Tuple (Point/Vector)

```
x, y, z, w : Double

dot(Vector) -> Double
cross(Vector) -> Vector
reflectOver(Vector) -> Vector

* scalar
/ scalar
```

Intersection

```
object : Object
t : Double
ray : Ray
-----
generateHitRecord() -> Intersection
```

HitRecord (struct)

hitPoint : Point normal : Vector (unit) eye : Vector (unit) overPoint : Point underPoint : Point

isInside: bool

Matrix

```
elements : Array, List, Vector/1 or 2D
-----
calculateDeterminant() -> Double
cofactor(i, j) -> Double
```

minor(i, j) -> Double submatrix(i, j) -> Matrix inverseMatrix() -> Matrix transposeMatrix() -> Matrix

Light

position : Point color : Color

virtual directionFromPoint(Point) -> Vector virtual distanceFromPoint(Point) -> Double

PointLight: Light

directionFromPoint(Point) -> Vector
distanceFromPoint(Point) -> Double

DirectionalLight: Light

direction: Vector

virtual directionFromPoint(Point) -> Vector
virtual distanceFromPoint(Point) -> Double

Material

color : Color diffuse : Double ambient : Double specular : Double shininess : Double reflectivity : Double transparency : Double indexOfRefraction : Double

colorAtPoint(HitRecord, World) -> Color

Shape

material : Material transform : Matrix

translate(x, y, z)
scale(x, y, z)
rotateAroundX(Double)
rotateAroundY(Double)
rotateAroundZ(Double)
virtual intersectionsWith(Ray) -> Intersections[]
virtual normalAt(Point) -> Vector(unit)

Sphere: Shape

intersectionsWith(Ray) -> Intersections[]
normalAt(Point) -> Vector(unit)

Plane: Shape

intersectionsWith(Ray) -> Intersections[]
normalAt(Point) -> Vector(unit)

Triangle: Shape

vertices : Point[]

intersectionsWith(Ray) -> Intersections[]
normalAt(Point) -> Vector(unit)

MeshTriangle: Triangle

indices : Int[] mesh : Mesh

Mesh: Shape

meshTriangles : MeshTriangle[]

vertices : Point[]

Color

Ray

```
origin : Point
direction : Vector

pointAtT(Double) -> Point
transform(Matrix) -> Ray
```

Scene

```
objects : Shape[]
lights : Light[]
-----
addObject(Shape)
addLight(Light)
intersectionsWith(Ray) -> Intersection[]
colorAtIntersection(Intersection, Intersection[]) -> Color
colorForRay(Ray) -> Color
```

Canvas

width : Int height : Int pixels : Color[]

toPPM() -> string writePPM(filename)