Homework 2

Please submit both an .ipynb version and an .html version (for easier visualization on Canvas)

```
In [1]: # Make sure you are running on Colab
        if 'google.colab' in str(get_ipython()):
            print('Running on CoLab')
            !pip install yellowbrick
            !pip install gower
            !pip install scikit-learn-extra
            !pip install kmodes
In [2]: import numpy as np # linear algebra
        import pandas as pd # data processing, CSV file I/O (e.g. pd.read_csv)
        import matplotlib.pyplot as plt # for data visualization
        import seaborn as sns # for statistical data visualization
        from sklearn.decomposition import PCA
        from sklearn.preprocessing import MinMaxScaler,StandardScaler
        import plotly.express as px
        # %matplotlib inline
        import warnings
        warnings.filterwarnings('ignore') # Ignore warnings
```

PCA and Clustering

Delta Airlines' website have data on all of their aircraft in a certain site section. In this homework, we will investigate the different aircraft in Delta's fleet. Which planes are similar? Which are dissimilar?

```
In [3]: # We begin by loading inspecting the data
    delta_data = pd.read_csv('delta.csv', index_col=0).reset_index()
In [4]: delta_data.head()
```

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	Aircraft	Seat Width (Club)	Seat Pitch (Club)	Seat (Club)	Seat Width (First Class)	Seat Pitch (First Class)	Seats (First Class)	Seat Width (Business)	Seat Pitch (Business)	Seats (Business)	•
0	Airbus A319	0.0	0	0	21.0	36.0	12	0.0	0.0	0	
1	Airbus A319 VIP	19.4	44	12	19.4	40.0	28	21.0	59.0	14	
2	Airbus A320	0.0	0	0	21.0	36.0	12	0.0	0.0	0	
3	Airbus A320 32-R	0.0	0	0	21.0	36.0	12	0.0	0.0	0	
4	Airbus A330- 200	0.0	0	0	0.0	0.0	0	21.0	60.0	32	

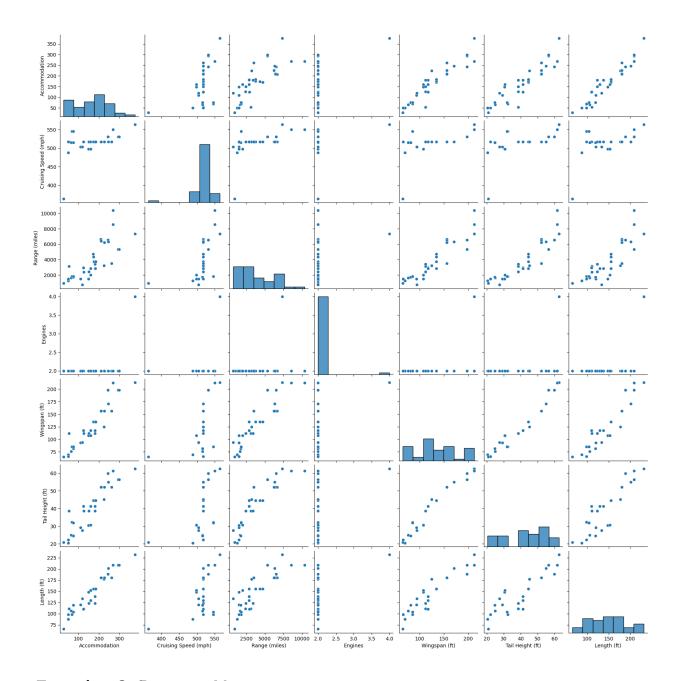
5 rows × 34 columns

Exercise 1: check correlation with visualization

```
(1 point) Visualize pairwise correlation using scatterplot for columns 'Accommodation',
'Cruising Speed (mph)', 'Range (miles)', 'Engines', 'Wingspan (ft)',
'Tail Height (ft)', 'Length (ft)' (i.e., columns 16-23 in delta_data)
```

```
In [5]: comp_df = pd.DataFrame(delta_data,columns=['Accommodation', 'Cruising Speed (mg
sns.pairplot(comp_df)
```

