n-30_ins-7.dat KP_p-3_n-30_ins-8.dat	30 30	1 1	5.43 3.89	130.76 138.09	85591 163167	$\frac{2.5}{0.86}$	442 132	$26.82 \\ 6.81$	14837 3449
KP_p-3_n-30_ins-9.dat	30	1	4.06	61.42	61839	1.6	239	4.83	2007
KP_p-3_n-40_ins-1.dat	40	1	10.85	1127.83	416541	30.15	3723	305.78	110739
$KP_p-3_n-40_ins-10.dat$	40	1	6.98	427.93	201071	11.2	1424	198.01	80313
KP_p-3_n-40_ins-2.dat	40	1	4.9	410.78	293999	3.43	397	29.28	17843
KP_p-3_n-40_ins-3.dat KP p-3 n-40 ins-4.dat	40 40	1 1	7.08 7.34	661.87 411.7	330229 202315	25.06 9.18	2966 1243	$127.1 \\ 83.84$	77037 35711
KP_p-3_n-40_ins-5.dat	40	1	6.25	195.14	89405	8.74	1216	28.1	10959
KP_p-3_n-40_ins-6.dat	40	1	6.51	974.94	533111	5.67	769	175.29	92505
$KP_p-3_n-40_ins-7.dat$	40	1	6.03	390.71	168359	7.41	1044	73.0	32859
KP_p-3_n-40_ins-8.dat	40	1	5.19	255.48	126623	3.6	477	17.68	7801
KP_p-3_n-40_ins-9.dat KP_p-3_n-50_ins-1.dat	40 50	1 1	$4.54 \\ 8.2$	249.14 3396.44	123349 791843	3.22 23.21	$\frac{288}{2695}$	11.44 868.56	4305 231455
KP_p-3_n-50_ins-1.dat	50	1	10.63	1878.02	537177	45.23	5284	250.33	85045
KP_p-3_n-50_ins-2.dat	50	1	7.43	1554.52	556121	10.37	1375	263.51	84009
$KP_p-3_n-50_ins-3.dat$	50	1	8.21	1041.98	236569	45.63	4650	139.82	45341
KP_p-3_n-50_ins-4.dat	50	1	8.95	2376.67	754917	23.03	2460	703.21	217873
KP_p-3_n-50_ins-5.dat	50	1	9.72	2606.89	718235	51.47	5245	616.2	169213
KP_p-3_n-50_ins-6.dat KP_p-3_n-50_ins-7.dat	50 50	1 1	7.08 12.83	910.89 3451.32	320875 892759	14.84 54.47	1800 6163	174.23 1340.8	65713 343499
KP_p-3_n-50_ins-8.dat	50	1	7.33	1208.39	286477	22.29	2388	169.03	43257
KP_p-3_n-50_ins-9.dat	50	1	8.31	1105.04	373805	20.63	2363	194.56	69129
KP_p-3_n-60_ins-1.dat	60	1	9.07	$_{ m TL}$	620951	46.21	4334	928.08	204957
KP_p-3_n-60_ins-10.dat	60 60	1	11.53	$_{ m TL}$	470763	86.11	8489 10075	1693.76 507.67	374047
KP_p-3_n-60_ins-2.dat KP_p-3_n-60_ins-3.dat	60 60	1 1	11.05 8.95	TL	467547 859799	92.34 46.61	$10075 \\ 4588$	597.67 805.02	$\frac{143075}{231101}$
KP_p-3_n-60_ins-4.dat	60	1	10.29	$^{ m TL}$	671153	50.84	5410	1481.71	388987
KP_p-3_n-60_ins-5.dat	60	1	9.94	3516.32	642995	48.53	5010	783.95	181455
KP_p-3_n-60_ins-6.dat	60	1	10.87	TL	477293	44.42	4132	1016.92	246169
KP_p-3_n-60_ins-7.dat	60	1	12.67	$_{ m TL}$	639245	84.5	7928	1092.27	254515
KP_p-3_n-60_ins-8.dat KP p-3 n-60 ins-9.dat	60 60	1 1	14.53 12.54	$_{ m TL}$	323855 313091	88.06 121.62	9122 11497	$_{ m TL}$	376061 458979
KP_p-3_n-70_ins-1.dat	70	1	12.34 12.17	$^{ m TL}$	227657	121.02 103.17	8500	2101.46	284807
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KP_p-3_n-70_ins-10.dat	70	1	10.18	TL	403475	76.83	7775	2578.54	525681
$KP_p-3_n-70_ins-2.dat$	70	1	9.68	TL	290347	44.27	4324	2954.58	431701
KP_p-3_n-70_ins-3.dat	70	1	16.85	TL	247995	496.53	43556	2812.9	567605
KP_p-3_n-70_ins-4.dat	70	1	8.28	TL	428153	61.16	6448	1245.71	269021
