

Home Alarm case write-up

Yuhan Xu 474154

1. What is the LTV (looking 8 years out) of a customer who will use auto-pay? (7 points)

\$1585.29

	Year 2	Year 3	Year 4	Year 5	Year 6	Year 7	Year 8	Year 9			
revenue	480	494.4	509.232	524.509	540.2442	556.4516	573.1451	590.3395	×	103.00%	
cost of service	72	74.16	76.3848	78.67634	81.03663	83.46773	85.97177	88.55092	×	103.00%	
MKT cost	24	24.72	25.4616	26.22545	27.01221	27.82258	28.65726	29.51697	×	103.00%	
profit	384	395.52	407.3856	419.6072	432.1954	445.1612	458.5161	472.2716	revenue - cost of service - MKT cost		
probability of being active	93.00%	0.83979	0.753292	0.681729	0.628554	0.585184	55.07%	52.15%	$Y(n-1) * (1 - \text{attrition rate of year } n)$		
profit expected on average	357.12	332.1537	306.8802	286.0583	271.6582	260.5012	252.4855	246.2769	profit * probability		
discount rate	1.1	1.21	1.331	1.4641	1.61051	1.771561	1.948717	2.143589	$1.1^{(n-1)}$		
present value	324.6545	274.5072	230.5636	195.3817	168.6783	147.0461	129.565	114.89	profit * discount rate		
	LTV	1585.287	total present value								

2. What is the LTV (looking 8 years out) of a customer who will not use auto-pay? (7 points)

\$1291.75

	Year 2	Year 3	Year 4	Year 5	Year 6	Year 7	Year 8	Year 9			
revenue	480	494.4	509.232	524.509	540.2442	556.4516	573.1451	590.3395	×	103.00%	
cost of service	72	74.16	76.3848	78.67634	81.03663	83.46773	85.97177	88.55092	×	103.00%	
MKT cost	24	24.72	25.4616	26.22545	27.01221	27.82258	28.65726	29.51697	×	103.00%	
profit	384	395.52	407.3856	419.6072	432.1954	445.1612	458.5161	472.2716	revenue - cost of service - MKT cost		
probability of being active	87.80%	0.735764	0.622456	0.539047	47.44%	0.421707	38.12%	34.84%	$Y(n-1) * (1 - \text{attrition rate of year } n)$		
profit expected on average	337.152	291.0094	253.5798	226.1881	205.0169	187.7278	174.7971	164.5575	profit * probability		
discount rate	1.1	1.21	1.331	1.4641	1.61051	1.771561	1.948717	2.143589	$1.1^{(n-1)}$		
present value	306.5018	240.5036	190.5182	154.4895	127.2993	105.9674	89.69855	76.76728	profit * discount rate		
	LTV	1291.746	total present value								

3. What is the maximum amount that Home Alarm could spend on incentives to convert such an existing customer to auto-pay? (6 points)

The difference between the two LTVs calculated in question 1 and 2 is the maximum amount.

The maximum amount is \$293.54. As long as Home Alarm spends less than that amount to convert an existing customer to auto-pay, the LTV of that customer will increase.

	Year 2	Year 3	Year 4	Year 5	Year 6	Year 7	Year 8	Year 9			
revenue	480	494.4	509.232	524.509	540.2442	556.4516	573.1451	590.3395	×	103.00%	
after discount	432	444.96	458.3088	472.0581	486.2198	500.8064	515.8306	531.3055	×	(1-10%)	
cost of service	72	74.16	76.3848	78.67634	81.03663	83.46773	85.97177	88.55092	×	103.00%	
MKT cost	24	24.72	25.4616	26.22545	27.01221	27.82258	28.65726	29.51697	×	103.00%	
profit	336	346.08	356.4624	367.1563	378.171	389.5161	401.2016	413.2376	revenue - cost of service - MKT cost		
probability of being active	93.00%	0.83979	0.753292	0.681729	0.628554	0.585184	55.07%	52.15%	Y(n-1)*(1-attribution rate of year n)		
profit											
expected on average	312.48	290.6345	268.5201	250.3011	237.7009	227.9385	220.9249	215.4923	profit * probability		
discount rate	1.1	1.21	1.331	1.4641	1.61051	1.771561	1.948717	2.143589	1.1^(n-1)		
present value	284.0727	240.1938	201.7432	170.959	147.5936	128.6654	113.3694	100.5288	profit * discount rate		
	LTV	1387.126	total present value								

(Auto-pay with 15% off)

	Year 2	Year 3	Year 4	Year 5	Year 6	Year 7	Year 8	Year 9			
revenue	480	494.4	509.232	524.509	540.2442	556.4516	573.1451	590.3395	×	103.00%	
after discount	408	420.24	432.8472	445.8326	459.2076	472.9838	487.1733	501.7885	×	(1-15%)	
cost of service	72	74.16	76.3848	78.67634	81.03663	83.46773	85.97177	88.55092	×	103.00%	
MKT cost	24	24.72	25.4616	26.22545	27.01221	27.82258	28.65726	29.51697	×	103.00%	
profit	312	321.36	331.0008	340.9308	351.1587	361.6935	372.5443	383.7206	revenue - cost of service - MKT cost		
probability of being active	93.00%	0.83979	0.753292	0.681729	0.628554	0.585184	55.07%	52.15%	$Y(n-1) * (1 - \text{attrition rate of year } n)$		
profit expected on average	290.16	269.8749	249.3401	232.4224	220.7223	211.6572	205.1445	200.1	profit * probability		
discount rate	1.1	1.21	1.331	1.4641	1.61051	1.771561	1.948717	2.143589	$1.1^{(n-1)}$		
present value	263.7818	223.0371	187.3329	158.7476	137.0512	119.475	105.2716	93.34813	profit * discount rate		
	LTV	1288.045	total present value								

(Auto-pay with 14% off)

	Year 2	Year 3	Year 4	Year 5	Year 6	Year 7	Year 8	Year 9			
revenue	480	494.4	509.232	524.509	540.2442	556.4516	573.1451	590.3395	×	103.00%	
after discount	408	420.24	432.8472	445.8326	459.2076	472.9838	487.1733	501.7885	×	(1-15%)	
cost of service	72	74.16	76.3848	78.67634	81.03663	83.46773	85.97177	88.55092	×	103.00%	
MKT cost	24	24.72	25.4616	26.22545	27.01221	27.82258	28.65726	29.51697	×	103.00%	
profit	312	321.36	331.0008	340.9308	351.1587	361.6935	372.5443	383.7206	revenue - cost of service - MKT cost		
probability of being active	93.00%	0.83979	0.753292	0.681729	0.628554	0.585184	55.07%	52.15%	$Y(n-1) * (1 - \text{attrition rate of year } n)$		
profit expected on average	290.16	269.8749	249.3401	232.4224	220.7223	211.6572	205.1445	200.1	profit * probability		
discount rate	1.1	1.21	1.331	1.4641	1.61051	1.771561	1.948717	2.143589	$1.1^{(n-1)}$		
present value	263.7818	223.0371	187.3329	158.7476	137.0512	119.475	105.2716	93.34813	profit * discount rate		
	LTV	1288.045	total present value								