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Torus Primitive

Torus is one of the most important shape in our life. We have bagels, doughnuts and many other things. In order to have a better reconstruction of our daily life scenes in a 3D renderer, the best way to introduce torus as a single primitive instead of a combination of triangles or any other shapes.

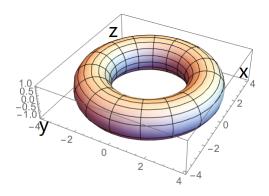


Figure 1: Torus Perspective View

I. Defining a Torus

There are three circles in a torus C_1, C_2, C_3 as shown in the graph below. C_2 is how a torus is defined, because the center of the tube is uniformly lying on it and by utilizing it we can reduce our equation for the torus. Then, we have the radius of C_2 as R and the raidus of the tube as r. Therefore, we know that from this graph: $x^2 + y^2 = R^2$.

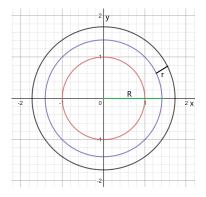


Figure 2: Torus Top View

Then, we just need to obtain the torus from x, y and z. Based on observation, we can see the cross section of a torus as the following graph, and could interpret that the size of the cube should be a function like the following: $(g(x,y))^2 + z^2 = r^2$. This means

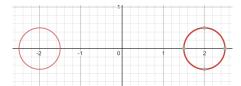


Figure 3: Torus Top View