Out[5]: <seaborn.axisgrid.PairGrid at 0x13870d960>



Exercise 2: Prepare X

(1 point) Identify all binary columns (i.e., a binary column is the column that only contains0 and 1 as values)

(1 point) Generate a dataframe X removing these binary columns and column Aircraft (since this is the y)

```
In [6]: binary_columns = []
    for column in delta_data.columns:
        unique_values = delta_data[column].unique()
        if len(unique_values) == 2 and 0 in unique_values and 1 in unique_values:
            binary_columns.append(column)

    print(binary_columns)

['Wifi', 'Video', 'Power', 'Satellite', 'Flat-bed', 'Sleeper', 'Club', 'First Class', 'Business', 'Eco Comfort', 'Economy']
```

Out[8]:

	Seat Width (Club)	Seat Pitch (Club)	Seat (Club)	Seat Width (First Class)	Seat Pitch (First Class)	Seats (First Class)	Seat Width (Business)	Seat Pitch (Business)	Seats (Business)	Seat Width (Eco Comfort)
0	0.0	0	0	21.0	36.0	12	0.0	0.00	0	17.20
1	19.4	44	12	19.4	40.0	28	21.0	59.00	14	0.00
2	0.0	0	0	21.0	36.0	12	0.0	0.00	0	17.20
3	0.0	0	0	21.0	36.0	12	0.0	0.00	0	17.20
4	0.0	0	0	0.0	0.0	0	21.0	60.00	32	18.00
5	0.0	0	0	0.0	0.0	0	21.0	80.00	34	18.00
6	0.0	0	0	0.0	0.0	0	21.0	80.00	34	18.00
7	0.0	0	0	0.0	0.0	0	20.0	60.00	34	18.00
8	0.0	0	0	19.6	37.0	12	0.0	0.00	0	18.10
9	0.0	0	0	21.0	37.0	12	0.0	0.00	0	17.20
10	0.0	0	0	21.0	37.0	16	0.0	0.00	0	17.20
11	0.0	0	0	21.0	38.0	16	0.0	0.00	0	17.20
12	0.0	0	0	21.0	37.0	20	0.0	0.00	0	17.20
13	0.0	0	0	0.0	0.0	0	20.5	82.00	48	17.20
14	0.0	0	0	21.0	40.0	24	0.0	0.00	0	17.20
15	0.0	0	0	0.0	0.0	0	21.0	54.50	16	17.20
16	0.0	0	0	21.0	37.0	22	0.0	0.00	0	17.20
17	0.0	0	0	21.0	37.0	22	0.0	0.00	0	17.20
18	0.0	0	0	21.0	37.5	24	0.0	0.00	0	17.20
19	0.0	0	0	21.0	45.0	22	0.0	0.00	0	17.20
20	0.0	0	0	0.0	0.0	0	21.0	38.00	26	17.20
21	0.0	0	0	21.0	37.0	24	0.0	0.00	0	17.20
22	0.0	0	0	0.0	0.0	0	18.5	60.00	30	17.90
23	0.0	0	0	0.0	0.0	0	21.0	78.95	36	17.90
24	0.0	0	0	18.5	37.5	30	0.0	0.00	0	17.90
25	0.0	0	0	18.5	37.5	30	0.0	0.00	0	17.90
26	0.0	0	0	0.0	0.0	0	21.0	78.95	36	17.90
27	0.0	0	0	18.5	60.0	36	0.0	0.00	0	17.90
28	0.0	0	0	0.0	0.0	0	21.0	78.95	26	17.90
29	0.0	0	0	0.0	0.0	0	21.0	78.95	26	17.90
30	0.0	0	0	0.0	0.0	0	21.0	78.95	40	17.90
31	0.0	0	0	0.0	0.0	0	21.0	78.00	45	18.50
32	0.0	0	0	0.0	0.0	0	21.0	78.00	45	18.50