KP_p-3_n-70_ins-5.dat KP p-3 n-70 ins-6.dat	70 70	1 1	12.19 17.38	${ m TL}$	$\begin{array}{c} 275257 \\ 281053 \end{array}$	111.13 341.25	10290 29624	1790.07 TL	305253 558635
KP p-3 n-70 ins-7.dat	70 70	1	11.52	TL	312615	68.05	6580	1411.88	274591
KP_p-3_n-70_ins-8.dat	70	1	12.18	TL	208349	132.23	11264	2319.14	437903
KP p-3 n-70 ins-9.dat	70	1	14.77	TL	304809	156.85	13996	TL	358761
KP_p-3_n-80_ins-1.dat	80	1	12.72	TL	192695	194.17	16501	TL	255197
KP_p-3_n-80_ins-10.dat	80	1	14.86	TL	244877	263.94	20676	TL	326467
$KP_p-3_n-80_ins-2.dat$	80	1	19.94	TL	180475	305.48	24014	TL	186813
KP_p-3_n-80_ins-3.dat	80	1	34.5	$_{ m TL}$	158459	1660.92	131430	$_{ m TL}$	167819
KP_p-3_n-80_ins-4.dat	80	1	22.69	TL	187183	411.33	31797	TL	205605
KP_p-3_n-80_ins-5.dat KP_p-3_n-80_ins-6.dat	80 80	1 1	12.35 22.25	$_{ m TL}$	$\begin{array}{c} 223417 \\ 205911 \end{array}$	158.08 369.99	14166 31287	$\begin{array}{c} 2558.52 \\ \text{TL} \end{array}$	367331 265371
KP p-3 n-80 ins-7.dat	80	1	22.38	$^{ m TL}$	151975	708.65	55705	$^{ m TL}$	218713
KP_p-3_n-80_ins-8.dat	80	1	32.3	TL	133873	1580.32	123140	$^{ m TL}$	141727
KP_p-3_n-80_ins-9.dat	80	1	19.41	TL	179509	412.02	33408	TL	246265
KP_p-3_n-90_ins-1.dat	90	1	16.13	TL	170877	319.83	23025	TL	201427
$KP_p-3_n-90_ins-10.dat$	90	1	12.91	TL	173383	222.24	16637	TL	207005
KP_p-3_n-90_ins-2.dat	90	1	21.3	TL	132437	1251.44	92403	TL	181599
KP_p-3_n-90_ins-3.dat	90	1	19.67	TL	152219	462.15	36724	TL	180275
KP_p-3_n-90_ins-4.dat	90	1 1	25.68	TL	155947	1225.55	88588	${ m TL}$ ${ m TL}$	199541
KP_p-3_n-90_ins-5.dat KP p-3 n-90 ins-6.dat	90 90	1	15.94 11.48	${ m TL}$	$\begin{array}{c} 219265 \\ 170441 \end{array}$	400.75 167.85	33886 13933	3468.87	426297 510825
KP_p-3_n-90_ins-7.dat	90	1	18.34	TL	157455	778.25	61114	7400.87 TL	190685
KP_p-3_n-90_ins-8.dat	90	1	28.26	TL	127345	1517.83	115516	$^{ m TL}$	147511
KP_p-3_n-90_ins-9.dat	90	1	22.43	TL	144491	554.85	41113	TL	150841
KP_p-4_n-10_ins-1.dat	10	1	3.53	1.76	333	0.08	29	2.66	115
$KP_p-4_n-10_ins-10.dat$	10	1	3.19	1.76	541	0.05	15	2.42	77
KP_p-4_n-10_ins-2.dat	10	1	3.64	1.72	295	0.1	35	2.75	133
KP_p-4_n-10_ins-3.dat	10	1	3.36	1.63	65	0.02	7	2.43	41
KP_p-4_n-10_ins-4.dat	10 10	1 1	3.31	1.6	95	0.06	25 37	2.52	43
KP_p-4_n-10_ins-5.dat KP_p-4_n-10_ins-6.dat	10	1	$3.44 \\ 3.59$	1.77 1.79	451 777	$0.11 \\ 0.07$	37 17	2.94 2.85	213 413
KP p-4 n-10 ins-7.dat	10	1	3.72	1.73	217	0.07	29	$\frac{2.53}{2.52}$	153
KP p-4 n-10 ins-8.dat	10	1	3.22	1.64	123	0.03	13	2.35	69
KP_p-4_n-10_ins-9.dat	10	1	3.4	1.68	143	0.06	17	2.55	149
$KP_p-4_n-20_ins-1.dat$	20	1	3.98	8.43	14793	0.24	45	3.18	481
$KP_p-4_n-20_ins-10.dat$	20	1	4.71	22.13	17801	0.98	194	5.77	2723
KP_p-4_n-20_ins-2.dat	20	1	4.77	16.98	14033	0.97	165	6.42	2749
KP_p-4_n-20_ins-3.dat	20	1	4.2	10.42	11411	0.57	147	3.9	1605
KP_p-4_n-20_ins-4.dat KP p-4 n-20 ins-5.dat	20 20	1 1	3.82 3.98	5.98 17.09	4155 16053	$0.44 \\ 0.49$	73 97	3.43 3.9	597 731
