

test1

## APPENDIX A

The intermediate parameters in (??), (??), (??), (??) and (??) are given by:

$$\begin{aligned}\theta_1 &= \arccos\left(\frac{d^2 + r^2 - r_i^2}{2dr}\right), \theta_2 = \arccos\left(\frac{r^2 + r_i^2 - d^2}{2rR_I}\right), \\ \theta_3 &= \arccos\left(\frac{d}{2r_i}\right), \theta_4 = \arccos\left(\frac{r^2 + r_i^2 - r_{cs}^2}{2rr_i}\right), \\ \theta_5 &= \arccos\left(\frac{2r_i^2 - d^2}{2r_i^2}\right), \theta_6 = \arccos\left(\frac{r}{2r_i}\right), \\ \varphi_1 &= \arccos\left(\frac{\delta_2^2 + d^2 - r_i^2}{2\delta_2 d}\right), \varphi_2 = \arccos\left(\frac{\delta_2^2 + \delta_3^2 - d^2}{2\delta_2 \delta_3}\right), \\ \varphi_3 &= \arccos\left(\frac{\delta_3^2 + d^2 - r_i^2}{2\delta_3 d}\right), \\ \delta_1 &= \sqrt{r_{cs}^2 - \frac{d^2}{4}} - \sqrt{r_i^2 - \frac{d^2}{4}}, \\ \delta_2 &= \sqrt{r^2 + r_i^2 + 2rr_i \cos(\theta - \theta_3)}, \\ \delta_3 &= \sqrt{r^2 + r_i^2 - 2rr_i \cos(\theta + \theta_3)}.\end{aligned}$$

## APPENDIX B

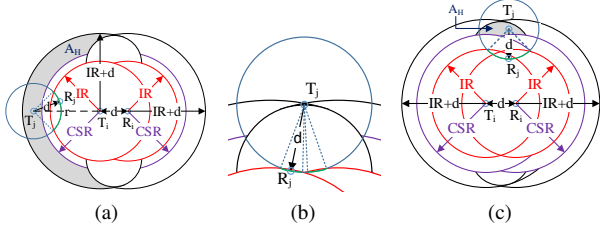


Fig. 1: (a) Geometry of  $V_{HN1}$ , (b) the small overlap HN region, and (c) geometry of  $V_{HN2}$ .

The calculation of  $V_{HN}$  can be divided into two situations, which are corresponding to the expressions (??) and (??), respectively.

*Situation 1:* In Fig. 1 (a),  $T_j$  is randomly distributed in the left-hand side HN region. If  $T_j$  is a hidden node,  $R_j$  will be located within the interference range of  $T_i$ . According to the symmetry principle, we can easily find that the right-hand side HN region is the same as the left-hand side HN region. But there is a small overlap HN region as shown in Fig. 1 (b).

The small overlap HN region requires special consideration, because  $R_j$  could not only fall in the interference region of  $T_i$ , but also the interference region of  $R_i$ . Since the location that  $R_j$  is within the bicircle interference region is discontinuous, we only consider  $R_j$  is located within the interference region of  $T_i$  in the left-hand side and similarly assume  $R_j$  is located within the interference region of  $R_i$  in the right-hand side.

*Situation 2:* In Fig. 1 (c),  $T_j$  is randomly located in the upper side HN region. If  $T_j$  is a hidden node,  $R_j$  is interfered by both  $T_i$  and  $R_i$ , and the location where  $R_j$  may be within the bicircle interference region is continuous. According to

symmetry, the lower side HN region is similar to the upper side HN region.

## APPENDIX C

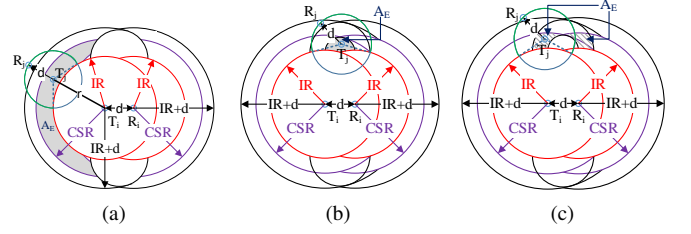


Fig. 2: (a) Geometry of  $V_{EN1}$ , (b) geometry of  $V_{EN2}$ , and (c) geometry  $V_{EN3}$ .

The calculation of  $V_{EN}$  can be divided into three situations, which are corresponding to the expressions (??), (??) and (??), respectively.

*Situation 1:* In Fig. 2 (a),  $T_j$  is located in the left-hand side EN region where  $T_j$  may be an exposed node if  $R_j$  is outside the bicircle interference region. Symmetrically, the right-hand side EN region the same as the left-hand side EN region.

*Situation 2:* In Fig. 2 (b),  $T_j$  is inside the circle with the upper intersection of the two interference circles as the center and  $\delta_3$  as the radius. Symmetrically, there is a region at the bottom that is the same as  $V_{EN2}$ .

*Situation 3:* In Fig. 2 (c), There is a discontinuous symmetric region that the EN problem may exist. In this case, we can only calculate the half part because the other half can be obtained by symmetry. Besides, the corresponding lower region is similar to  $V_{EN3}$ .