$Individual_assignment 11$

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Prefix

Consider the USArrests data. We will now perform hierarchical clustering on the states.

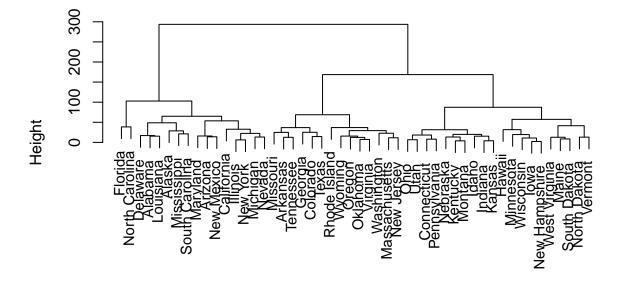
fix(USArrests)

(a)

Using hierarchical clustering with complete linkage and Euclidean distance, cluster the states.

```
hc.complete = hclust(dist(USArrests), method = "complete")
plot(hc.complete,main="Complete Linkage", xlab = "", sub="", cex=0.9)
```

Complete Linkage



(b)

Cut the dendrogram at a height that results in three distinct clusters. Which states belong to which clusters?

cutree(hc.complete,3)

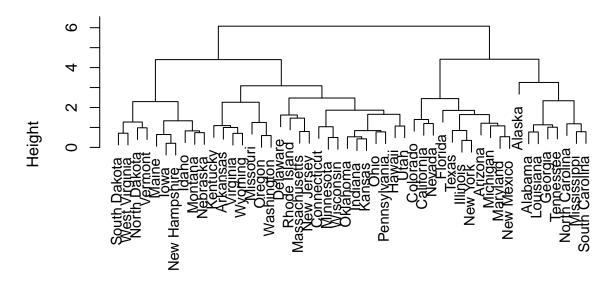
| ## | Alabama | Alaska | Arizona | Arkansas | California |
|----|---------------|-------------|----------------|---------------|----------------|
| ## | 1 | 1 | 1 | 2 | 1 |
| ## | Colorado | Connecticut | Delaware | Florida | Georgia |
| ## | 2 | 3 | 1 | 1 | 2 |
| ## | Hawaii | Idaho | Illinois | Indiana | Iowa |
| ## | 3 | 3 | 1 | 3 | 3 |
| ## | Kansas | Kentucky | Louisiana | Maine | Maryland |
| ## | 3 | 3 | 1 | 3 | 1 |
| ## | Massachusetts | Michigan | Minnesota | Mississippi | Missouri |
| ## | 2 | 1 | 3 | 1 | 2 |
| ## | Montana | Nebraska | Nevada | New Hampshire | New Jersey |
| ## | 3 | 3 | 1 | 3 | 2 |
| ## | New Mexico | New York | North Carolina | North Dakota | Ohio |
| ## | 1 | 1 | 1 | 3 | 3 |
| ## | Oklahoma | Oregon | Pennsylvania | Rhode Island | South Carolina |
| ## | 2 | 2 | 3 | 2 | 1 |
| ## | South Dakota | Tennessee | Texas | Utah | Vermont |
| ## | 3 | 2 | 2 | 3 | 3 |
| ## | Virginia | Washington | West Virginia | Wisconsin | Wyoming |
| ## | 2 | 2 | 3 | 3 | 2 |

(c)

Hierarchically cluster the states using complete linkage and Euclidean distance, after scaling the variables to have standard deviation one.

```
USArrests.sc = scale(USArrests)
hc.complete1 = hclust(dist(USArrests.sc), method = "complete")
plot(hc.complete1,main="Complete Linkage", xlab = "", sub="", cex=0.9)
```

Complete Linkage



(d)

What effect does scaling the variables have on the hierarchical clustering obtained? In your opinion, should the variables be scaled before the inter-observation dissimilarities are computed? Provide a justification for your answer.

cutree(hc.complete1,3)

| ## | Alabama | Alaska | Arizona | Arkansas | California |
|----|---------------|-------------|----------------|---------------|----------------|
| ## | 1 | 1 | 2 | 3 | 2 |
| ## | Colorado | Connecticut | Delaware | Florida | Georgia |
| ## | 2 | 3 | 3 | 2 | 1 |
| ## | Hawaii | Idaho | Illinois | Indiana | Iowa |
| ## | 3 | 3 | 2 | 3 | 3 |
| ## | Kansas | Kentucky | Louisiana | Maine | Maryland |
| ## | 3 | 3 | 1 | 3 | 2 |
| ## | Massachusetts | Michigan | Minnesota | Mississippi | Missouri |
| ## | 3 | 2 | 3 | 1 | 3 |
| ## | Montana | Nebraska | Nevada | New Hampshire | New Jersey |
| ## | 3 | 3 | 2 | 3 | 3 |
| ## | New Mexico | New York | North Carolina | North Dakota | Ohio |
| ## | 2 | 2 | 1 | 3 | 3 |
| ## | Oklahoma | Oregon | Pennsylvania | Rhode Island | South Carolina |
| ## | 3 | 3 | 3 | 3 | 1 |

```
##
     South Dakota
                        Tennessee
                                             Texas
                                                              Utah
                                                                           Vermont
##
                                                 2
                                                                 3
                                                                                  3
                 3
         Virginia
##
                                    West Virginia
                                                         Wisconsin
                                                                           Wyoming
                       Washington
##
                 3
                                 3
                                                                 3
                                                                                  3
```

```
table(cutree(hc.complete,3))
```

```
table(cutree(hc.complete1,3))
```

```
##
## 1 2 3
## 8 11 31
```

Scaling the variables will result in different clusters.

From the summary of this dataset, we know that different variables have different magnitudes. So, I think the variables should be scaled to avoid those variables with bigger magnitude dominating in clustering.

summary(USArrests)

| ## | Murder | Assault | UrbanPop | Rape |
|----|----------------|---------------|---------------|---------------|
| ## | Min. : 0.800 | Min. : 45.0 | Min. :32.00 | Min. : 7.30 |
| ## | 1st Qu.: 4.075 | 1st Qu.:109.0 | 1st Qu.:54.50 | 1st Qu.:15.07 |
| ## | Median : 7.250 | Median :159.0 | Median :66.00 | Median :20.10 |
| ## | Mean : 7.788 | Mean :170.8 | Mean :65.54 | Mean :21.23 |
| ## | 3rd Qu.:11.250 | 3rd Qu.:249.0 | 3rd Qu.:77.75 | 3rd Qu.:26.18 |
| ## | Max. :17.400 | Max. :337.0 | Max. :91.00 | Max. :46.00 |