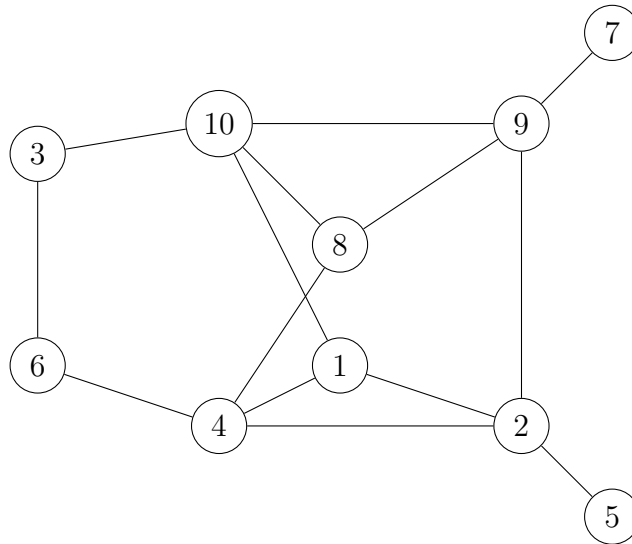


Given the adjacency list representation of graph  $G$  from tutorial. We'll trace through the steps of running DFS on  $G$  starting at node with value 1.

1	2, 4, 10
2	1, 4, 5, 9
3	6, 10
4	1, 2, 6, 8
5	2
6	3, 4
7	9
8	4, 9, 10
9	2, 7, 8, 10
10	1, 3, 8, 9

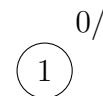


We'll have a stack on the side to help us keep track of edges we need to push/pop. The DFS-tree that starts at 1 will be drawn beside the stack. A node is drawn iff it's discovered (visited for the very first time) and will have an edge pointing toward it from whichever node that led to the discovery, that edge is called a tree-edge.

- Time = 0;  
Stack.push(1, NULL); # push starting node  
Stack.push((1, 2), (1, 4), (1, 10)); # 1's neighbours

(1, 10)
(1, 4)
(1, 2)
(1, NULL)

Stack

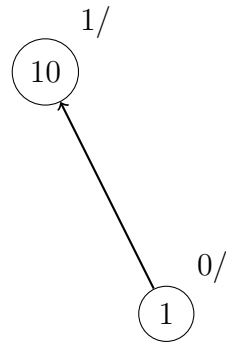


**Note.** We'll jot down the discovery time and finish time beside each node.

2.     Stack.pop(); # pops (1, 10)  
           Time = 1;  
           Stack.push((10, NULL), (10, 1), (10, 3), (10, 8), (10, 9));

(10, 9)
(10, 8)
(10, 3)
(10, 1)
(10, NULL)
<del>(1, 10)</del>
(1, 4)
(1, 2)
(1, NULL)

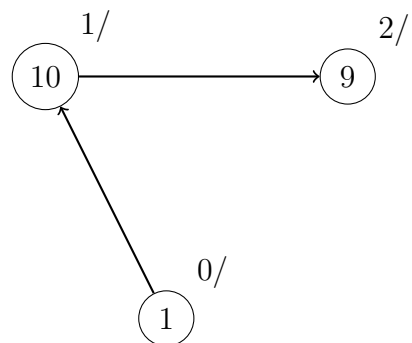
Stack



3.     Stack.pop(); # pops (10, 9)  
           Time = 2;  
           Stack.push((9, NULL), (9, 2), (9, 7), (9, 8), (9, 10))

(9, 10)
(9, 8)
(9, 7)
(9, 2)
(9, NULL)
<del>(10, 9)</del>
(10, 8)
(10, 3)
(10, 1)
(10, NULL)
(1, 4)
(1, 2)
(1, NULL)