	Seat Width (Club)	Seat Pitch (Club)	Seat (Club)	Seat Width (First Class)	Seat Pitch (First Class)	Seats (First Class)	Seat Width (Business)	Seat Pitch (Business)	Seats (Business)	Seat Width (Eco Comfort)
33	0.0	0	0	0.0	0.0	0	0.0	0.00	0	0.00
34	0.0	0	0	0.0	0.0	0	0.0	0.00	0	0.00
35	0.0	0	0	19.6	36.0	9	0.0	0.00	0	17.30
36	0.0	0	0	19.6	37.0	12	0.0	0.00	0	17.30
37	0.0	0	0	0.0	0.0	0	0.0	0.00	0	0.00
38	0.0	0	0	20.0	37.0	9	0.0	0.00	0	18.25
39	0.0	0	0	20.0	37.0	12	0.0	0.00	0	18.25
40	0.0	0	0	0.0	0.0	0	0.0	0.00	0	0.00
41	0.0	0	0	19.6	37.0	16	0.0	0.00	0	18.10
42	0.0	0	0	19.6	37.0	16	0.0	0.00	0	18.10
43	0.0	0	0	19.6	38.0	16	0.0	0.00	0	18.10

44 rows × 22 columns

Exercise 3: PCA

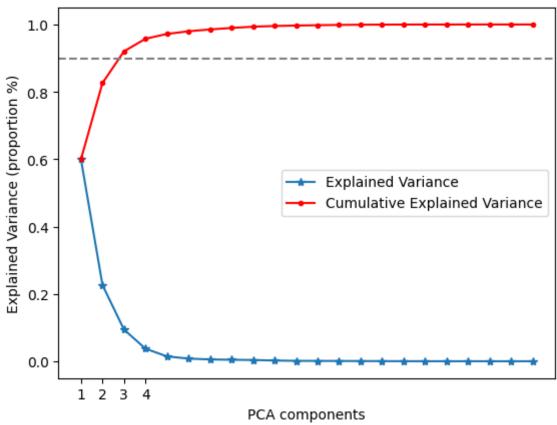
(1 point) Standardize X

(1 point) conduct PCA

(1 point) calculate the amount of varialce each principal component explain, as well as the cumulative sum

(1 point) visualize the cumulative sum of explained variance and set the xticks as the number of components

```
exp_var_cumsum = np.cumsum(exp_var)
         exp_var_cumsum
         array([0.59969059, 0.82614954, 0.92024801, 0.95759235, 0.97197078,
Out[18]:
                0.9798339 , 0.98526776, 0.98967525, 0.99340048, 0.99559481,
                0.99684689, 0.99784246, 0.99871658, 0.99924138, 0.9996311 ,
                0.99981893, 0.99989555, 0.999995505, 0.99999149, 1.
In [19]: #visualize the cumulative sum of explained variance and set the xticks as the
         plt.plot(range(1, len(exp_var)+1),
                 exp_var,'*-',label='Explained Variance')
         plt.plot(range(1, len(exp_var)+1),
                 exp_var_cumsum,'r.-',label='Cumulative Explained Variance')
         plt.legend()
         ax = plt.gca()
         ax.set_xticks([1,2,3,4])
         ax.set_xlabel('PCA components')
         ax.set_ylabel('Explained Variance (proportion %)')
         # which shows that the first two PCs accounts for more than 90% of the variance
         plt.axhline(0.9,linestyle='--',color='grey')
         <matplotlib.lines.Line2D at 0x13e6ddcc0>
Out[19]:
            1.0
```



Exercise 4: Clustering

So, now that we've simplified the complex data set into a lower dimensional space we can visualize and work with, we will use clustering to find patterns in the data, in our case, the aircraft which are most similar?

