

## Electric Circuits 1 ECSE-200 Section: 1

23 April 2013, 9:00AM

Examiner:

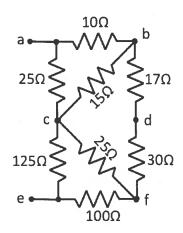
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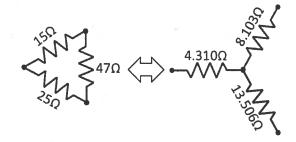
## **INSTRUCTIONS:**

- This is a CLOSED BOOK examination.
- NO CRIB SHEETS are permitted.
- Provide your answers in an EXAM BOOKLET.
- STANDARD CALCULATOR permitted ONLY.
- This examination consists of 4 questions, with a total of 6 pages, including the cover page.
- This examination is PRINTED ON BOTH SIDES of the paper

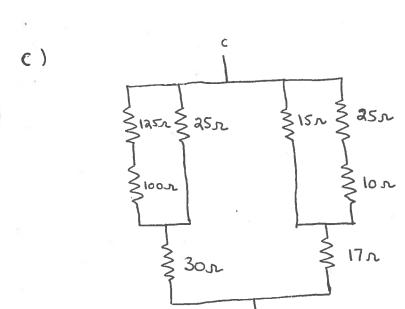
1. Consider the circuit below. Answer the questions. [12 pts]



- a) What is the definition of a passive element? [1pt]
- b) What is the definition of a linear element? [1pt]
- c) What is the equivalent resistance between terminals c and d? [3pts]
- d) What is the equivalent resistance between terminals a and b ? [3pts]
- e) What is the equivalent resistance between terminals a and e ? [4pts] **HINT:** You may find it useful to use the  $\Delta$ -to-Y transformation below.



- as An element that cannot deliver more energy to a circuit than it has received. [41]
- b) An element where terminal voltage and current are related by a linear function or linear operator. CHI



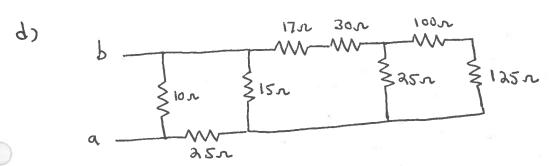
$$R_{cd} = (30x + 225x/125x)$$

$$// (17x + 35x//15x)$$

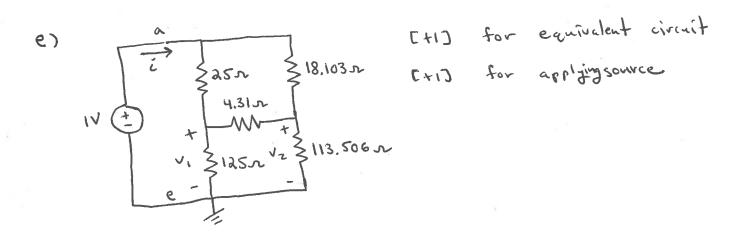
$$(+2)$$

$$= 52.5x/127.5x$$

= 18.05 sc C+13



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$$O = \frac{V_1}{145} + \frac{V_1 - V_2}{4.31} + \frac{V_1 - 1}{25}$$

$$O = \frac{V_2}{113.506} + \frac{V_2 - V_1}{4.31} + \frac{V_2 - 1}{18.103}$$

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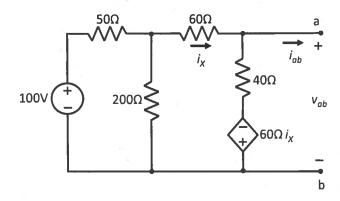
$$V_{1} = \frac{\begin{vmatrix} 0.04 & -0.332 \\ 0.05524 & 0.2461 \end{vmatrix}}{\begin{vmatrix} 0.2800 & -0.232 \\ -0.232 & 0.2461 \end{vmatrix}} = 0.848 \text{ V}$$

$$V_{a} = \frac{\begin{vmatrix} 0.2800 & 0.04 \\ -0.232 & 0.05524 \end{vmatrix}}{\begin{vmatrix} 0.2800 & -0.232 \\ -0.232 & 0.2961 \end{vmatrix}} = 0.851 V$$

$$\dot{c} = \frac{V_1}{1250} + \frac{V_2}{113.5060} = 14.28 \text{ mA}$$

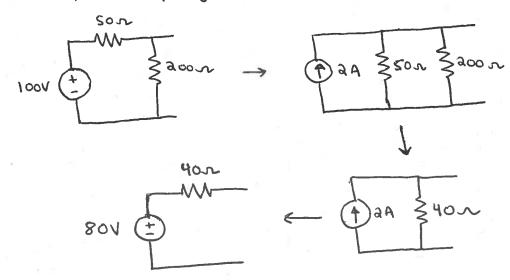
$$R_{ae} = \frac{1V}{i} = 70.0 \text{ s. C+1]}$$
 $C+13$ 

