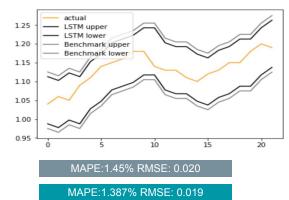
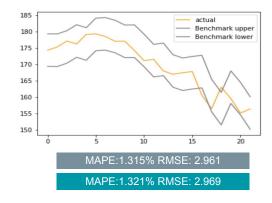
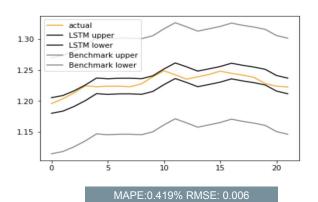
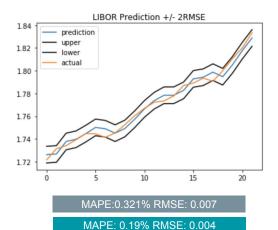
Long Short Term Memory







MAPE: 0.406% RMSE: 0.006



- Load the dataset from CSV file.
- 2. Transform the dataset to make it suitable for the LSTM model, including:
 - 2.1. Transforming the data to be **stationary**: differencing
 - 2.2. Transforming the data to a supervised learning problem: shifting
 - 2.3. Transforming the data so that it has the **scale** -1 to 1: MinMaxScaler(min=-1, max=1)
 - 2.4. Spliting data to training set and testing set

No.	Value
0	10
1	16
2	20
3	15

No.	Diff
0	NA
1	6
2	4
3	-5

No.	Х	Υ
0	NA	6
1	6	4
2	4	-5
3	-5	-6

No.	X_Scaled	Y-Scaled
0	0	0.8
1	0.8	0.7
2	0.7	-0.75
3	-0.75	-0.78

No.	
0-1237	Training Set
1238-1259	Testing Set

Step 2.4 Spliting

Original Data

Diff = [6,4,-5,...]

Step 2.1 Stationary Step 2.2 Shifting

X = [0,6,4,-5,...]Y = [6,4,-5,...,0] Step 2.3 Scaling

 $X_Scaled = [0,0.8,0.7,-0.75,...]$ $Y_Scaled = [0.8,0.7,-0.75,...0]$ $X_Scaled_Train = [0,0.8,0.7,-0.75,...]$ (1238) $Y_Scaled_Train = [0.8,0.7,-0.75,...]$ (1238)

X_Scaled_Test = [...] (length = 22)

Y_Scaled_Test = [...0] (length = 22)

Values = [10,16,20,15...]

- 3. Fitting a stateful LSTM network model to the training data: training
- 4. Recoding training **RMSE**
- 5. Evaluating the static LSTM model on the test data: **testing**;
- 6. Applying 2*RMSE (95% confidence) to prediction as upper and lower bounds.
- 7. Reverting scaling
- 8. Reverting differencing

No.	X_Training _Scaled	Prediction in last Epoch
0	0	0
1	0.8	0.4
2	0.7	0.6
3	-0.75	0.1
1237	0.5	0.4

No.	X_Test	Prediction by Trained Model
1238	0.8	0.9
1239	0.6	0.4
1240	0.5	0.3
1241	-0.75	0.1
1259	0.4	0.5

RMSE=rmse(X_Training_Scaled, Prediction in last Epoch) Suppose RMSE = 0.05

test rmse = rmse (X_Test, prediction by trained model)

No.	X_Test	Prediction by Trained Model	Lower Bound	Upper Bound
1238	0.8	0.9	0.7	1.0
1239	0.6	0.4	0.3	0.5
1240	0.5	0.3	0.2	0.4
1241	-0.75	0.1	0.0	0.2
1259	0.4	0.5	0.4	0.6

Step 6 Applying Bounds

Lower bound = Prediction - 2*RMSEUpper bound = Prediction + 2*RMSE"If the data are roughly normal, then most of the residuals lie within about \pm 2 RMSE of their mean (at zero)"

Benchmark -- Persistence Model

Yufei Zhang

- Load the dataset from CSV file.
- 2. Spliting data as LSTM
- 3. Make prediction: using observation of prior time stamp
- 4. Recording training RMSE
- 5. (For Random Walk Data only) Applying training rmse to testing data to get bounds.

"A good baseline forecast for a time series with a linear increasing trend is a persistence forecast." (1)

No.	Value
0	10
1	16
2	20
3	15

Step 1 Original Data

Values = [10,16,20,15...]

No.	
0-1237	Training Set
1238-1259	Testing Set

Step 2 Spliting

No.	X_Train	Benchmark prediction
0	10	0
1	16	10
2	20	16
1237	22	14

Step 3,4 Predicting

benchmark rmse = rmse (X_Train, Benchmark prediction)

No.	X_Test	Benchmark prediction	Lower Bound	Upper Bound
1238	15	18	17	19
1239	16	15	14	16
1259	13	0	-1	1

Step 5 Bounds

RMSE is getting from Step 4. Suppose rmse=0.5. Lower bound = Prediction - 2*RMSE Upper bound = Prediction + 2*RMSE

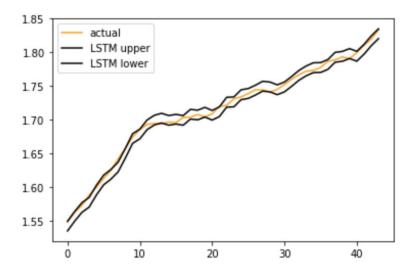
Random Walk Test usig MatLab econometrics toolbox

[h,pValue, stat, cValue, ratio] = vratiotest(data)

	LIBOR	APPL	SWAP	DEXUSEU
h (logical)	1	0	0	0
Random Walk?	N	Υ	Υ	Υ

h=0 : vratiotest does not reject the hypothesis that a random walk is a reasonable model for the stock series.

h=1: vratiotest reject the hypothesis that a random walk is a reasonable model for the stock series.



