### # 1.Flowchart

```
In [33]: #定义函数
          def Print_values():
              a = float(input('Enter number a:'))
              b = float(input('Enter number b:'))
              c = float(input('Enter number c:'))
              if a>b:
                  if b>c:
                      print(a, b, c)
                  else:
                      if a>c:
                          print (a, c, b)
                      else:
                          print(c, a, b)
              else:
                  if b>c:
                      if a>c:
                          print(a, c, b)
                      else:
                          print(c, a, b)
                  else:
                      print(c, b, a)
          Print_values()
```

```
Enter number a:9
Enter number b:45
Enter number c:11
11.0 9.0 45.0
```

## # 2.Matrix multiplication

```
In [247]: # 2.1 创建矩阵M1、M2
           import random
                       #定义矩阵M1、M2行列数
           r1 = 5
           c1 = 10
           r2 = 10
           c2 = 5
           M1 = [[0 \text{ for } j \text{ in } range(c1)]] \text{ for } i \text{ in } range(r1)]
                                                                 #创建空的二维list作为矩阵M1、M2
           M2 = [[0 \text{ for } j \text{ in } range(c2)] \text{ for } i \text{ in } range(r2)]
           for i in range(r1):
               for j in range(c1):
                   M1[i][j] = random. randint(0, 50)
           for j in range (r2):
              for k in range(c2):
                   M2[j][k] = random. randint(0, 50)
           print(M1)
           print (M2)
           # 2.2 矩阵乘法运算
           def Matrix multip(M1, M2):
                                                                #定义矩阵乘法函数
               result = [[0] * len(M2[0]) for in range(r1)] #矩阵result行数为M1的行数,列数为M2的列数
               for i in range(len(M1)):
                                                                #按行遍历M1矩阵
                   for j in range (1en(M2[0])):
                                                                #按列遍历M2矩阵
                       for k in range (len(M2)):
                                                                #按行遍历M2矩阵
                           result[i][j] += M1[i][k] * M2[k][j]
               return result
           print (result)
                                                               #打印矩阵乘法结果
```

[[42, 42, 50, 20, 43, 26, 9, 12, 22, 42], [34, 50, 50, 29, 2, 40, 17, 48, 33, 41], [14, 4, 16, 19, 4, 34, 39, 19, 29, 24], [30, 27, 30, 22, 28, 32, 0, 29, 14, 6], [23, 33, 23, 14, 0, 42, 46, 35, 39, 12]]
[[42, 22, 24, 2, 4], [21, 0, 50, 40, 2], [36, 41, 16, 9, 18], [30, 42, 12, 11, 13], [23, 34, 3, 46, 11], [5, 38, 33, 28, 24], [44, 17, 36, 1, 39], [8, 36, 0, 10, 23], [2, 2, 41, 37, 35], [47, 40, 25, 33, 46]]
[[4044, 5612, 4729, 2577, 4679], [6640, 5375, 6093, 5052, 7017], [5558, 5091, 4351, 4439, 6158], [4796, 6323, 5761, 3241, 5222], [4584, 3394, 5596, 3304, 4966]]

### #3 Pascal triangle

```
[333]: def Pascal triangle(n):
                                                                                                                        #定义帕斯卡函数,参数n为行数
                            result = []
                            for i in range(n):
                                     k = \lceil 1 \rceil
                                     if i > 0:
                                               for i in range(1, i):
                                                         new k = k[j-1] + result[i-1][j] # 当前行各元素等于上一行对应位置元素之和
                                                         k. append (new k)
                                               k. append (1)
                                     result.append(k)
                            return result
                   n1 = 100
                   n2 = 200
                  for r in Pascal triangle(n1): #打印前100行、前200行帕斯卡三角
                            print(r)
                  print("\n-
                   for r in Pascal triangle(n2):
                            print(r)
                   [1]
                   [1, 1]
                   [1, 2, 1]
                  [1, 3, 4, 1]
                  [1, 4, 8, 9, 1]
                  [1, 5, 13, 22, 23, 1]
                   [1, 6, 19, 41, 64, 65, 1]
                   [1, 7, 26, 67, 131, 196, 197, 1]
                  [1, 8, 34, 101, 232, 428, 625, 626, 1]
                   [1, 9, 43, 144, 376, 804, 1429, 2055, 2056, 1]
                  [1, 10, 53, 197, 573, 1377, 2806, 4861, 6917, 6918, 1]
                   [1, 11, 64, 261, 834, 2211, 5017, 9878, 16795, 23713, 23714, 1]
                   [1, 12, 76, 337, 1171, 3382, 8399, 18277, 35072, 58785, 82499, 82500, 1]
                  [1, 13, 89, 426, 1597, 4979, 13378, 31655, 66727, 125512, 208011, 290511, 290512, 1]
                   [1, 14, 103, 529, 2126, 7105, 20483, 52138, 118865, 244377, 452388, 742899, 1033411, 1033412, 1]
                  [1, 15, 118, 647, 2773, 9878, 30361, 82499, 201364, 445741, 898129, 1641028, 2674439, 3707851, 3707852, 1]
                   [1, 16, 134, 781, 3554, 13432, 43793, 126292, 327656, 773397, 1671526, 3312554, 5986993, 9694844, 13402696, 13402697, 1]
                  [1, 17, 151, 932, 4486, 17918, 61711, 188003, 515659, 1289056, 2960582, 6273136, 12260129, 21954973, 35357669, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 4876036, 48760366, 4876036, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 48760366, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 4876066, 48760666, 48760666, 48760666, 48760666, 48760666, 48760666, 487606666, 487606666, 487606666, 48760666666, 48760666666, 48760666666, 487606666666, 4876066666666666, 48760666666666666666666666666666
                   0367, 1
```

