

第15章作业

[15-6] 图示波形为奇函数, 且具有半波对称性

知 $T=14s$, 令 $\omega_0 T=2\pi$ $\therefore \omega_0=\frac{\pi}{7} \text{ rad/s}$

当 $t=0$ 时 $f(t)=0$ $2 \leq t \leq 4$ 时, $f(t)=\begin{cases} 1, & 2 \leq t \leq 3 \\ 0, & 3 \leq t \leq 4 \\ -1, & 4 \leq t \leq 5 \\ 0, & 5 \leq t \leq 6 \end{cases}$

为奇函数 $\therefore a_k=0$

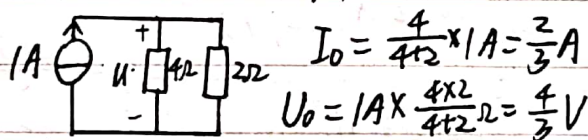
$$b_k = \frac{4}{T} \int_0^T f(t) \sin k\omega_0 t dt$$

$$= \frac{4}{k\omega_0 T} (-\cos k\omega_0 t) \Big|_2^5$$

$$= \frac{2}{k\pi} (\cos \frac{2\pi k}{7} - \cos \frac{5\pi k}{7}) \quad (k=1, 3, 5, \dots)$$

$\therefore f(t) = \frac{2}{\pi} \sum_{k=1,3,5,\dots} \frac{1}{k} (\cos \frac{2\pi k}{7} - \cos \frac{5\pi k}{7}) \sin \frac{\pi k t}{7}$

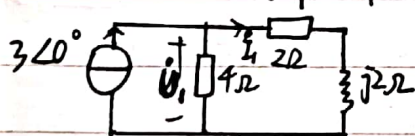
[15-8] ① 直流分量单独作用



$I_0 = \frac{4}{4+2} \times 1A = \frac{2}{3}A$

$U_0 = 1A \times \frac{4 \times 2}{4+2} \Omega = \frac{4}{3}V$

② 基波电源单独作用

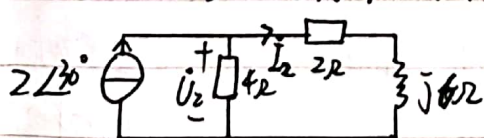


$Z_{eq1} = \frac{4 \times (2+j2)}{6+j2} = (1.6+j0.8)\Omega$

$\dot{U}_1 = 3\angle 0^\circ \times \frac{1.6+j0.8}{1.6+j0.8} = 5.37\angle 26.57^\circ V$

$\dot{I}_1 = 3\angle 0^\circ \times \frac{4}{6+j2} = 1.8-j0.6 = 1.90\angle -18.43^\circ A$

③ 三次谐波电源单独作用



$Z_{eq2} = \frac{4 \times (2+j6)}{6+j6} = (\frac{8}{3}+j\frac{4}{3})\Omega$

$\dot{U}_2 = 2\angle 30^\circ \times \frac{4}{6+j2} = \frac{4+8j}{3} + j\frac{8+4j}{3}$

$= 5.96\angle 56.57^\circ = \frac{8\sqrt{5}}{3}\angle 56.57^\circ V$

$\dot{I}_2 = 2\angle 30^\circ \times \frac{4}{6+j6} = \frac{4\sqrt{3}}{3} + j\frac{4\sqrt{3}}{3}$

$= 0.94\angle -15^\circ A$

$\therefore \dot{i} = [0.67 + 1.90 \cos(t - 18.43^\circ) + 0.94 \sin(3t - 15^\circ)]A$

$u = [1.33 + 5.37 \cos(t + 26.57^\circ) + 5.96 \sin(3t + 56.57^\circ)]A$

(2) $I = \sqrt{I_0^2 + \sum_{k=1}^{\infty} I_k^2} = \sqrt{(\frac{2}{3})^2 + (\frac{1.90}{\sqrt{2}})^2 + (\frac{0.94}{\sqrt{2}})^2}$

$= 1.64A$

$U = \sqrt{U_0^2 + \sum_{k=1}^{\infty} U_k^2} = \sqrt{(\frac{4}{3})^2 + (\frac{5.37}{\sqrt{2}})^2 + (\frac{5.96}{\sqrt{2}})^2}$

