## An Alternative Method for Characterization and Comparison of Plant Root Shapes

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## Existing Morphological Descriptors for Root Systems

# An Alternative Mathematical Method for Shape Description

## LRWs in Artificial Images

### 3.1 Circle and Rectangle

#### 3.1.1 Image Description

 $\bullet$  Image size:  $1200\times1000$  pixels

• Surface area of shapes: 90000 pixels

• The centroid of the shape is located at the center of the image

#### 3.1.2 Output Analysis

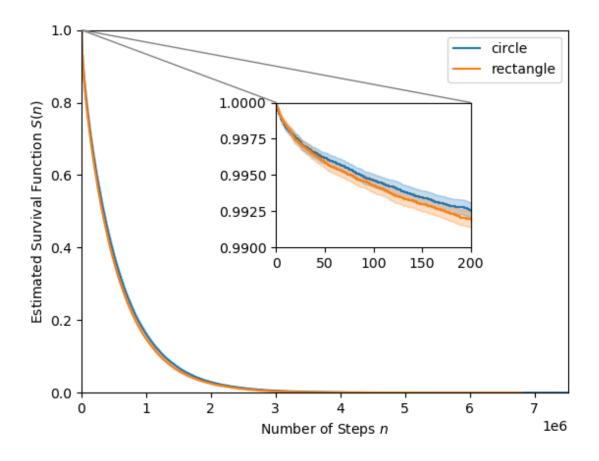


Figure 3.1

#### 3.1.3 Conclusion

Given two distinct convex geometries

	test_statistic	р
Peto	137.23	0.0
Logrank	137.23	0.0
Tarone-Ware	134.31	0.0
Gehan-Breslow	123.83	0.0
Fleming-Harrington	123.83	0.0

Table 3.1

- the behaviours of the survival function of LRWs are consistent with the theoretical results.
- $\bullet\,$  survival curves can be used to describe and distinguish them.

#### 3.2 Complicated Branching Structures

#### 3.2.1 Image Description

• Image size:  $1200 \times 1000$  pixels

• Surface area of shapes: 90000 pixels

• Iterate the template 3, 4, 5, 6 times to produce the targeted branching geometries labelled as  $L_3, L_4, L_5, L_6$ .

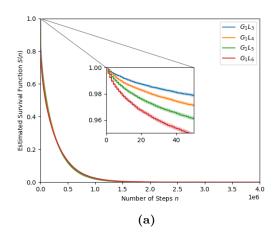
• Two groups of images labelled as  $G_1, G_2$ 

-  $G_1$ : the target object  $G_1L_i$  (i=3,4,5,6) is equidistant to the edges of an image.

-  $G_2$ : the template of  $G_2L_i$  (i = 3, 4, 5, 6) is distinct from  $G_1$  (thickness and aspect ratio).

#### 3.2.2 Output Analysis

#### **3.2.2.1** S(n)



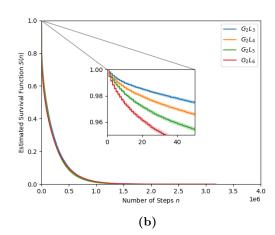


Figure 3.2

**3.2.2.2** S(d)

**3.2.2.3** S(R)

#### 3.2.3 Conclusion

- In a short time, the survival function of rectangle decays faster than the circle, which conforms to the analytical results.
- The differences of estimated survival functions between circle and rectangle are statistically significant, which coincides with the real shape dissimilarities.

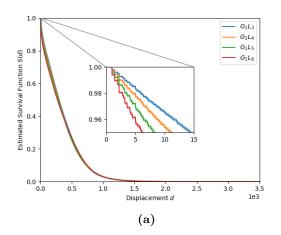
			p		
		Logrank	TW	GB	FH
$G_1 L_3$	$G_1 L_4$	0.4393	0.0285	0.0005	0.0005
	$G_1 L_5$	0.0	0.0	0.0	0.0
	$G_1 L_6$	0.0	0.0	0.0	0.0
$G_1 L_4$	$G_1 L_5$	0.0007	0.0	0.0	0.0
	$G_1 L_6$	0.0002	0.0	0.0	0.0
$G_1 L_5$	$G_1 L_6$	0.7223	0.0	0.0	0.0