(1 point) Pick the number of components which explain 90% (or a little greater) of the variation and represent the transformed data (projected onto the selected principal components) as components

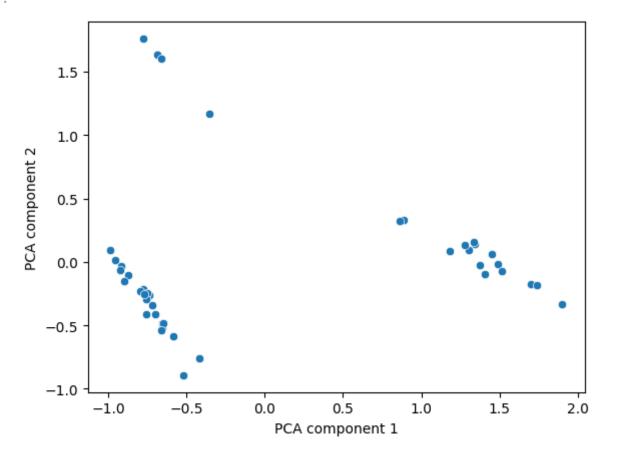
(1 point) Using components as the input, run k-means for k from 2 to 15 (with random_state=1), and visualize SSE by elbow curve.

(1 point) Select the best k using elbow curve and run clustering with the selected k to get the cluster assignment

(Extra credit: 1 point) Visualize the cluster membership by scatter plots (for each pair of principle components as x and y axes)

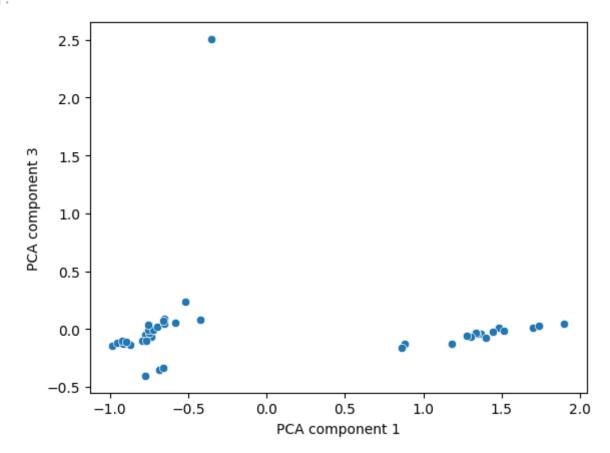
```
In [20]: # Pick the number of components which explain 90% (or a little greater) of the
    pca = PCA(n_components=3)
        components_3 = pca.fit_transform(X_normalized)

In [21]: sns.scatterplot(x = components_3[:,0], y=components_3[:,1])
    plt.xlabel('PCA component 1')
    plt.ylabel('PCA component 2')
Out[21]: Text(0, 0.5, 'PCA component 2')
```



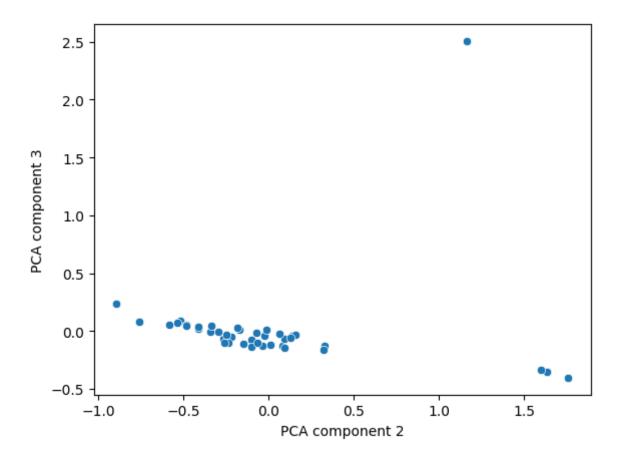
```
In [22]: sns.scatterplot(x = components_3[:,0], y=components_3[:,2])
   plt.xlabel('PCA component 1')
   plt.ylabel('PCA component 3')
```

Out[22]: Text(0, 0.5, 'PCA component 3')



