GRADE 100%

## **Interview Questions: Priority Queues (ungraded)**

1. **Dynamic median.** Design a data type that supports insert in logarithmic time, find-the-median in constant time, and remove-the-median in logarithmic time. If the number of keys in the data type is even, find/remove the lower median. 1 / 1 point

Note: these interview questions are ungraded and purely for your own enrichment. To get a hint, submit a solution.

Dynamic median

Specification:

- 1. insert in logarithmic time
- 2. find-the-median in constant time
- 3. remove-the-median in logarithmic time



Hint: maintain two binary heaps, one that is max-oriented and one that is min-oriented.

2. Randomized priority queue. Describe how to add the methods sample() and delRandom() to our binary heap implementation. The two methods return a key that is chosen uniformly at random among the remaining keys, with the latter method also removing that key. The sample() method should take constant time; the delRandom() method should take logarithmic time. Do not worry about resizing the underlying array.

1 / 1 point

Randomized priority queue:

Specification:

Add two methods to binary heap implementation:

- 1. sample() method, choose uniformly at random among the remaining keys. (constant time)
- 2. delRandom() also removing that key. (logarithmic time)



Hint: use sink() and swim().

3. **Taxicab numbers.** A *taxicab* number is an integer that can be expressed as the sum of two cubes of positive integers in two different ways:  $a^3+b^3=c^3+d^3$ . For example, 1729 is the smallest taxicab number:  $9^3+10^3=1^3+12^3$ . Design an algorithm to find all taxicab numbers with a, b, c, and d less than n.

1 / 1 point

- Version 1: Use time proportional to  $n^2 \log n$  and space proportional to  $n^2$ .
- Version 2: Use time proportional to  $n^2 \log n$  and space proportional to n.

Taxicab numbers:

Design an algorithm to find all taxicab numbers with a, b, c, and d less than n.

V1: Use time proportional to n^2logn and space proportional to n^2.

V2: Use time proportional to n^2logn and space proportional to n.



Hints:

- Version 1: Form the sums  $a^3 + b^3$  and sort.
- $\bullet\,$  Version 2: Use a min-oriented priority queue with n items.