2. Consider the circuit below. Answer the questions. [12 pts]

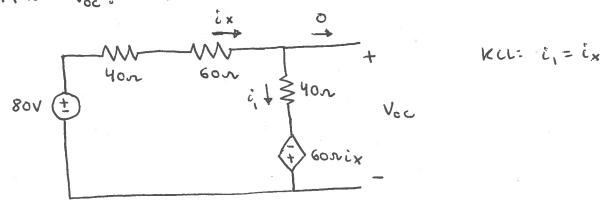


- a) What is Thévenin's theorem? [1pt]
- b) Draw the Thévenin equivalent circuit with respect to terminals a and b. Be sure to label the terminals a and b in your diagram. [6pts]
- c) What is the maximum power that can be delivered to an optimally chosen load resistor attached to the terminals a and b? [2pts]
- d) A load resistor R is attached to the terminals a and b. What are the two values of R that will cause a power of 1.5W to be absorbed by R? [3pts]
- a) Any circuit composed of ideal resistors, dependent sources and independent sources is equivalent to a Thévenin circuit (voltage source in series with a resistor). C+17

b) First simplify circuit:

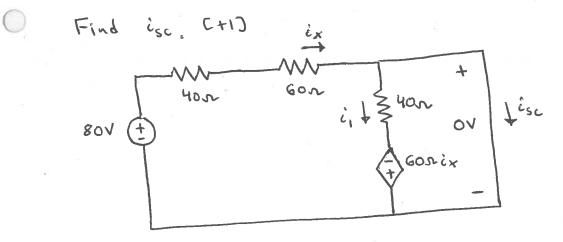


Find Voc . [+1]



KVL: 
$$0 = -80V + 40\pi i_X + 60\pi i_X + 40\pi i_X - 60\pi i_X$$
  
 $i_X = 1A$ 

$$V_{oc} = -20\pi i_x = -200$$
 C+13

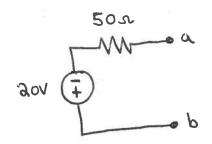


KVL: 
$$0 = -80V + 40x i_x + 60x i_x$$
  
 $i_x = \frac{80V}{100x} = 0.8A$ 

$$i_1 = \frac{60x \cdot i_X - 40x i_1}{40x} = 1.2A$$

$$R_{T} = \frac{V_{OC}}{i_{SC}} = 50 \text{ n}$$

$$E+17$$



Ctilfor diagram

() 
$$P_{\text{max}} = \frac{V_{\text{oc}}}{a} \cdot \frac{\dot{u}_{\text{sc}}}{a}$$
 [+1]
$$= aW \text{ [+1]}$$

d)
$$R = \frac{1}{200} \cdot R$$

$$1.5W = \left(\frac{200}{R+500}\right)^{3} \cdot R$$

$$[+1]$$

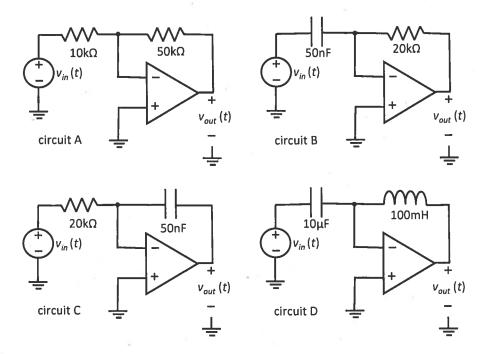
$$1.5(R+S0)^{a} = 400R$$
  
 $1.5R^{a} + 150R + 3750 = 400R$ 

$$R = \frac{250 \pm \sqrt{250^{9} - 4.1.5.3750}}{2.1.5}$$

$$= 150 \text{ and } 16.67 \text{ s}$$

$$[+1]$$

3. Consider the circuit below. Assume ideal op-amp behaviour. Answer the questions. [12 pts]



- a) Give one reason why negative feedback is used in op-amp circuits. [2pts]
- b) How does the output voltage  $v_{out}(t)$  depend upon the input voltage  $v_{in}(t)$  for circuit A? [2pts]
- c) How does the output voltage  $v_{out}(t)$  depend upon the input voltage  $v_{in}(t)$  for circuit B? [2pts]
- d) How does the output voltage  $v_{out}(t)$  depend upon the input voltage  $v_{in}(t)$  for circuit C? Assume that the capacitor stores zero energy at t = 0s, and consider only  $t \ge 0$ . [2pts]
- e) How does the output voltage  $v_{out}(t)$  depend upon the input voltage  $v_{in}(t)$  for circuit D? [2pts]
- f) Voltage sources of +10V and -10V are used to power the op-amp circuit A. What is the range of input voltages that can be used without causing the op-amp to saturate? [2pts]

$$0 = \frac{0 - v_{in}}{10hn} + \frac{0 - v_{out}}{50hn}$$
 (+1)

