

Rotating by an angle  $\theta$  around an arbitrary normalized direction  $(x, y, z)$ :

$$\begin{bmatrix} x^2 + \cos \theta(1 - x^2) & xy(1 - \cos \theta) - z \sin \theta & xz(1 - \cos \theta) + y \sin \theta & 0 \\ xy(1 - \cos \theta) + z \sin \theta & y^2 + \cos \theta(1 - y^2) & yz(1 - \cos \theta) - x \sin \theta & 0 \\ xz(1 - \cos \theta) - y \sin \theta & yz(1 - \cos \theta) + x \sin \theta & z^2 + \cos \theta(1 - z^2) & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Cross product of two vectors  $(x_1, y_1, z_1)$  &  $(x_2, y_2, z_2)$  is:

$$(y_1 z_2 - z_1 y_2, z_1 x_2 - x_1 z_2, x_1 y_2 - y_1 x_2)$$

Gives direction orthogonal to both vectors.

Cross product of  $(1, 0, 0)$  &  $(0, 1, 0)$ :

$$(0 \times 0 - 0 \times 1, 0 \times 0 - 1 \times 0, 1 \times 1 - 0 \times 0) = (0, 0, 1)$$