Data: LIBOR

Predict window: 44 days

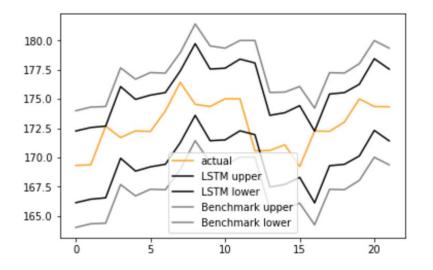
Breaches: 3

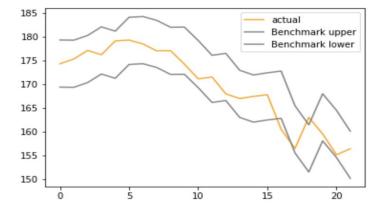
Bounds: 2* training rmse (22-43 days use a different rmse from 0-21 days)

Training set: 22-43 days have a larger(22 days more) training set.

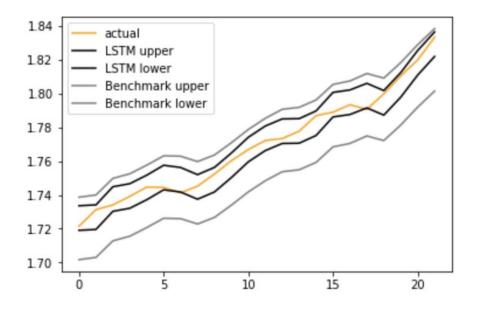
Still debugging the program that can automatcally backtesting. Once

completed, more days prediction can be provided.





LIBOR Yufei Zhang



RMSE: rmse got from model training process Upper bounds: prediction + 2 * RMSE Lower bounds: prediction - 2 * RMSE

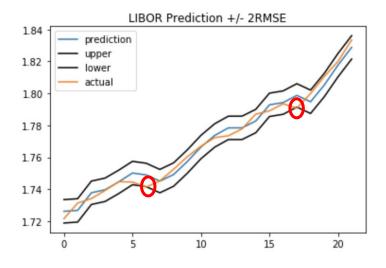
Accuracy	MAPE%	RMSE	Breach
Benchmark	0.321	0.00667	0
Before Stationary	0.28	0.0060	NA
After Stationary	0.1927	0.00412	2

Benchmark model got less breaches, however, it's using a wider bounds.

I suspect that benchmark model gives too wide bound to detect breaches. Still need real data with actual breaches to figure out which model is better.

LIBOR Hyperparameters Tuning (Batch_Size = 1)

No	Epochs	Neurons	MAPE	RMSE	Breaches
1	15	40	0.20450	0.00424	0
2	20	40	0.20349	0.00424	0
3	30	40	0.19677	0.00415	0
4	35	40	0.20030	0.00425	1
5	32	40	0.19435	0.00420	1
6	30	30	0.19888	0.00419	0
7	30	50	0.21470	0.00438	1
8	30	45	0.19271	0.04119	2



Lower Bound	Actual	Upper Bound
1.74158818901279	1.7413	1.75622873729980
1.791383221522132	1.7907	11.80602376980914

^{*}Blue Numbers are best are currently best accuracy. Orange numbers are chosen hyperparameters.

Why prediction looks like a left move

Random Walk Hypothesis

"A random walk is one in which future steps or directions cannot be predicted on the basis of past history. When the term is applied to the stock market, it means that short-run changes in stock prices are unpredictable."

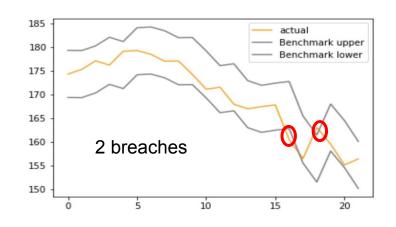
Page 26, <u>A Random Walk down Wall Street: The Time-tested Strategy</u>
 for Successful Investing

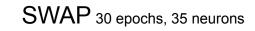
Persistance Model provides the best source of reliable predictions.

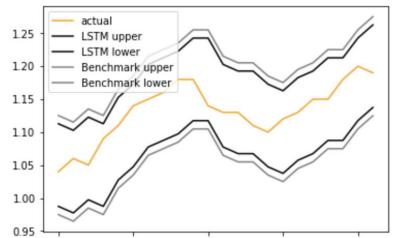
"This is key for time series forecasting. Baseline forecasts with the persistence model quickly flesh out whether you can do significantly better. If you can't, you're probably working with a random walk."

-- Jason Brownlee A Gentle Introduction to the Random Walk

Accuracy	MAPE%	RMSE	Breach
Benchmark	1.135	2.961	2
Before Stationary	1.28	2.99	NA
After Stationary	1.321	2.969	7



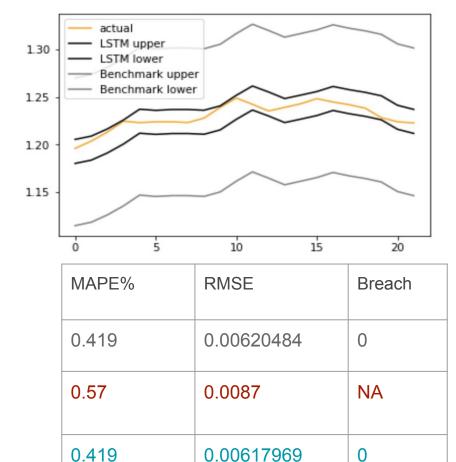




0.05	~		
0.95	5	10 15	20
Accuracy	MAPE %	RMSE	Breach
Benchmark	1.45	0.0197714	0
Before Stationary	1.42	0.018	NA
After Stationary	1.449	0.01975	0

DEXUSEU 60 epochs, 45 neurons

Yufei Zhang



Summary

- LIBOR is predictable. LSTM provides a significat improve on predicting over persistence model.
- SWAP, DEXUSEU and APPL are random walk, indicating they're **not predictable**.
- LSTM is still usful on random walk data by providing a tight bound.
 - bound is determined by training rmse
 - After rounds of training, LSTM can simulate **training** data better than persistence model
 - LSTM outputs a smaller rmse than persistence model

Market Data	Random Walk?	Best performance model	Breaches detected by best performance model in 22 days
LIBOR	N	LSTM	2
APPL (Stock)	Υ	Persistence Model	2
SWAP	Y	LSTM / Persistence Model	0
DEXUSEU (Exchange rate)	Υ	LSTM / Persistence Model	0

Prediction looks like a left move

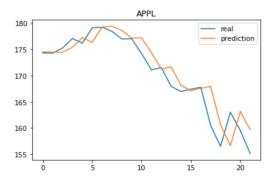
Random Walk Hypothesis

"A random walk is one in which future steps or directions cannot be predicted on the basis of past history. When the term is applied to the stock market, it means that short-run changes in stock prices are unpredictable."