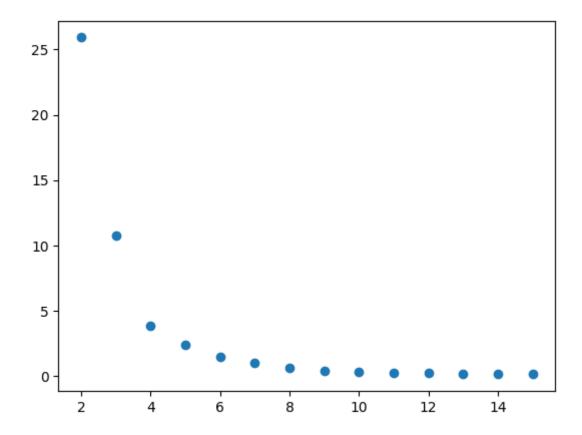
```
In [23]: sns.scatterplot(x = components_3[:,1], y=components_3[:,2])
   plt.xlabel('PCA component 2')
   plt.ylabel('PCA component 3')
```

Out[23]: Text(0, 0.5, 'PCA component 3')

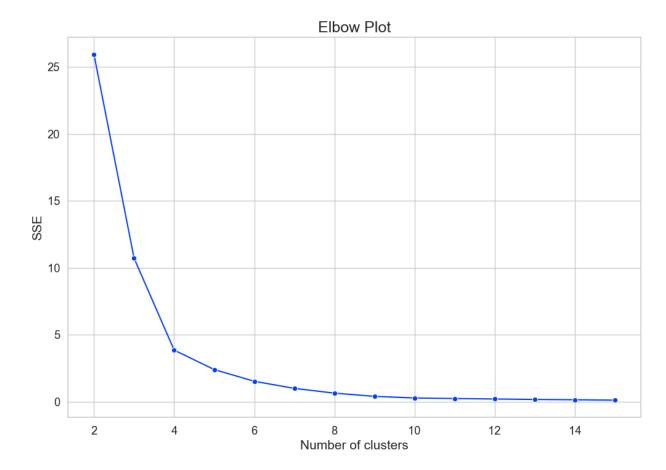


In [24]: #Using components as the input, run k-means for k from 2 to 15 (with random_state)
In [25]: from sklearn.datasets import make_blobs
 from sklearn.cluster import KMeans
 scores = []
 for k in range(2, 16):
 kmeans = KMeans(n_clusters = k)
 # Training the KMeans model on the normalized iris data.
 kmeans.fit(components_3)
 # Appending the negative score of the model to the scores list. The negative scores.append(-kmeans.score(components_3))
Plotting the scores for the range of clusters from 1 to 5.
 plt.scatter(list(range(2, 16)), scores)

Out[25]: <matplotlib.collections.PathCollection at 0x13f742590>



```
In [26]:
         # Function for plotting elbow curve
         def plot_elbow_curve(start, end, data):
             no_of_clusters = list(range(start, end+1))
             cost_values = []
             for k in no_of_clusters:
                 kmeans = KMeans(n_clusters = k, random_state = 1)
                 kmeans.fit_predict(data)
                 cost_values.append(kmeans.inertia_)
             sns.set_theme(style="whitegrid", palette="bright", font_scale=1.2)
             plt.figure(figsize=(12, 8))
             ax = sns.lineplot(x=no_of_clusters, y=cost_values, marker="o", dashes=False
             ax.set_title('Elbow Plot', fontsize=18)
             ax.set xlabel('Number of clusters', fontsize=15)
             ax.set_ylabel('SSE', fontsize=15)
             plt.plot();
         plot_elbow_curve(start=2,end=15,data = components_3)
```



In [27]: #Select the best k using elbow curve and run clustering with the selected k to

Based on the elbow plot, we can see that before cluster = 4, the SSE drops a lot, but after cluster = 4, the SSE drops not too much,

so we choose cluster = 4 as the number of the cluster

```
In [29]: #Visualize the cluster membership by scatter plots (for each pair of principle
In [30]: cluster = kmeans.fit_predict(X)
    X['Cluster'] = cluster
    X.head()
```