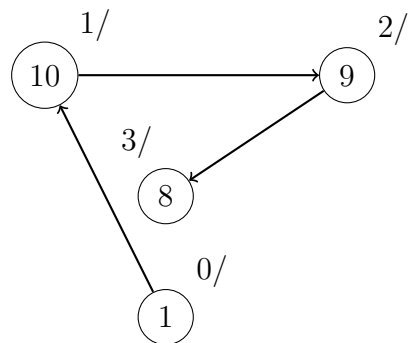
Stack



4.     Stack.pop(); # pops (9, 10)  
               # Since 10 was already discovered, do nothing.  
               # this would be a back-edge in the DFS-tree.  
               # => G has 1 or more cycles.  
    Stack.pop(); # pops (9, 8)  
    Time = 3;  
    Stack.push((8, NULL), (8, 4), (8, 9), (8, 10))

(8, 10)
(8, 9)
(8, 4)
(8, NULL)
<del>(9, 10)</del>
<del>(9, 8)</del>
(9, 7)
(9, 2)
(9, NULL)
(10, 8)
(10, 3)
(10, 1)
(10, NULL)
(1, 4)
(1, 2)
(1, NULL)

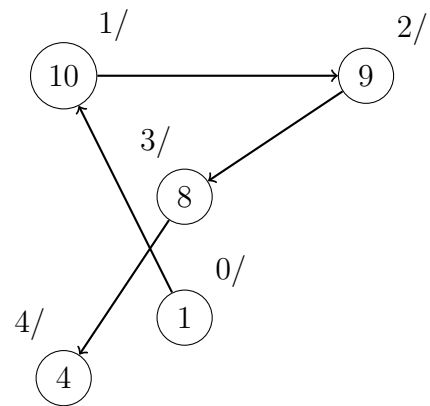
Stack



5.     Stack.pop(); # pops (8, 10), do nothing  
          Stack.pop(); # pops (8, 9), do nothing  
          Stack.pop(); # pops (8, 4)  
          Time = 4;  
          Stack.push((4, NULL), (4, 1), (4, 2), (4, 6), (4, 8))

(4, 8)
(4, 6)
(4, 2)
(4, 1)
(4, NULL)
<del>(8, 10)</del>
<del>(8, 9)</del>
<del>(8, 4)</del>
(8, NULL)
(9, 7)
(9, 2)
(9, NULL)
(10, 8)
(10, 3)
(10, 1)
(10, NULL)
(1, 4)
(1, 2)
(1, NULL)

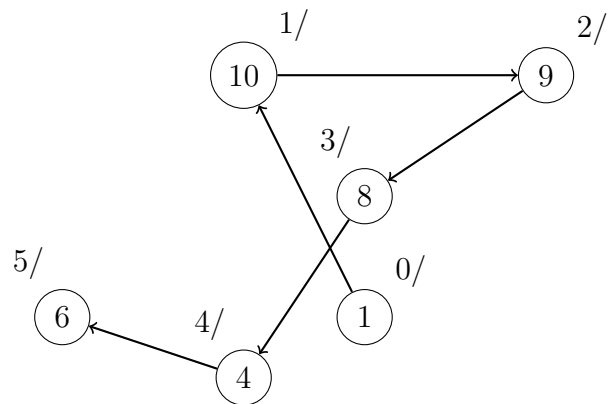
Stack



6.     Stack.pop(); # pops (4, 8), do nothing  
        Stack.pop(); # pops (4, 6)  
        Time = 5;  
        Stack.push((6, NULL), (6, 3), (6, 4))

(6, 4)
(6, 3)
(6, NULL)
<del>(4, 8)</del>
<del>(4, 6)</del>
(4, 2)
(4, 1)
(4, NULL)
(8, NULL)
(9, 7)
(9, 2)
(9, NULL)
(10, 8)
(10, 3)
(10, 1)
(10, NULL)
(1, 4)
(1, 2)
(1, NULL)