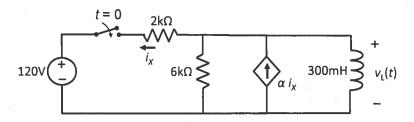
C) 
$$O = 50nF \frac{d}{dt} (0 - v_{in}) + \frac{0 - v_{out}}{20hn} C+1)$$

d) 
$$O = \frac{O - vin}{20hx} + 50nF \frac{d}{dt} (O - vont)$$
 C+1)

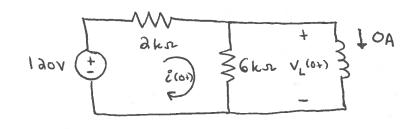
e) 
$$0 = 10 \, \text{MF} \cdot \frac{d}{dt} (0 - v_{in}) + \frac{1}{100 \, \text{mH}} \int_{0}^{t} (0 - v_{out}) \, dt'$$
 (+1)

$$V_{out} = -(lms)^2 - \frac{d^2v_{in}}{dt^2}$$
 [+1]

4. Consider the circuit below (useful for firing sparks). The switch is open for t < 0s, and closes instantaneously at t = 0s. Assume dc steady state behaviour for t < 0. Answer the questions. [12 pts]

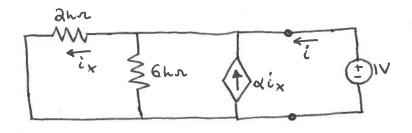


- a) What is the definition of a passive element? [1pt]
- b) Assume that  $\alpha = 0$ . What is the voltage  $v_L(t)$  for t > 0? Plot your solution for  $v_L(t)$  versus t. [6pts]
- c) What is the value of  $\alpha$  that causes the Thévenin resistance with respect to the inductor terminals to become  $-3k\Omega$  for t > 0? [2pts]
- d) For the value of  $\alpha$  found in part c), at what time t will  $v_L(t) = 36kV$ ? [3pts]
- a) An element that cannot deliver more energy to a circuit than it has received. C+1]
- b) Assume a=0.



$$V_{L}(t) = V_{L}(a) + (V_{L}(0+) - V_{L}(a)) \exp(-t/2)$$
 (+1)
$$= 90V \exp(-t/200\mu s)$$
 (+1)

c) Find Rth in terms of a:



$$i_x = \frac{1V}{ahr} = 0.5 \text{ mA}$$

$$\hat{L} = IV \cdot \left( \frac{1}{aur} + \frac{1}{6ur} - \frac{\alpha}{aur} \right)$$

$$R_{th} = \frac{IV}{i} = -3kn$$
 C+13 (or  $R_{th} = \frac{V_{cc}}{isc} = -3kn$  C+13)

$$\frac{1}{1} \frac{1}{\sqrt{\frac{1}{ahn} + \frac{1}{6hn} - \frac{\alpha}{ahn}}} = -3hn$$

d) 
$$t = 0 +$$

$$\frac{1}{i} \times \begin{cases} 6 \ln & \frac{1}{i} \times \frac{1}{i} \end{cases} \downarrow 0$$

$$O = \frac{V_L(0+) - 120V}{2kn} + \frac{V_L(0+)}{6kn} = 2 \cdot \left(\frac{V_L(0+) - 120V}{2kn}\right) + 0$$

t -> 00 de steady state would be reached, V\_(a) = 0 V

$$rac{L}{R_{th}} = \frac{300 \, \text{mH}}{-3 \, \text{hr}} = -100 \, \text{ms}$$

$$V_{L}(t) = V_{L}(\Delta) + (V_{L}(0+) - V_{L}(\Delta)) \exp(-t/2)$$
  
= 180V exp(t/100 ms) C+1]

$$36 \text{ kV} = 180 \text{V} \exp (t/100 \text{ ms})$$
  
 $t = 100 \text{ ms} \cdot \ln \left(\frac{36000}{180}\right)$   
 $= 530 \text{ ms} \quad (+1)$