KP p-4 n-20 ins-6.dat	20	1	4.32	9.95	9727	0.49	150	3.9	1159
KP_p-4_n-20_ins-7.dat	20	1	3.89	9.55	10255	0.43	95	3.77	1377
KP_p-4_n-20_ins-8.dat	20	1	4.09	4.69	3755	0.7	149	3.73	1029
$KP_p-4_n-20_ins-9.dat$	20	1	5.03	18.92	11369	2.67	493	4.48	1939
$KP_p-4_n-30_ins-1.dat$	30	1	5.45	131.27	61489	5.22	680	26.58	13027
KP_p-4_n-30_ins-10.dat	30	1	6.38	166.25	105453	6.8	1007	44.5	25559
KP_p-4_n-30_ins-2.dat	30	1	5.47	170.73	150541	2.71	421	20.15	12029
KP_p-4_n-30_ins-3.dat KP p-4 n-30 ins-4.dat	30 30	1 1	$4.45 \\ 4.62$	106.76 68.51	94513 61633	1.64 1.42	$\frac{215}{222}$	10.36 4.75	6261 1745
KP_p-4_n-30_ins-5.dat	30	1	4.33	68.32	65875	1.97	245	8.28	4337
KP_p-4_n-30_ins-6.dat	30	1	4.53	64.53	33927	2.05	307	7.45	2759
KP_p-4_n-30_ins-7.dat	30	1	5.2	126.16	63821	2.65	433	18.64	8391
$KP_p-4_n-30_ins-8.dat$	30	1	4.65	102.67	48187	2.79	350	15.52	6909
KP_p-4_n-30_ins-9.dat	30	1	5.3	70.95	67709	2.97	480	13.38	12153
KP_p-4_n-40_ins-1.dat	40	1	6.61	949.84	372349	12.89	1738	147.77	60357
KP_p-4_n-40_ins-10.dat	40	1	7.12	544.44	209429	12.19	1562	49.23	19617
KP_p-4_n-40_ins-2.dat KP_p-4_n-40_ins-3.dat	40 40	1 1	$6.01 \\ 7.74$	661.3 594.98	372563 399787	5.33 15.12	684 1800	37.77 73.97	18081 53503
KP_p-4_n-40_ins-4.dat	40	1	7.85	707.26	340137	18.68	2340	138.41	71293
KP p-4 n-40 ins-5.dat	40	1	6.95	909.01	394585	19.07	2411	212.9	109923
KP_p-4_n-40_ins-6.dat	40	1	6.65	846.46	358187	15.77	1746	78.95	40455
KP_p-4_n-40_ins-7.dat	40	1	7.44	471.87	153461	11.3	1535	68.7	23941
$KP_p-4_n-40_ins-8.dat$	40	1	6.82	348.17	218913	12.43	1680	33.08	16771
KP_p-4_n-40_ins-9.dat	40	1	8.8	895.95	316889	22.73	2824	198.1	71917
KP_p-5_n-10_ins-1.dat	10	1 1	3.27	1.84	459	0.15	43	2.73 2.44	151
KP_p-5_n-10_ins-10.dat KP_p-5_n-10_ins-2.dat	10 10	1	$3.32 \\ 3.52$	1.64 1.73	101 293	$0.05 \\ 0.12$	19 36	$\frac{2.44}{2.78}$	49 109
KP_p-5_n-10_ins-3.dat	10	1	3.56	1.73	505	0.12	20	2.72	207
KP_p-5_n-10_ins-4.dat	10	1	3.34	1.86	313	0.05	21	2.44	185
KP_p-5_n-10_ins-5.dat	10	1	3.37	1.68	355	0.06	21	2.81	103
KP_p-5_n-10_ins-6.dat	10	1	3.46	1.67	241	0.08	32	2.94	177

$KP_p-5_n-10_ins-7.dat$	10	1	3.36	1.69	165	0.05	19	2.47	87
$KP_p-5_n-10_ins-8.dat$	10	1	3.4	1.74	321	0.11	28	2.38	133
$KP_p-5_n-10_ins-9.dat$	10	1	3.29	1.67	199	0.01	3	0.53	1
$KP_p-5_n-20_ins-1.dat$	20	1	4.47	13.7	28861	0.83	138	4.52	2481
KP_p-5_n-20_ins-10.dat	20	1	4.69	20.0	12211	1.57	297	5.82	2487
$KP_p-5_n-20_ins-2.dat$	20	1	4.25	11.55	7729	0.8	178	4.05	1115
$KP_p-5_n-20_ins-3.dat$	20	1	4.19	13.02	7369	0.98	159	4.59	1535
$KP_p-5_n-20_ins-4.dat$	20	1	3.59	5.5	10611	0.24	59	2.45	379
$KP_p-5_n-20_ins-5.dat$	20	1	3.71	14.16	10741	0.49	97	3.87	915
$KP_p-5_n-20_ins-6.dat$	20	1	3.68	19.18	22119	0.57	104	3.74	1217
KP_p-5_n-20_ins-7.dat	20	1	4.0	6.08	3897	0.61	96	3.86	879
KP_p-5_n-20_ins-8.dat	20	1	4.61	23.46	36303	1.59	261	8.06	7207
$KP_p-5_n-20_ins-9.dat$	20	1	3.88	10.6	11693	0.66	113	4.6	2573