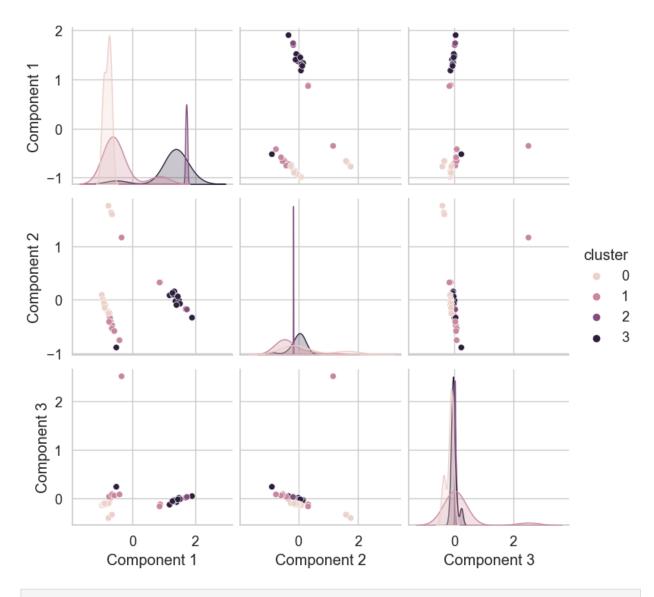
Out[30]:		Seat Width (Club)	Seat Pitch (Club)	Seat (Club)	Seat Width (First Class)	Seat Pitch (First Class)	Seats (First Class)	Seat Width (Business)	Seat Pitch (Business)	Seats (Business)	Seat Width (Eco Comfort)
	0	0.0	0	0	21.0	36.0	12	0.0	0.0	0	17.2
	1	19.4	44	12	19.4	40.0	28	21.0	59.0	14	0.0
	2	0.0	0	0	21.0	36.0	12	0.0	0.0	0	17.2
	3	0.0	0	0	21.0	36.0	12	0.0	0.0	0	17.2
	4	0.0	0	0	0.0	0.0	0	21.0	60.0	32	18.0

5 rows × 23 columns

```
In [38]: X['Cluster'].unique()
Out[38]: array([0, 1, 3, 2], dtype=int32)
In [41]: n_components = 3
   components = pca.fit_transform(X_normalized)[:, :n_components]
In [42]: components
```

```
array([[-0.77466193, -0.21700729, -0.05355604],
Out[42]:
                [-0.35226585, 1.16500076, 2.50730036],
                [-0.73733865, -0.2634676, -0.06844264],
                [-0.73733865, -0.2634676, -0.06844264],
                [1.37047615, -0.02529343, -0.03735896],
                [ 1.48556093, -0.01374743, 0.01117171],
                [1.51617041, -0.07366905, -0.01791195],
                [1.40183588, -0.09829394, -0.07752105],
                [-0.868668 , -0.10111375, -0.1336597 ],
                [-0.74769565, -0.24559031, -0.03609813],
                [-0.75344767, -0.29498722, -0.00991356],
                [-0.7204656, -0.34206006, -0.0046536],
                [-0.69723216, -0.41366629, 0.01945511],
                [1.89965131, -0.33493074, 0.04540639],
                [-0.65290643, -0.51957737, 0.0909585],
                [0.88393359, 0.32712588, -0.1240362],
                [-0.65480761, -0.48044357, 0.05384107],
                [-0.65058242, -0.48190108, 0.04914975],
                [-0.75373969, -0.4109464, 0.03478625],
                [-0.6618634, -0.53679833, 0.07593217],
                [0.86292227, 0.32343072, -0.16534424],
                [-0.58495708, -0.58611543, 0.05862966],
                [1.18108388, 0.08292413, -0.12922966],
                [1.34320516, 0.14019767, -0.04099879],
                [-0.42013889, -0.75781804, 0.07976157],
                [-0.42013889, -0.75781804, 0.07976157],
                [ 1.33255971, 0.15705407, -0.03557833],
                [-0.52110108, -0.89332543, 0.23689738],
                [1.30402865, 0.09416289, -0.06425664],
                [1.27576751, 0.12907932, -0.05643265],
                [1.4471444, 0.06133449, -0.02134079],
                [1.69964438, -0.17381433, 0.01395651],
                [1.73621642, -0.18048987, 0.02911536],
                [-0.68521893, 1.63349135, -0.34940691],
                [-0.68521893, 1.63349135, -0.34940691],
                [-0.98356099, 0.09138576, -0.14223844],
                [-0.95384144, 0.01179537, -0.11491241],
                [-0.77360417, 1.76062425, -0.40421758],
                [-0.91343473, -0.03524607, -0.12917053],
                [-0.91954989, -0.0675653, -0.10520977],
                [-0.65834354, 1.5984617, -0.33481665],
                [-0.79362836, -0.2334027, -0.10538464],
                [-0.76729883, -0.2569345, -0.09900036],
                [-0.89715117, -0.15006853, -0.10758358]])
In [43]:
        labels = {
             str(i): f"PC {i+1} ({var:.1f}%)"
             for i, var in enumerate(pca.explained variance ratio * 100)
         }
         comp df = pd.DataFrame(components,columns=['Component 1','Component 2','Component
         comp df['cluster']=X['Cluster']
         sns.pairplot(comp df,hue='cluster')
```