$= 5.83V$

(3) $P_0 = (\frac{2}{3})^2 \times 2 = 0.89W$

$P_1 = (\frac{1.9}{\sqrt{2}})^2 \times 2 = 3.61W$

$P_2 = (\frac{0.94}{\sqrt{2}})^2 \times 2 = 0.88W$

$\therefore P = P_0 + P_1 + P_2 = 5.39W$

(4) $P_0' = \frac{4}{3} \times 1 = 1.33W$

$\dot{U}_1' = 3\angle 0^\circ \times (1.6 + j0.8)$

$P_1' = \frac{1}{2} U_1' I_1' \cos(\phi_{U1} - \phi_{I1}) = 7.20W$

$\dot{U}_2' = 2\angle 30^\circ \times (\frac{8}{3} + j\frac{4}{3})$

$P_2' = \frac{1}{2} U_2' I_2' \cos(56.57^\circ - 30^\circ)$

$= 5.33W$

$\therefore P' = P_0' + P_1' + P_2' = 13.86W$

[15-12] ① 知 $T=2\pi \times 10^{-3}s$

知 $\omega_0 T=2\pi$ 则 $\omega_0=1000 \text{ rad/s}$

$\omega_0 L=100\Omega, \frac{1}{\omega_0 C}=2500\Omega$

(2) U_S 为正方形波, 查表知

$f(t) = 5\pi + 20 \sum_{k=1}^{\infty} \frac{1}{2k-1} \sin 1000(2k-1)t$

取前5项, 则

$U_S = [5\pi + 20 \sin 1000t + \frac{20}{3} \sin 3000t + 4 \sin 5000t + \frac{20}{7} \sin 7000t]V$

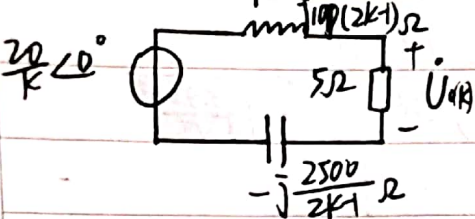
(3) ① 直流分量单独作用下

$U_0 = 0$

→



② K次谐波单独作用下



$$\dot{U}_{(k)} = \frac{20}{k} \angle 0^\circ \times \frac{5}{j100(2k+1) + 5 - j\frac{2500}{2k+1}}$$

$$\therefore k=1 \text{ 时, } \dot{U}_{01} = 20 \angle 0^\circ \times \frac{5}{j100 + 5 - j2500} = 0.042 \angle 89.9^\circ \text{ V}$$

$$k=2 \text{ 时, } \dot{U}_{02} = \frac{20}{2} \angle 0^\circ \times \frac{5}{j300 + 5 - j\frac{2500}{2}} = 0.062 \angle 89.5^\circ \text{ V}$$

$$k=3 \text{ 时, } \dot{U}_{03} = \frac{20}{3} \angle 0^\circ \times \frac{5}{j500 + 5 - j\frac{2500}{3}} = 4 \angle 0^\circ \text{ V (串联谐振)}$$

$$k=4 \text{ 时, } \dot{U}_{04} = \frac{20}{4} \angle 0^\circ \times \frac{5}{j700 + 5 - j\frac{2500}{4}} = 0.042 \angle -89.2^\circ \text{ V}$$

取前5项

$$\therefore u_0 \approx [0.042 \sin(1000t + 89.9^\circ) + 0.062 \sin(3000t + 89.5^\circ) + 4 \sin(5000t + 0.042 \sin(7000t - 89.2^\circ)] \text{ V}$$

$$\text{4) } U_0 = \sqrt{\left(\frac{0.042}{\sqrt{2}}\right)^2 + \left(\frac{0.062}{\sqrt{2}}\right)^2 + \left(\frac{4}{\sqrt{2}}\right)^2 + \left(\frac{0.042}{\sqrt{2}}\right)^2} \approx 2.829 \text{ V}$$

15) 取前5项合适

(带通滤波器, 选择5次谐波分量)

[15-21] \dot{I}_S 单独作用时,



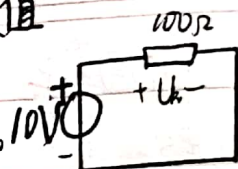
$j100 \Omega$ 电感与 $-j100 \Omega$ 电容并联谐振

$$\therefore U_{k1} = -1 \times 100 \text{ V} = -100 \text{ V}$$

取有效值

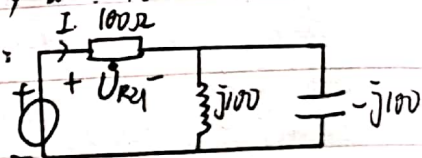
U_S 单独作用时,

① 直流分量单独作用



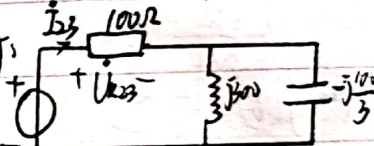
$$U_{k0} = 10 \text{ V}, P_{21} = \frac{10^2}{100} = 1 \text{ W}$$