— Page 26, A Random Walk down Wall Street: The Time-tested Strategy for Successful Investing

- Persistance Model provides the best source of reliable predictions.
- "This is key for time series forecasting. Baseline forecasts with the persistence model quickly flesh out whether you can do significantly better. If you can't, you're probably working with a random walk."
- -- Jason Brownlee https://machinelearningmastery.com/gentle-introduction-random-walk-times-series-forecasting-python/

APPL Stock
Yufei Zhang



First Four days:

predicted:[[174.06352]], actual:[[174.33]]
predicted:[[174.0441]], actual:[[174.29]]
predicted:[[174.00528]], actual:[[175.28]]
predicted:[[174.96577]], actual:[[177.09]]

Tuning the Epoch

One Epoch: Whole data set go through neural network once Larger the epoch size, longer the calculation time

Epochs	MAPE	RMSE
100	1.15510211	2.7777774914911446
300	1.15351336	2.7631627514012953
500	1.21856932	2.9026333327139775
1000	1.19991636	2.685796528535209

Tuning the Training Batch size *Under epoch size=300

Batch: subset of sample. Iteration in each epoch = sample size/ batch size Smaller the batch size, longer the calculation time

Tuning the Num of Neurals *epoch=300, batch size=100

The number of neurons affects the learning capacity of the network.

More neurons, longer the training time.

More learning capacity also creates the problem of potentially overfitting the training data.

Batchs	MAPE	RMSE
10	1.32042804	3.0935492293336155
100	1.16456492	2.7869327110175006
500	1.55472734	3.3439883563233956
1000	1.50658704	3.2703686091609

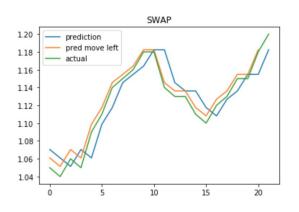
J	J	
Neurons	MAPE	RMSE
128	1.16724945	2.7926793040158913
256	1.16456492	2.7869327110175006
512	1.55472734	3.3439883563233956
1000	1.50658704	3.2703686091609

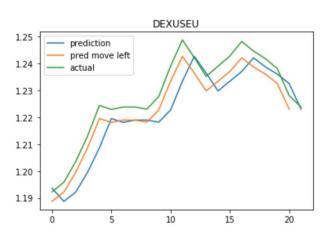
^{*}Instead of using 1000 epochs which takes a long time to run, I choose 300 epochs finally.

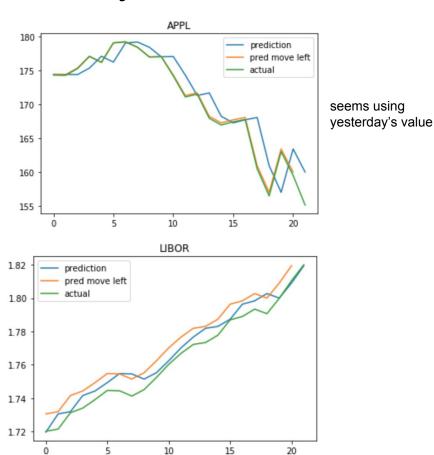
Two concerns of should we continue using LSTM

- 1. It seems LSTM just use yesterday's value as the prediction for today ???
 - a. Depends on nature of data. For some data set, it is true. For some, it isn't.
 - b. Common across other one-day prediction algorithm
- 2. Impossible to get prediction interval

Prediction=actual move right one day?







Two concerns of should we continue using LSTM

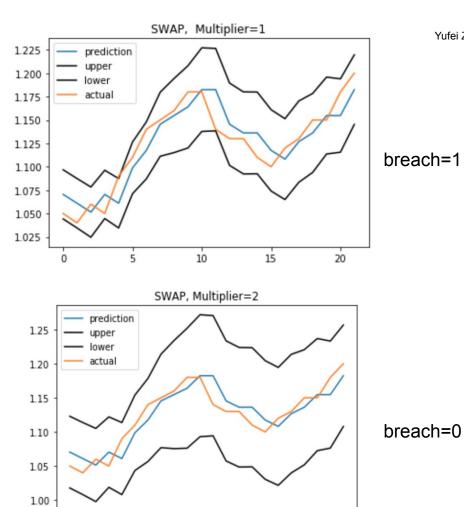
1. It seems LSTM just use yesterday's value as the prediction for today ???

2. Impossible to get prediction interval

- a. But we can always +/- a std of past N days to prediction value to get bound like Bollinger Bands:
 - i. upper bound= LSTM prediction + (std of past 20 days * multiplier)
 - ii. lower bound= LSTM prediction (std of past 20 days * multiplier)

	Muptilpier=0.5	Muptilpier=1	Muptilpier=2 (BB)
SWAP	8	1	0
APPL	10	4	0
US-EU	10	4	0
LIBOR	1	0	0