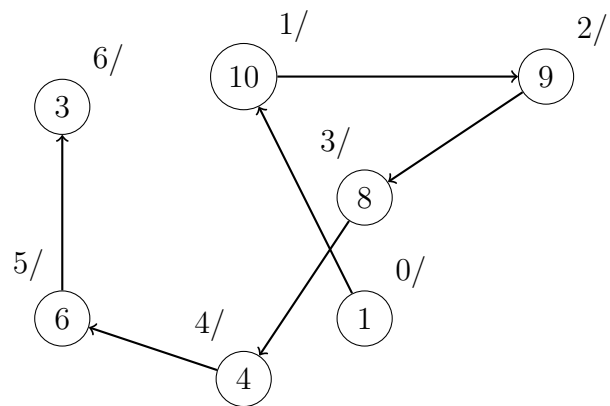
Stack



7.     Stack.pop(); # pops (6,4), do nothing  
        Stack.pop(); # pops (6,3)  
        Time = 6;  
        Stack.push((3, NULL), (3, 6), (3, 10));

(3, 10)
(3, 6)
(3, NULL)
<del>(6, 4)</del>
<del>(6, 3)</del>
(6, NULL)
(4, 2)
(4, 1)
(4, NULL)
(8, NULL)
(9, 7)
(9, 2)
(9, NULL)
(10, 8)
(10, 3)
(10, 1)
(10, NULL)
(1, 4)
(1, 2)
(1, NULL)

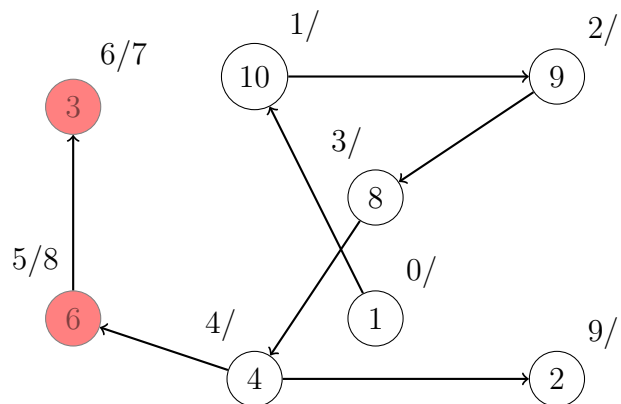
Stack



8.     Stack.pop(); # pops (3, 10), do nothing  
        Stack.pop(); # pops (3, 6), do nothing  
        Stack.pop(); # pops (3, NULL), finished  
        Time = 7;  
        Stack.pop(); # pops (6, NULL), finished  
        Time = 8;  
        Stack.pop(); # pops (4, 2)  
        Time = 9;

<del>(3, 10)</del>
<del>(3, 6)</del>
<del>(3, NULL)</del>
<del>(6, 4)</del>
<del>(6, 3)</del>
<del>(6, NULL)</del>
<del>(4, 2)</del>
(4, 1)
(4, NULL)
(8, NULL)
(9, 7)
(9, 2)
(9, NULL)
(10, 8)
(10, 3)
(10, 1)
(10, NULL)
(1, 4)
(1, 2)
(1, NULL)