② 基波单独作用时,



L与C并联谐振 $I=0, \dot{U}_{k1}=0, P_{22}=0$

③ 三次谐波单独作用时,



$$Z_{eq} = \frac{j300 \times (-j\frac{100}{3})}{j300 - j\frac{100}{3}} = -j37.5 \Omega$$

$$\dot{U}_{k3} = 20 \angle 0^\circ \times \frac{100}{100 - j37.5} = (17.53 - j6.58) \text{ V} = 18.72 \angle -20.5^\circ \text{ V}$$

$$\text{由叠加定理, } U_R = \sqrt{10^2 + 10^2 + (18.72)^2} = 102.22 \text{ V}$$

$$\dot{I}_{33} = \frac{20 \angle 0^\circ}{100 - j37.5} = (0.175 + j0.066) \text{ A} = 0.187 \angle 20.66^\circ \text{ A}$$

$$P_{23} = 20 \times 0.187 \cos(0^\circ - 20.66^\circ) = 3.499 \text{ W}$$

$$P = P_{21} + P_{23} = 1 + 3.499 = 4.5 \text{ W}$$

即 U_R 有效值 102.22 V,

U_S 提供的平均功率 4.5 W

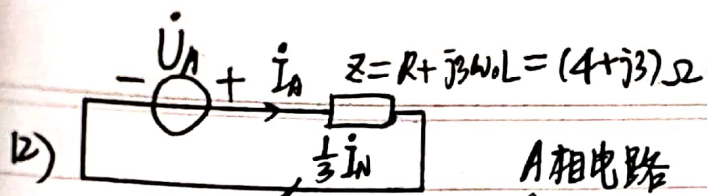
[15-22] 11) 由对称三相非正弦稳态电路零序电压、电流的分布特征知, $Y_N - Y_n$ 联结下, 线电流中含零序分量, 除线电压外, 其他电量均含零序分量。中线电流、中性点之间的电压全是零序分量, 没有正序和负序分量

$x \neq k=1, 7, 13, \dots$ 正序; $k=3, 9, 15, \dots$ 零序;

$k=5, 11, 17, \dots$ 负序

$$\therefore U_{nn} = -U_3 = -120 \sin 3\omega t \text{ V}$$





$$\dot{I}_A = \frac{1}{3} \dot{I}_N = \frac{\dot{U}_A}{Z} = \frac{120 \angle 0^\circ}{4 + j3} = 24 \angle -36.86^\circ \text{ A}$$

$$\therefore \dot{I}_N = 72 \angle -36.86^\circ \text{ A}$$

$$\text{即 } i_N = 72 \sin(3\omega t - 36.86^\circ) \text{ A}$$

(3) 线电压中总没有零序分量, 无论三线制还是

四线制连接. \therefore 上述两种情况下, 均为:

$U_{A1} = 180 \sin \omega t \text{ V}$ 作用时, 正序对称,

$$U_{A1} = 180\sqrt{3} \sin(\omega t + 30^\circ) \text{ V}$$

$U_{A5} = 80 \sin 5\omega t \text{ V}$ 作用时, 负序对称

$$U_{A5} = 80\sqrt{3} \sin(5\omega t - 30^\circ) \text{ V}$$

$$\text{叠加得: } U_{AB} = [180\sqrt{3} \sin(\omega t + 30^\circ) + 80\sqrt{3} \sin(5\omega t - 30^\circ)] \text{ V}$$

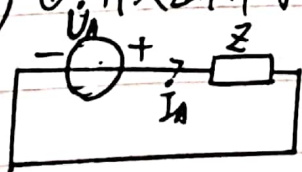
$$\text{同理, } U_{BC} = [180\sqrt{3} \sin(\omega t + 30^\circ - 120^\circ) + 80\sqrt{3} \sin(5\omega t - 30^\circ + 120^\circ)] \text{ V}$$

$$= [180\sqrt{3} \sin(\omega t - 90^\circ) + 80\sqrt{3} \sin(5\omega t + 90^\circ)] \text{ V}$$

$$U_{AC} = [180\sqrt{3} \sin(\omega t + 30^\circ + 120^\circ) + 80\sqrt{3} \sin(5\omega t - 30^\circ - 120^\circ)] \text{ V}$$

$$= [180\sqrt{3} \sin(\omega t + 150^\circ) + 80\sqrt{3} \sin(5\omega t - 150^\circ)] \text{ V}$$

14) ① 开关断开时: 线电流中不含零序分量! (Y-Y 联结)



$$\dot{I}_A = \frac{180 \angle 0^\circ}{4 + j1} = 43.66 \angle -14.04^\circ \text{ A}$$

$$\dot{I}_{A5} = \frac{80 \angle 0^\circ}{4 + j5} = 12.49 \angle -51.34^\circ \text{ A}$$

$$\therefore \dot{I}_A = [43.66 \sin(\omega t - 14.04^\circ) + 12.49 \sin(5\omega t - 51.34^\circ)] \text{ A}$$

② 开关闭合时: Y_N-Y_n 联结, 线电流中含有零序分量

$$\dot{I}_{A3} = \frac{120 \angle 0^\circ}{4 + j3} = 24 \angle -36.86^\circ \text{ A}$$

$$\therefore \dot{I}_A = [43.66 \sin(\omega t - 14.04^\circ) + 24 \sin(3\omega t - 36.86^\circ) + 12.49 \sin(5\omega t - 51.34^\circ)] \text{ A}$$