Number of breaches using different multiplies on different dataset



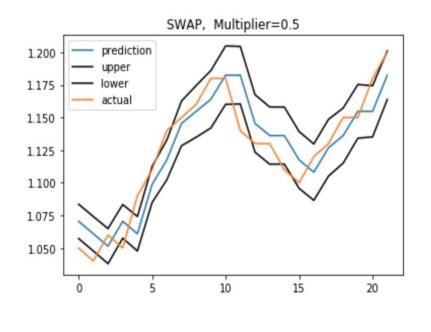
10

5

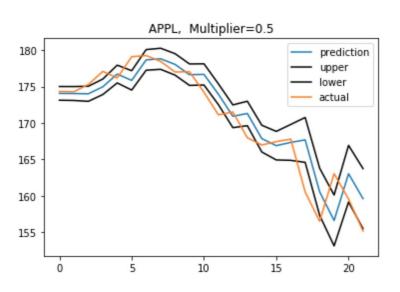
15

20

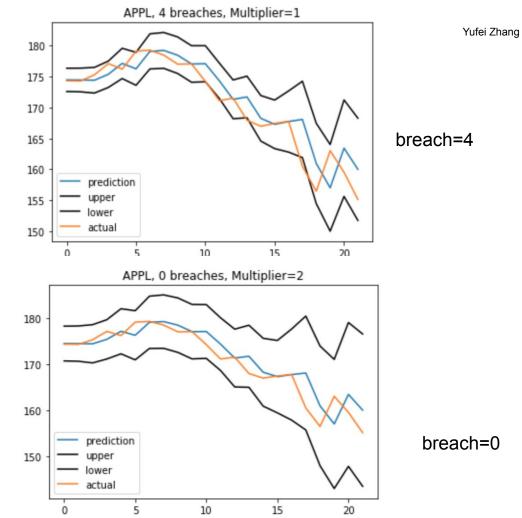
Yufei Zhang



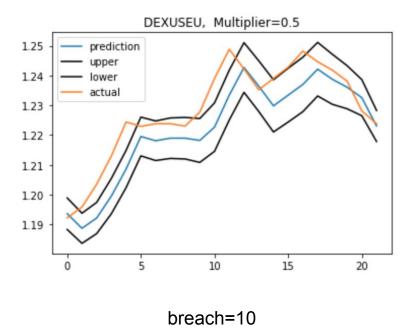
breach=8

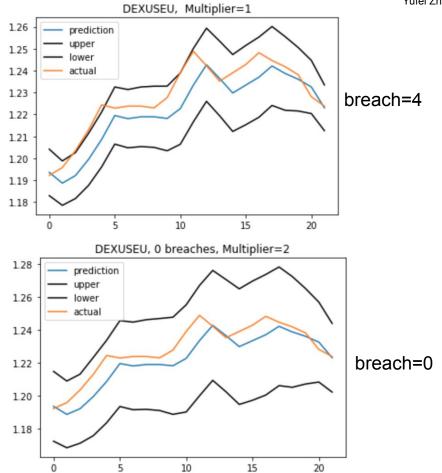


breach=10

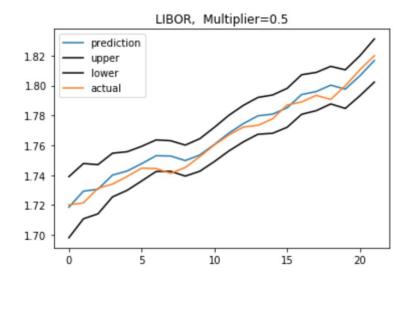


DEXUSEU

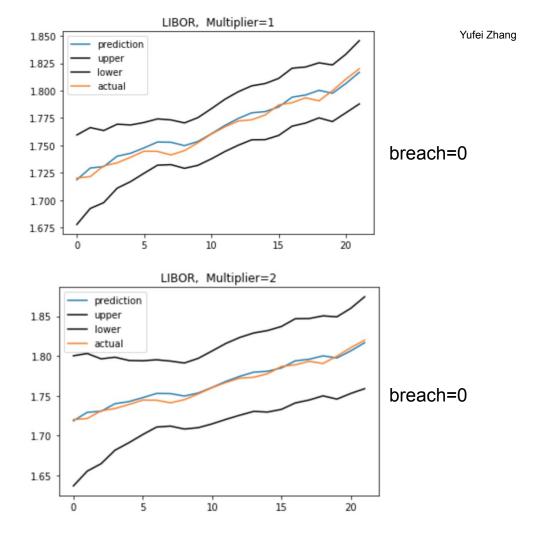




LIBOR



breach=1



Literature Review of Time Series Data Analysis

METHOD	DETAIL	PROS	CONS
SIMPLE MOVING AVERAGE	Adding up the last 'n' period's values and then dividing that number by 'n'. Moving average value is considering as the forecast for next period	 Quickly detect trend A moving average is used to smooth out irregularities (peaks and valleys) to easily recognize trends. 	Not accurate compared with other methods
EXPONENTIAL SMOOTHING	Exponential Smoothing assigns exponentially decreasing weights as the observation get older.	 Can "smoothing" out the data by removing much of the "noise" (random effect) from the data by giving a better forecast. 	Restrict to data with no trend or seasonal pattern
ARIMA	The parameters used in the ARIMA is (P, d, q) which refers to the autoregressive, integrated and moving average parts of the data set, respectively.	 Simple Achieve great performance on many data set 	 Fail to detect complex time series patterns that cannot be determined by simple parametric models.
ARITIFICIAL NEURAL NETWORK	Machine learning approach that models human brain and consists of a number of artificial neurons	Flexible Detect complex patterns	 Takes long time to run Often require more data than other models

Reference

https://www.bistasolutions.com/resources/blogs/5-statistical-methods-for-forecasting-quantitative-time-series/https://datascience.stackexchange.com/questions/12721/time-series-prediction-using-arima-vs-lstm

Random Walk Test usig MatLab econometrics toolbox

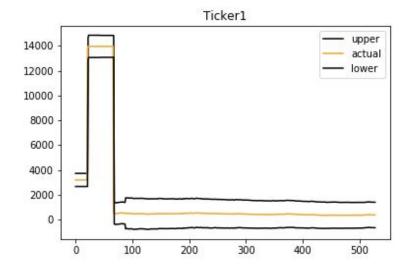
[h,pValue,stat,cValue,ratio] = vratiotest(data)

	1	2	3
h (logical)	0	1	0
Random Walk?	Υ	N	Υ

2.1	2.2
1	0
N	Υ

h=0 : vratiotest does not reject the hypothesis that a random walk is a reasonable model for the stock series.

h=1: vratiotest reject the hypothesis that a random walk is a reasonable model for the stock series.