Stack

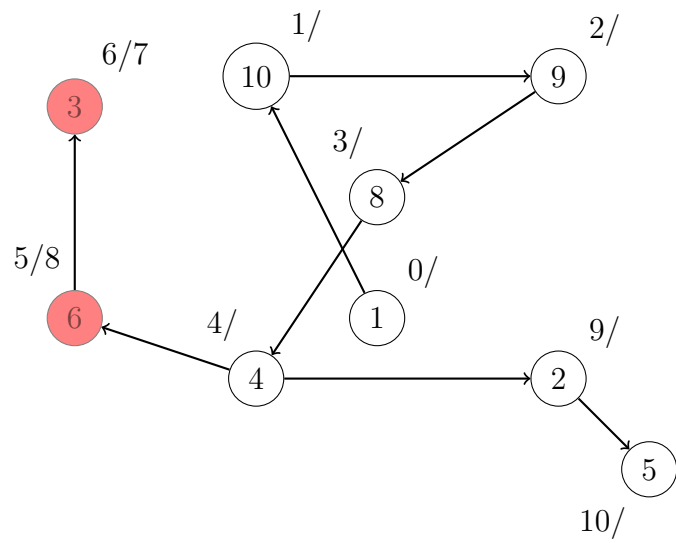


**Note.** We'll indicate a node's finished by colouring it in with red.

9.     Stack.push((2, NULL), (2, 1), (2, 4), (2, 5), (2, 9));  
        Stack.pop(); # pops (2, 9), do nothing  
        Stack.pop(); # pops (2, 5)  
        Time = 10;

<del>(2, 9)</del>
<del>(2, 5)</del>
(2, 4)
(2, 1)
(2, NULL)
(4, 1)
(4, NULL)
(8, NULL)
(9, 7)
(9, 2)
(9, NULL)
(10, 8)
(10, 3)
(10, 1)
(10, NULL)
(1, 4)
(1, 2)
(1, NULL)

Stack

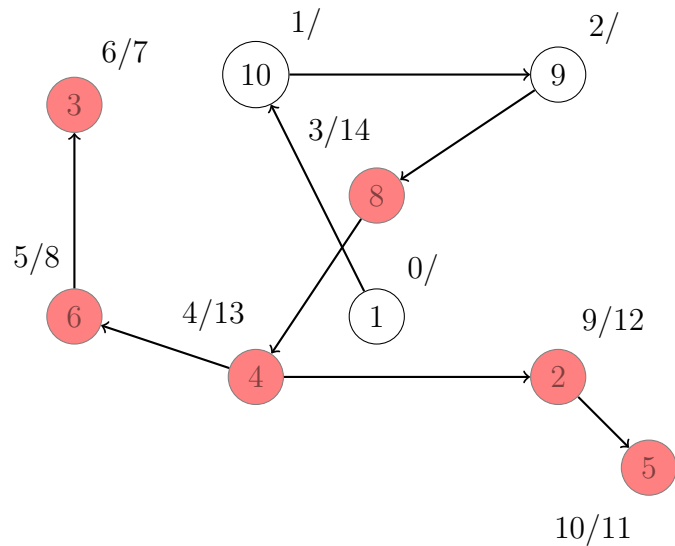




10.     Stack.push((5, NULL), (5, 2))  
           Stack.pop(); # pop (5, 2), do nothing  
           Stack.pop(); # pop (5, NULL), finished  
           Time = 11;  
           Stack.pop(); # pop (2, 4), do nothing  
           Stack.pop(); # pop (2, 1), do nothing  
           Stack.pop(); # pop (2, NULL), finished  
           Time = 12;  
           Stack.pop(); # pop (4, 1), do nothing  
           Stack.pop(); # pop (4, NULL), finished  
           Time = 13  
           Stack.pop(); # pop (8, NULL), finished  
           Time = 14

<del>(5, 2)</del>
<del>(5, NULL)</del>
<del>(2, 4)</del>
<del>(2, 1)</del>
<del>(2, NULL)</del>
<del>(4, 1)</del>
<del>(4, NULL)</del>
<del>(8, NULL)</del>
(9, 7)
(9, 2)
(9, NULL)
(10, 8)
(10, 3)
(10, 1)
(10, NULL)
(1, 4)
(1, 2)
(1, NULL)

