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## Formulae and constants

## **Mathematical constants**

 $\sqrt{2} = 1.414...$ 

 $\sqrt{3} = 1.732...$ 

 $\sqrt{5} = 2.236...$ 

 $\hbox{Eulers constant: } e=2.718...$ 

Golden ratio:  $\varphi_g=1.618...$ 

Pi:  $\pi = 3.141...$ 

## Values of Euler's Gamma function $\Gamma(x)$

(The Gamma function is not the Gamma distribution.)

 $\Gamma(1) = \Gamma(2) = 1$ 

 $\Gamma(3) = 2$ 

 $\Gamma(\pi) = 2.288...$ 

 $\Gamma(1.5) = \sqrt{\pi/2}$ 

 $\Gamma(2.5) = \frac{3}{4}\sqrt{\pi}$ 

## Integrals related to Gaussians

$$\int_{-\infty}^{+\infty} e^{-a(x+b)^2} \mathrm{d}x = \sqrt{\frac{\pi}{a}} \tag{0.1}$$

$$\int e^{-ax^2} dx = \sqrt{\frac{\pi}{4a}} \operatorname{erf}(\sqrt{a}x) \tag{0.2}$$