Random Walk: Y

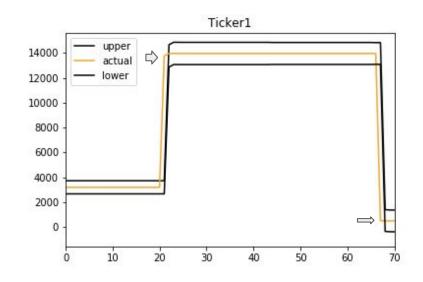
Train: 819 days

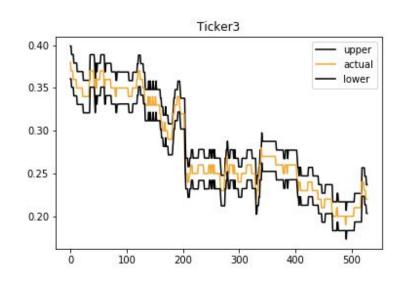
Test: 528 days

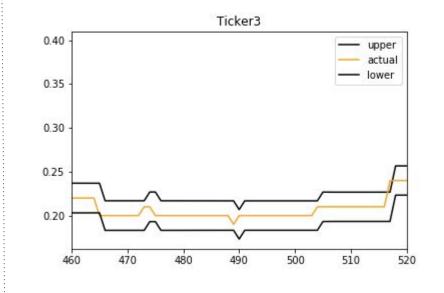
Model: Persistence Model

Breachs: 2

Breach Position: 21, 67







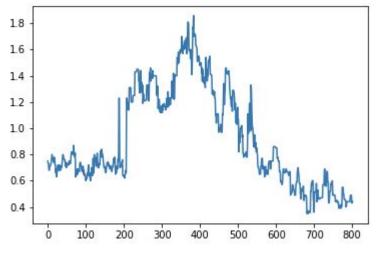
Random Walk: Y Breachs: 13

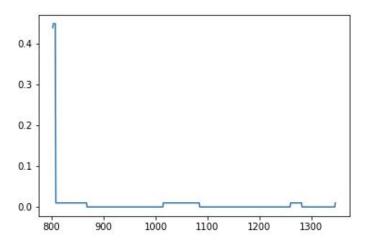
Train: 819 days Breach Position: 34, 43, 44,

Test: 528 days 60, 132, 203, 204, 274, 329,

Model: Persistence 336, 339, 465,517

I tried LSTM for ticker 3. Number of breaches and position of breaches were exactly same with persistence model.

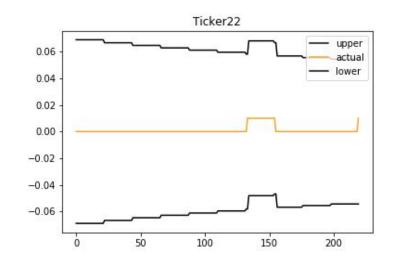




0 - 819 Day

820 ~

Ticker 2.2



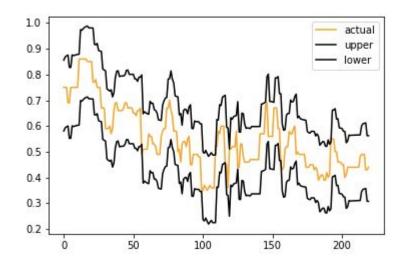
Random Walk: Y Breachs: 0

Train: 819 days Breach Position: NA

Test: 528 days

Model: Persistence

Ticker 2.1



Random Walk: N

Train: 580 days

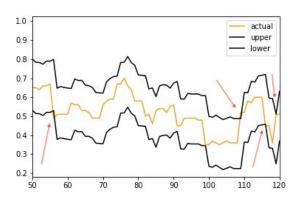
Test: 220 days

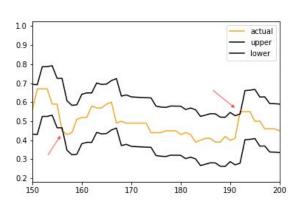
Model: LSTM

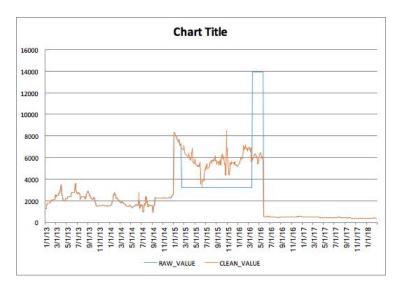
Breachs: 6

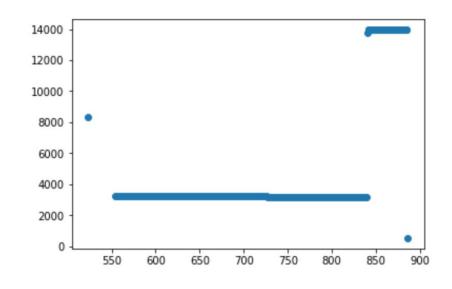
Breach Position: 56, 109, 116,

119, 156, 192









Random Walk: Y

Model: Persistence Model

Train: 520 days

Breachs: 2

Test: 528 days

Breach Position: 21, 67



Random Walk: N

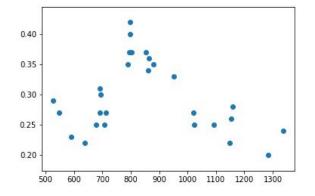
Train: 520 days Breachs: 2

Test: 528 days

Breach Position: 21, 67

Model: Persistence Model





Predict\Actual	Wrong Input	Correct Input	Sum
Wrong Input	1	27	28
Correct Input	1	798	799
Sum	2	825	827



Random Walk: N

Train: 520 days

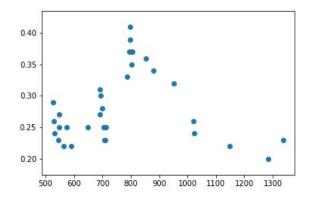
Test: 528 days

Model: Persistence Model

Breachs: 2

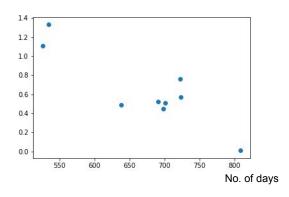
Breach Position: 21, 67





Predict\Actual	Wrong Input	Correct Input	Sum
Wrong Input	1	32	33
Correct Input	1	793	794
Sum	2	825	827