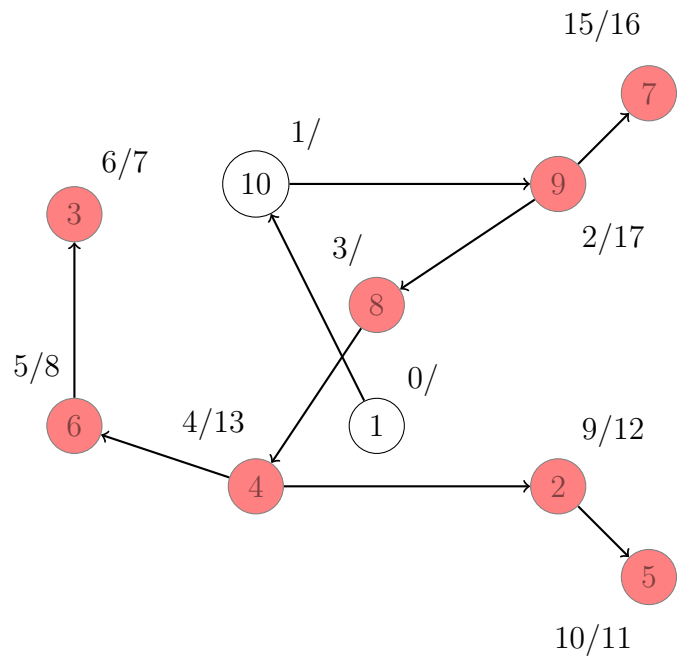
Stack



11.     Stack.pop() # pops (9, 7)  
           Time = 15;  
           Stack.push((7, NULL), (7, 9));  
           Stack.pop(); # pops (7, 9), do nothing  
           Stack.pop(); # pops (7, NULL), finished  
           Time = 16;  
           Stack.pop(); # pops (9, 2), do nothing  
           Stack.pop(); # pops (9, NULL), finished  
           Time = 17;

<del>(7, 9)</del>
<del>(7, NULL)</del>
<del>(9, 7)</del>
<del>(9, 2)</del>
<del>(9, NULL)</del>
(10, 8)
(10, 3)
(10, 1)
(10, NULL)
(1, 4)
(1, 2)
(1, NULL)

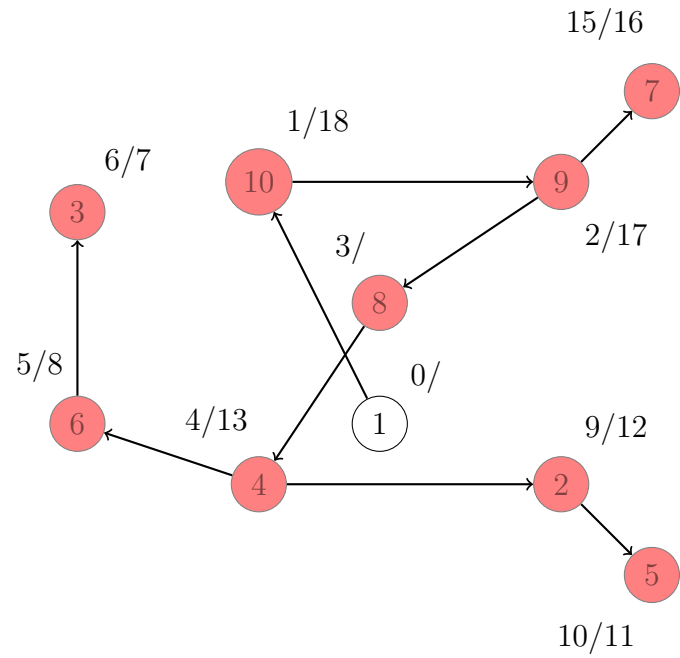
Stack



12.     Stack.pop() # pops (10, 8), do nothing  
          Stack.pop() # pops (10, 3), do nothing  
          Stack.pop() # pops (10, 1), do nothing  
          Stack.pop() # pops (10, NULL), finished  
          Time = 18;

<del>(10, 8)</del>
<del>(10, 3)</del>
<del>(10, 1)</del>
<del>(10, NULL)</del>
(1, 4)
(1, 2)
(1, NULL)

Stack



13.     Stack.pop() # pops (1, 4), do nothing  
           Stack.pop() # pops (1, 2), do nothing  
           Stack.pop() # pops (1, NULL), finished  
           Time = 19;

<del>(1, 4)</del>
<del>(1, 2)</del>
<del>(1, NULL)</del>

Stack