<seaborn.axisgrid.PairGrid at 0x14b5f29b0> Out[43]:



In [45]: comp_df

	Component 1	Component 2	Component 3	cluster
0	-0.774662	-0.217007	-0.053556	0
1	-0.352266	1.165001	2.507300	1
2	-0.737339	-0.263468	-0.068443	0
3	-0.737339	-0.263468	-0.068443	0
4	1.370476	-0.025293	-0.037359	3
5	1.485561	-0.013747	0.011172	3
6	1.516170	-0.073669	-0.017912	3
7	1.401836	-0.098294	-0.077521	3
8	-0.868668	-0.101114	-0.133660	0
9	-0.747696	-0.245590	-0.036098	1
10	-0.753448	-0.294987	-0.009914	1
11	-0.720466	-0.342060	-0.004654	1
12	-0.697232	-0.413666	0.019455	1
13	1.899651	-0.334931	0.045406	3
14	-0.652906	-0.519577	0.090958	1
15	0.883934	0.327126	-0.124036	1
16	-0.654808	-0.480444	0.053841	1
17	-0.650582	-0.481901	0.049150	1
18	-0.753740	-0.410946	0.034786	1
19	-0.661863	-0.536798	0.075932	1
20	0.862922	0.323431	-0.165344	1
21	-0.584957	-0.586115	0.058630	1
22	1.181084	0.082924	-0.129230	3
23	1.343205	0.140198	-0.040999	3
24	-0.420139	-0.757818	0.079762	1
25	-0.420139	-0.757818	0.079762	1
26	1.332560	0.157054	-0.035578	3
27	-0.521101	-0.893325	0.236897	3
28	1.304029	0.094163	-0.064257	3
29	1.275768	0.129079	-0.056433	3
30	1.447144	0.061334	-0.021341	3
31	1.699644	-0.173814	0.013957	2
32	1.736216	-0.180490	0.029115	2
33	-0.685219	1.633491	-0.349407	0
34	-0.685219	1.633491	-0.349407	0

Out[45]:

	Component 1	Component 2	Component 3	cluster
35	-0.983561	0.091386	-0.142238	0
36	-0.953841	0.011795	-0.114912	0
37	-0.773604	1.760624	-0.404218	0
38	-0.913435	-0.035246	-0.129171	0
39	-0.919550	-0.067565	-0.105210	0
40	-0.658344	1.598462	-0.334817	0
41	-0.793628	-0.233403	-0.105385	0
42	-0.767299	-0.256935	-0.099000	0
43	-0.897151	-0.150069	-0.107584	0