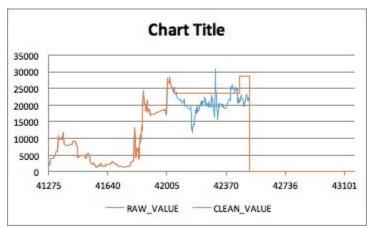




Predict\Actual	Wrong Input	Correct Input	Sum
Wrong Input	1	8	9
Correct Input	0	818	818
Sum	1	826	827

Train: 520 days

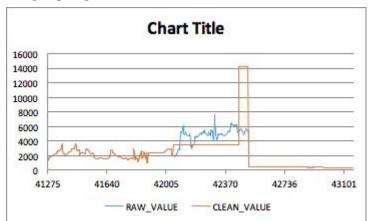
Test: 827 days



Ticker 9



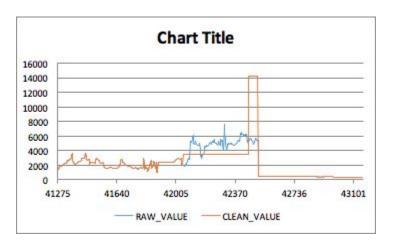
Ticker 8



Ticker 10



Yufei Zhang



Random Walk: Y | Model: Persistence Model

Train: 520 days Breachs: 2

Test: 528 days Breach Position: 21, 67



Random Walk: Y | Model: Persistence Model

Train: 520 days Breachs: 2

Test: 528 days Breach Position: 21, 67



Random Walk: Y | Model: Persistence Model

Train: 520 days Breachs: 2

Test: 528 days Breach Position: 21, 67

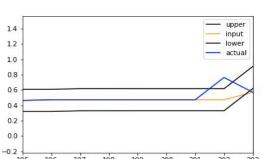
1.5

1.5

2

Problem Group 1: Fail to detect flat.

From model's view, the "anomaly" is very consistent with previous days.



0

0

0.0238

0.0192

			o dayo.	0.8 - 0.6 - 0.4 - 0.2 - 0.0 - -0.2 - 195 196 197 198	199 200 201 202 203
Ticker	Multiplier	Missed Anomalies	Total Anamalies	Recall	Precision

				0.0 - -0.2 - 195 196 197 198	199 200 201 202 203
Ticker	Multiplier	Missed Anomalies	Total Anamalies	Recall	Precision

0

0

0

0.5

0.5

		14000	1			- input
Extremely small multiplier can incr	ed by wrong flat	1			- lower - actual	
Extraction of their manaphor bear mor	ace recail. But the presion to cade	-	1			
input, and should not be solved in	his wav.	8000	N 17	M.		
ļ,	mpat, and onedia not be contea in the may.					
Ticker 1 and 14 can use a normal multiplier just because real data doesn't come across the			my V	-		
	•	2000	1			
flat frequently.		0	-			
			0 200	400	600	800

Ticker	Recall	Precision	<u> </u>	
flat frequently.	2000 -			
Ticker 1 and 14 can	4000 -			
input, and should no	t be solved in this	8000 - 6000 -	_m	

0.0028

0.00001

0.05

0.005

0.5

2

8

12

13

14

0

0

36

0

332

334

332

750

332

332

332

0.9969

0.952

0.9969

0.9969

0.9792

0.9002

0.8447

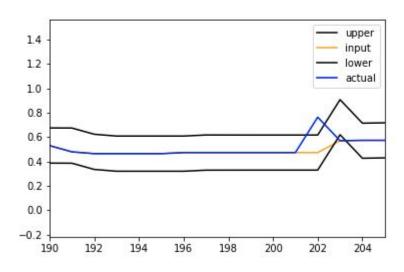
0.9107

0.8422

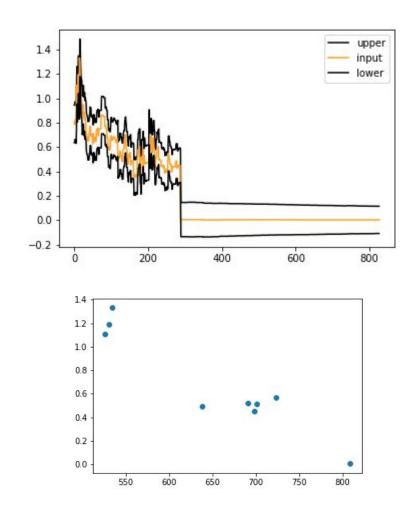
0.9792

0.9910

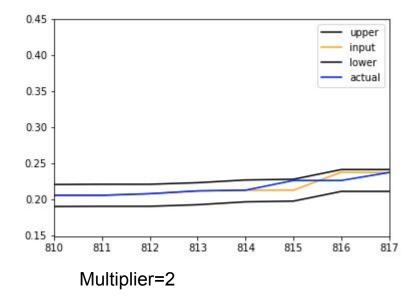
Missed Anomalies: 1

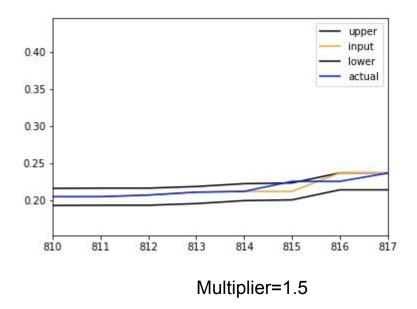


From models's view, input of No722 day is very normal.



Ticker 3 Missed Anomalies : 1

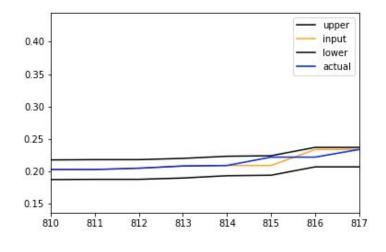




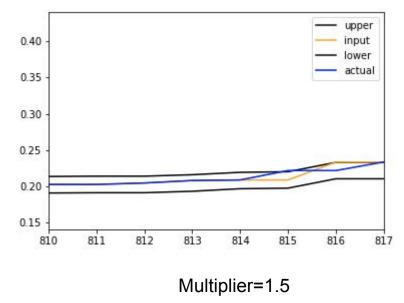
Decreasing Multiplier can solve the second anomaly

For the first anomaly: Flat Problem!

Ticker 5 Missed Anomalies : 1



Multiplier=2



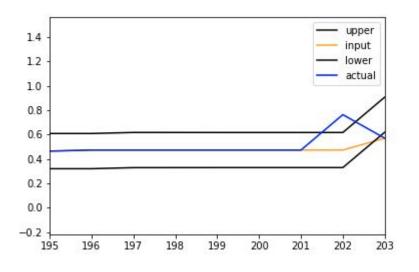
Decreasing Multiplier can solve the second anomaly

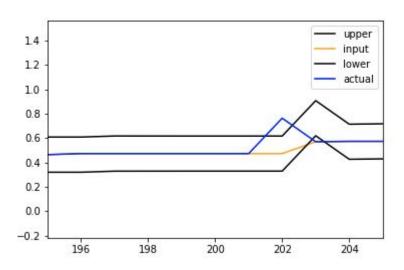
For the first anomaly: Flat Problem!

Missed Anomalies: 1

Ticker 6

Missed Anomalies: 1

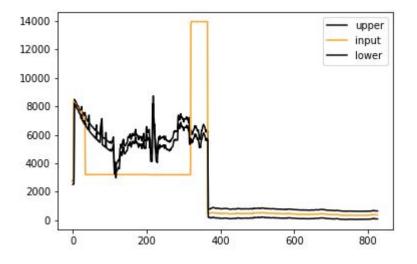


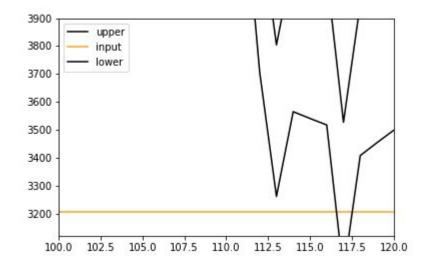


Flat Problem!

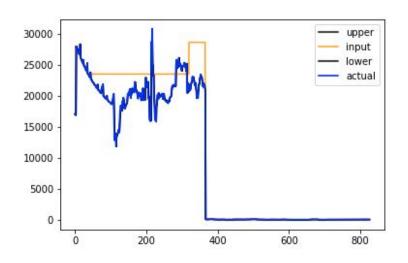
Flat Problem!

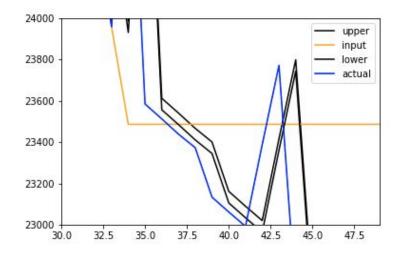
Ticker 1 Missed Anomalies : 1



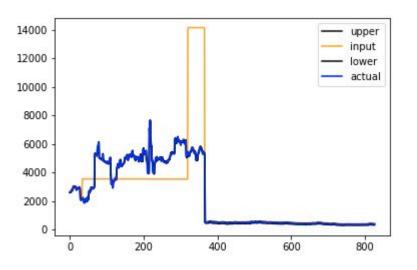


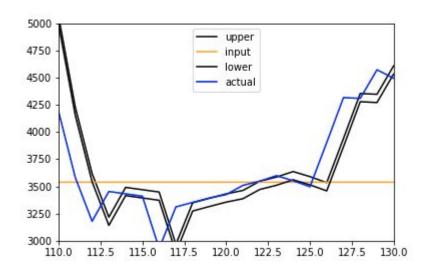
Missed Anomalies: 0 Multiplier: 0.0028

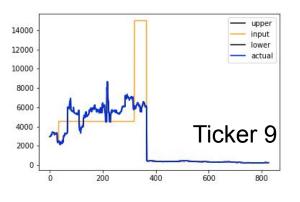


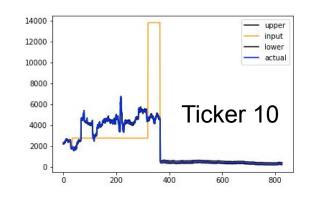


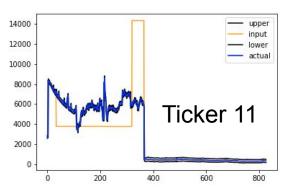
when Multiplier=0.003, Missed Anomalies : 0
Reason : Input happens to be in the range

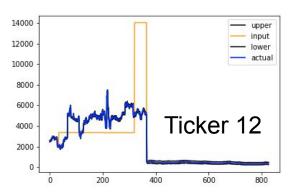


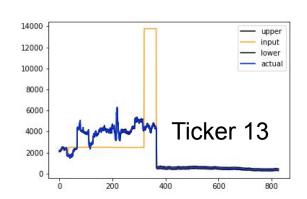


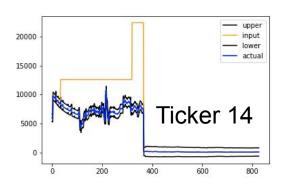










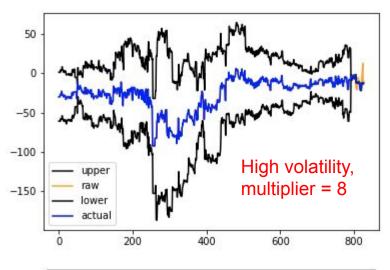


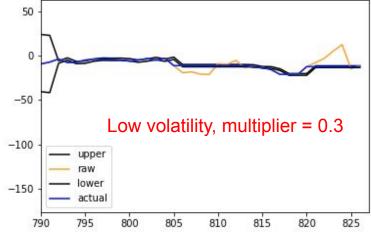
Lucky! Multiplier = 2 can achieve recall =1

Ticker	Multiplier	Total Breaches	Total Anamalies	# False Positive	Missed Anomalies	Recall	Precision
15	1.3	364	307	57	0	1	0.8434
16	5 for Day 521-961 0.05 for the rest	345	317	28	6	0.9810	0.9014
17	10 for Day 521-1313 0.3 for the rest	26	17	9	3	0.8235	0.5384

CLEAN _DATE	BEFORE_ADJU STMENT	ADJUST MENT	CLEAN_ VALUE	
8/1/16	-46.605	-47.1376	-47.1376	
5/18/17	-21.0302	-21.0238	-21.0238	
5/19/17	-21.0302	-21.0174	-21.0174	
1/31/18	-19.1105	-11.0808	-11.0808	
2/1/18	-18.1049	-11.0808	-11.0808	

Missing anomalies.
Changes were too small to detect.





Precision

0.9014

Ticker 16

Day	Multiplier	Total Breaches	Total Anamalies	# False Positive	Missed Anomalies
521-961	5	345	317	28	6
962-	0.05				
		60 40 - 20 - 0 - 20 -	200	400	upper raw lower actual

Recall

0.9810

Persistence Model -- Iteratively Test Multiplier

Environment: Jupyter Notebook / Jupyter Lab. Free.

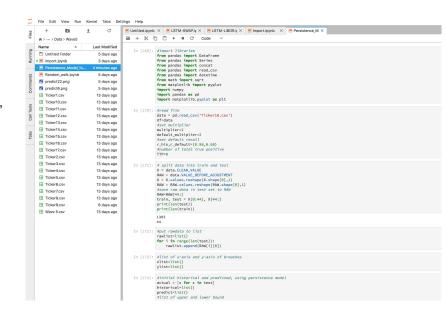
Files

import.ipynb

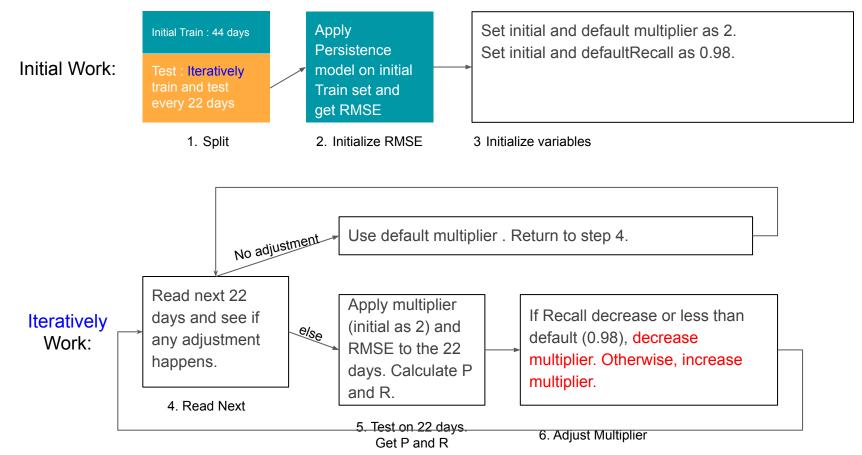
- Input: a csv file with all data (various tickers, raw value, clean value, adjustments...)
- Output: csv files. Number of output files = number of tickers. Each
 csv file contains data of one ticker.
- Function: Import and pre-processing data. Can be used to split different tickers to seperate files.
- How to use: save with sourcing csv file (e.g. wave5.csv). Run from the first cell.

Persistence_Model.ipynb

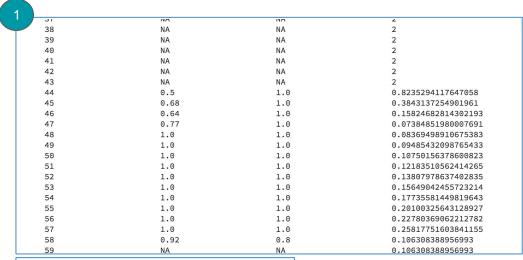
- Input: Output of import.ipynb, ticker csv files.
- Output: Multiplier, precision, recall, breaches.
- Function: Predict values and calculate bounds. Logic can be found in next slide. Text anotations can be found in code.
- How to use: save with sourcing csv file (e.g. ticker1.csv). Run from the first cell.

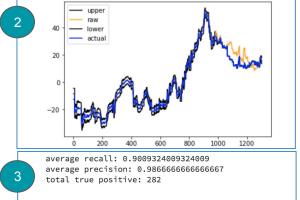


Persistence Model -- Iteratively Test Multiplier



Output of Persistence_Model.ipynb





- Table of p, r and multiplier after adjustment in each period. IF there's no adjustment in that period, p and r will be "NA".
- 2. Visualization of data and bounds.
- Average recall and average precision in 60 periods, and number of total true positives.

Objective

- Detecting anomalies using Prediction + Dynamic Bound
- Predicting one day forward using Persistence Model
- Automatically adjusting bound by iteratively train and test on given data

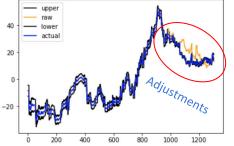
Outcome

- Prediction -- Using observation of (N-1)th day as prediction to Nth day.
 - Comparison between LSTM and Persistence model showing that Persistence Model is more suitable for market data, which is mostly a random walk.
- Dynamic Range -- Adjusting range after every testing.
 - Taking every 22 days as a train/test slice.
 - Testing: Applying current range to a test slice. Using precision and recall as result of test.
 - Training: Adjusting bound when recall is not satisfying.

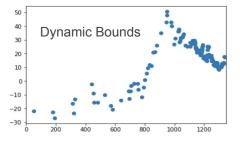
Conclusions

- Persistence model is suitable for providing a prediction of market data.
- Dynamic bound can learn from the past pattern and self-adjust to fit the ticker.

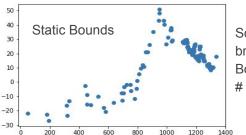
Yufei Zhang



Bounds and adjustments.
Total Adjustments = 317



Scatter plot of breaches using Dynamic Bounds. # Well-detected = 282



Scatter plot of breaches using Static Bounds.

Well-detected = 189