**Table 3.2** 

			р		
		Logrank	TW	GB	FH
$G_2 L_3$	$G_2 L_4$	0.0	0.0	0.0	0.0
	$G_2 L_5$	0.0	0.0	0.0	0.0
	$G_2 L_6$	0.0	0.0	0.0	0.0
$G_2 L_4$	$G_2 L_5$	0.0016	0.0	0.0	0.0
	$G_2 L_6$	0.0004	0.0	0.0	0.0
$G_2 L_5$	$G_2 L_6$	0.7199	0.0	0.0	0.0

Table 3.3

- Within a same group, when t is small, the more branching the object is, the faster the survival function decays.
- Within a same group, the pairwise survival functions are statistically different.
- The corresponding target structures in  $G_1$  and  $G_3$  are invariant shapes under translation since their survival function are not statistically different. In other words, periodic boundary conditions of the image can eliminate the effect of the locations.
- LRWs can describe and classify the geometries, their spatial configurations, and the unoccupied area in the image.



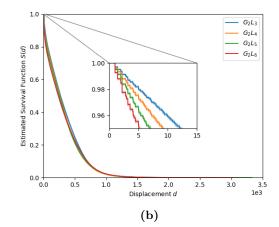


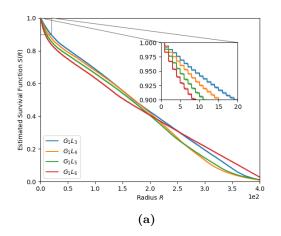
Figure 3.3

			p		
		Logrank	TW	GB	FH
$G_1 L_3$	$G_1 L_4$	0.0	0.0	0.0	0.0
	$G_1 L_5$	0.0	0.0	0.0	0.0
	$G_1 L_6$	0.0	0.0	0.0	0.0
$G_1 L_4$	$G_1 L_5$	0.0072	0.0	0.0	0.0
	$G_1 L_6$	0.0003	0.0	0.0	0.0
$G_1 L_5$	$G_1 L_6$	0.2883	0.0	0.0	0.0

Table 3.4

			р		
		Logrank	TW	GB	FH
$G_2 L_3$	$G_2 L_4$	0.0	0.0	0.0	0.0
	$G_2 L_5$	0.0	0.0	0.0	0.0
	$G_2 L_6$	0.0	0.0	0.0	0.0
$G_2 L_4$	$G_2 L_5$	0.0001	0.0	0.0	0.0
	$G_2 L_6$	0.0015	0.0	0.0	0.0
$G_2 L_5$	$G_2 L_6$	0.7019	0.0	0.0	0.0

Table 3.5



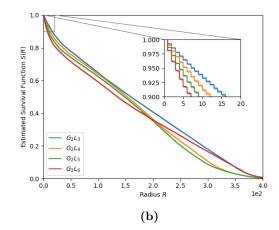


Figure 3.4

			р		
		Logrank	TW	GB	FH
$G_1 L_3$	$G_1 L_4$	0.0	0.0	0.0	0.0
	$G_1 L_5$	0.0	0.0	0.0	0.0
	$G_1 L_6$	0.0	0.0	0.0	0.0
$G_1 L_4$	$G_1 L_5$	0.1773	0.0	0.0	0.0
	$G_1 L_6$	0.0	0.0	0.0	0.0
$G_1 L_5$	$G_1 L_6$	0.0	0.0	0.0	0.0

**Table 3.6** 

			р		
		Logrank	TW	GB	FH
$G_2 L_3$	$G_2 L_4$	0.0	0.0	0.0	0.0
	$G_2 L_5$	0.0	0.0	0.0	0.0
	$G_2 L_6$	0.0	0.0	0.0	0.0
$G_2 L_4$	$G_2 L_5$	0.0	0.0	0.0	0.0
	$G_2 L_6$	0.0	0.0	0.0	0.0
$G_2 L_5$	$G_2 L_6$	0.0	0.0	0.0253	0.0253

Table 3.7

## LRWs in Real Root Images

### CONCLUSION

## FUTURE WORK

### Appendix A

# Numerical Methods for Solving Parabolic Partial Differential Equations

- A.1 Introduction
- A.2 Summary of Commonly Used Numerical Techniques
- A.3 Limitation in Practice

## APPENDIX B METHOD VALIDATION IN ANNULUS

- **B.1** Analytical Results
- **B.2** Numerical Approximation
- **B.3** Comparison of Numerical and Analytical Results
- B.4 Conclusion

### REFERENCES