#### # 4 Add or double

In [362]: 1 import random  $2 \mid x = \text{random. randint}(1, 100)$ 3 def Least moves(x): #定义函数 if x == 1: #x==1时,返回0,表示0次即获得1元 5 return 0 else: #初始化次数tt tt = 0while x > 1: if x % 2 == 0: 9 #若x为偶数,则将x除以2(即钱数double) 10 x = x // 211 else: #若x为奇数,则将x减去1(即钱数增加1元) 12  $\mathbf{x} = 1$ 13 tt += 114 return tt 15 16 #Least moves(x) 17 print(x) #打印随机整数x 18 print(Least\_moves(x)) #打印计算所需最小次数

15 6

# # 5 Dynamic programming

```
In [690]: #5.1
         import random
         #定义函数,参数为数字串、目标为1到100随机整数、当前表达式和当前结果
         def Find expression(str nums, target, exp="", result=0):
                                   #若数字串为空,说明已经遍历完所有数字
            if not str nums:
                if result == target: #若当前结果等于目标整数,就打印出表达式
                   print(str(exp) + "=" + str(target))
                                   #找到1个对应结果的表达式
                   return 1
                else:
                                   #未找到对应结果的表达式
                   return 0
                                   #do nothing
                   pass
            else:
                count = 0
                for i in range(1, len(str nums) + 1): #遍历数字串中每个数字
                   num = int(str nums[ :i])
                                                 #提取当前已遍历的数字串
                                         #若为第一个数,则直接加入表达式和结果中,再递归剩余数字
                   if not exp:
                      count += Find expression(str nums[i: ], target, str(num), num)
                   else: # 否则进行加法或减法
                      count += Find expression(str nums[i:], target, exp + "+" + str(num), result + num) #插入加号, 更新表达式和结果
                      count += Find expression(str nums[i:], target, exp + "-" + str(num), result - num) #插入减号,更新表达式和结果;
                return count
         rr = random. randint(1, 101)
         Find expression("123456789", rr)
         print("结果等于"+ str(rr)+"的表达式有"+ str(count)+"个")
         1+2+34-5+67-89=10
         1-2+34-5+6-7-8-9=10
         1-2-34-5+67-8-9=10
         12+3+4+5-6-7+8-9=10
         12+3+4-5+6+7-8-9=10
```

12+3-4-5-6-7+8+9=10 12+3+45-67+8+9=10 12-3+4-5-6+7-8+9=10 12-3-4+5+6-7-8+9=10 12-3-4+5-6+7+8-9=10 12-34+56-7-8-9=10 123-45-67+8-9=10

结果等于10的表达式有26个

```
In [691]: #5. 2
         #5.1
         import random
         import matplotlib.pyplot as plt
         #定义函数,参数为数字串、目标为1到100随机整数、当前表达式和当前结果
         def Find_expression(str_nums, target, exp="", result=0):
                                  #若数字串为空,说明已经遍历完所有数字
            if not str nums:
               if result == target: #若当前结果等于目标整数,就打印出表达式
                  print(str(exp) + "=" + str(target))
                                   #找到1个对应结果的表达式
                   return 1
               else:
                  return 0 #未找到对应结果的表达式
                                   #do nothing
                   pass
            else:
                count = 0
               for i in range(1, len(str nums) + 1): #遍历数字串中每个数字
                                                #提取当前已遍历的数字串
                  num = int(str nums[ :i])
                                        #若为第一个数,则直接加入表达式和结果中,再递归剩余数字
                   if not exp:
                      count += Find_expression(str nums[i: ], target, str(num), num)
                   else: # 否则进行加法或减法
                      count += Find expression(str nums[i:], target, exp + "+" + str(num), result + num) #插入加号,更新表达式和结果;
                      count += Find expression(str nums[i:], target, exp + "-" + str(num), result - num) #插入减号, 更新表达式和结果
                return count
         rr = random. randint(1.101)
         Find expression ("123456789", rr)
         print("结果为"+ str(rr)+"的表达式有"+ str(count)+"个")
         #5.2
         counts = np. zeros((100))
         for i in range (100):
            counts[i] = Find expression("123456789", i)
            print("结果为"+ str(i)+"的表达式有"+ str(count)+"个")
            # Append the number of solutions to the list
         # counts.append(str(count))
         print(counts)
         import numpy as np
         print(np. where (counts==max(counts))) #打印最大个数表达式
         print(np. where (counts==min(counts))) #打印最小个数表达式
```

```
plt.plot(range(1, 101), counts) # 用matplotlib库来绘制列表,横轴是整数,纵轴是解的数量
plt.title("counts of the expression") #添加标题和坐标轴标签
plt. xlabel ("Integer")
plt.ylabel("counts of solutions")
plt.show()
1-2+34-56+78-9=46
1-2-34+5-6-7+89=46
1+23-4-56-7+89=46
1-23+4+56+7-8+9=46
12+3+4+5-67+89=46
12+3-4+5+6+7+8+9=46
12+3+45-6-7+8-9=46
12+3-45-6-7+89=46
12-34+5-6+78-9=46
123+4-5+6+7-89=46
123-4-5-67+8-9=46
结果为46的表达式有26个
1+2+3-4-5+67-8-9=47
1+2+3+45+6+7-8-9=47
1+2-3+45-6+7-8+9=47
1-2+3+45+6-7-8+9=47
1-2+3+45-6+7+8-9=47
1-2+3-45-6+7+89=47
1-2-3-4+5+67-8-9=47
```

In [ ]: