

# Modeling Ebola: System, Agent, and Spatial Models

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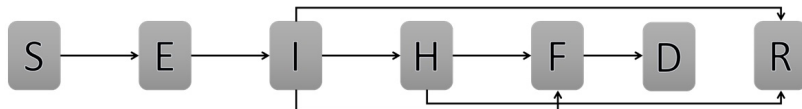
# Overview

- ① Introduction
- ② Models
  - System-based
  - Agent-based
  - Spatial agent-based
- ③ Comparison
- ④ Summary

# Introduction

- Ebola was discovered in 1976
- Early symptoms: headache, fatigue, joint pain
- Later symptoms: abdominal pain, diarrhea, vomiting, rashes
- Diseases like HIV and Malaria have the same symptoms
- The virus is contracted through direct contact with bodily fluids and secretion
- Incubation period may last up to two weeks
- Serious outbreaks in Liberia, Sierra Leone, and Guinea (2014)

# Compartment Model of the Ebola Epidemic in Liberia



S: Susceptible  
E: Exposed  
I: Infectious  
H: Hospitalized  
F: Funeral  
R: Recovered  
D: Dead

# Assumptions

- Focus on Liberia in 2014-2015
- Closed system
- Everyone who dies has a traditional funeral

# System Dynamics Differential Equations

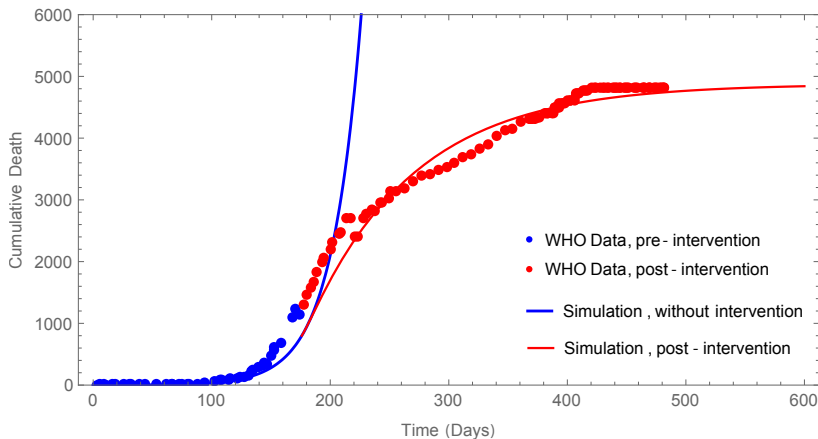
$$\begin{aligned}\frac{dS}{dt} &= -\frac{\beta_I SI + \beta_H SH + \beta_F SF}{N} \\ \frac{dE}{dt} &= \frac{\beta_I SI + \beta_H SH + \beta_F SF}{N} - \gamma_P E \\ \frac{dI}{dt} &= \gamma_P E - [\gamma_H \theta + \gamma_I(1 - \theta)(1 - \delta_1) + \gamma_D(1 - \theta)\delta_1]I \\ \frac{dH}{dt} &= \gamma_H \theta I - [\gamma_{HF}\delta_2 + \gamma_{IH}(1 - \delta_2)]H \\ \frac{dF}{dt} &= \gamma_D(1 - \theta)\delta_1 I + \gamma_{DH}\delta_2 H - \gamma_F F \\ \frac{dR}{dt} &= \gamma_I(1 - \theta)(1 - \delta_1)I + \gamma_{HR}(1 - \delta_2)H \\ \frac{dD}{dt} &= \gamma_F F\end{aligned}$$

# Model Parameters for Ebola Epidemic in Liberia

| Parameter   | Value      |
|---|------------|
| Incubation Period ( $t_P$ )                       | 11 days    |
| Duration of Traditional Funeral ( $t_F$ )         | 2.00 days  |
| Time from Infection to Recovery ( $t_I$ )         | 10.00 days |
| Time from Infection to Death ( $t_D$ )            | 8.00 days  |
| Case Fatality Rate, Unhospitalized ( $\delta_1$ ) | 0.500      |
| Case Fatality Rate, Hospitalized ( $\delta_2$ )   | 0.500      |

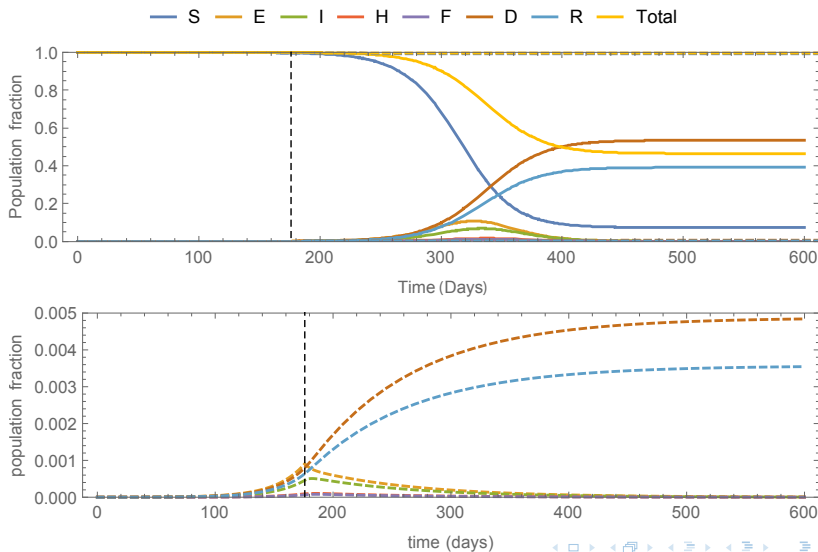
| Parameter  | Pre-intervention<br>(Mar 2014 to Sept 2014) | Post-intervention<br>(Sept 2014 to July 2015) |
|--|---|---|
| Contact Rate, Community ( $\beta_I$ )            | 0.148 (0.0953)                              | 0.0446 (0.0338)                               |
| Contact Rate, Hospital ( $\beta_H$ )             | 0.235 (0.143)                               | 0.0877 (0.0563)                               |
| Contact Rate, Funeral ( $\beta_F$ )              | 0.465 (0.287)                               | 0.283 (0.208)                                 |
| Time from Infection to Hospitalization ( $t_H$ ) | 4.49 (1.44) days                            | 4.63 (1.43) days                              |
| Probability a Case is Hospitalized ( $\theta$ )  | 0.248 (0.142)                               | 0.233 (0.145)                                 |

# World Health Organization Data vs. Systems Model





# System Model Results: With and Without Intervention

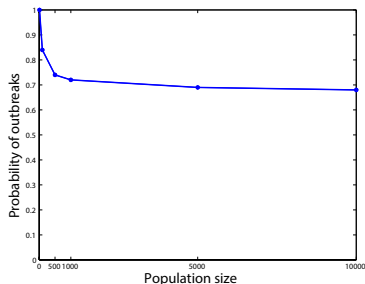
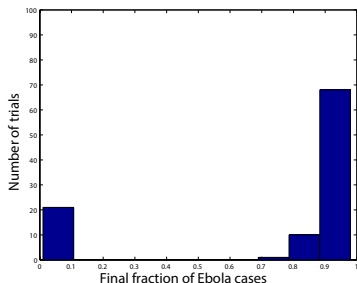


# Agent-based model

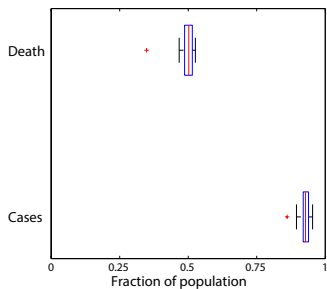
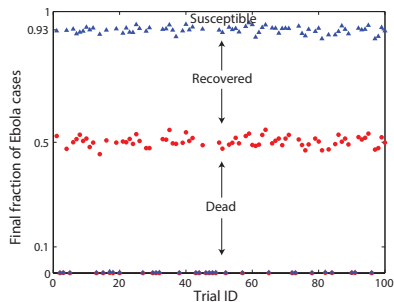
- System  $\implies$  agent
- Compartment  $\implies$  state
- Deterministic  $\implies$  probabilistic
- Simulation:
  - 1000 individuals; 1 exposed
  - 300 days
  - 100 repetitions

# Probability of having an outbreak

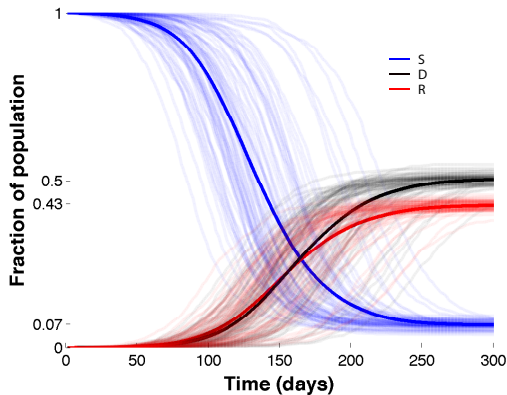
outbreak: 2% of population contracts disease



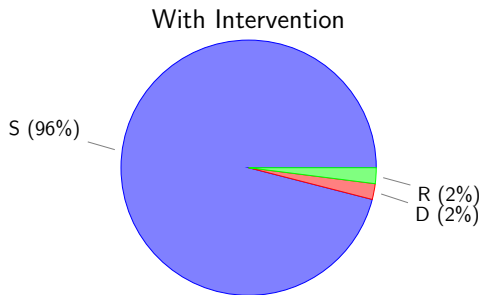
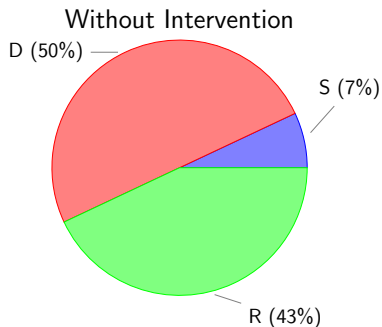
# Effects of Ebola outbreak



# Trajectories of S, D and R

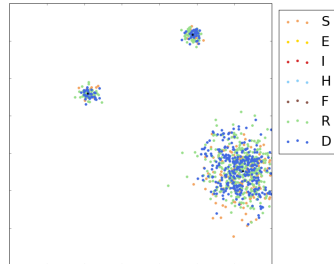


# Results of Intervention



# Spatial Agent-Based Model: Overview

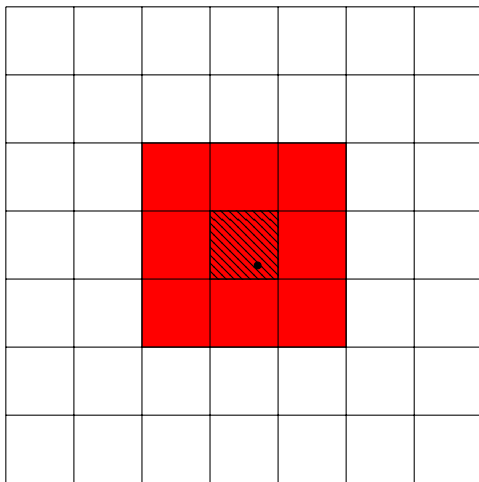
- Importance of incorporating the spatial information
  - Distinct contact rates within households, communities and funerals
  - Different travel patterns for cities and villages
- Initialization: an example
- Regions of infection spread
- Available travel routes
- Differences:
  - Hospitalized people are quarantined
  - Transition time between states



# An Example for SBAM



# Regions of Infection Spread



funeralized



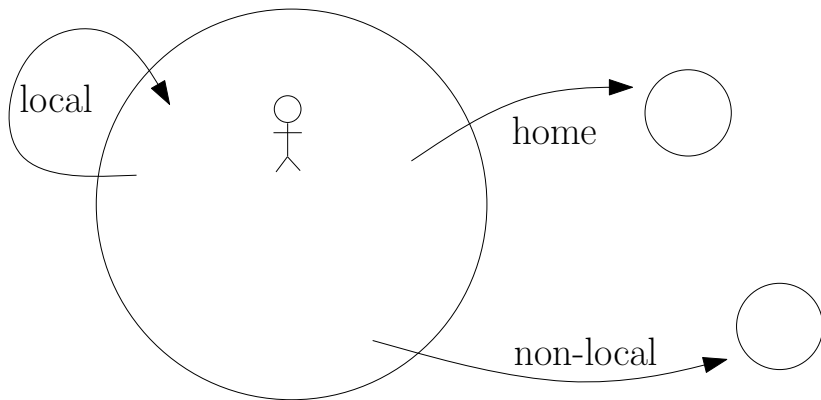
infected



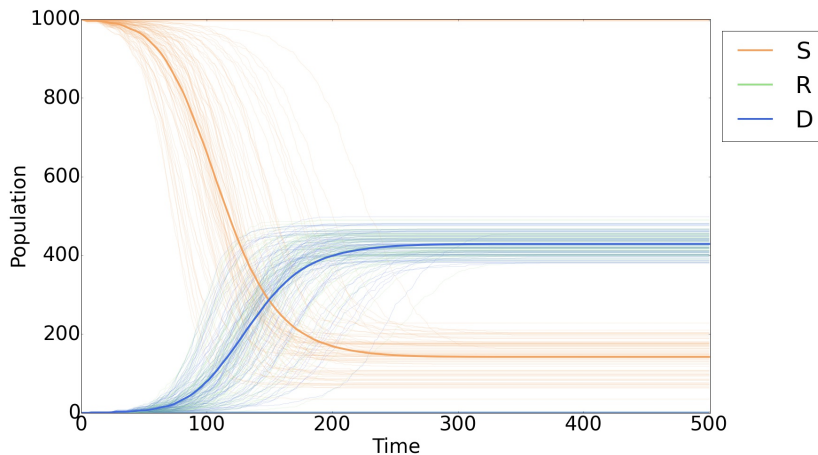
individual

# Available Travel Routes

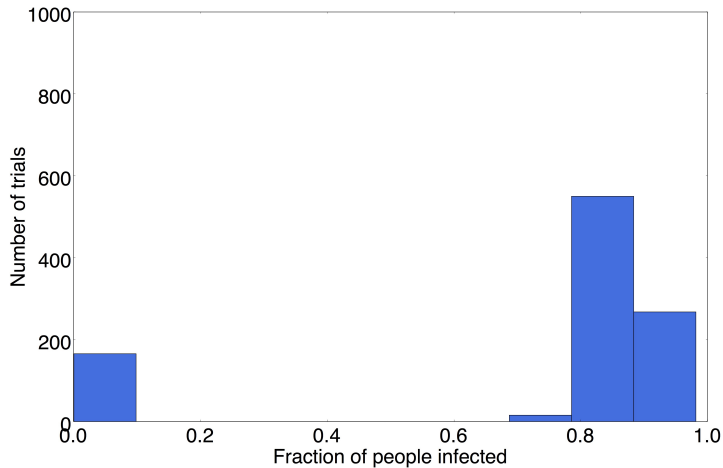
if he travels...



# Trajectories of S, R, D: 100 simulations



# Probability of an Outbreak



# Summary

- Deterministic and probabilistic approaches give similar results
- Incorporating spatial information is useful
- Intervention has a big effect:
  - Over 90 percent contract the disease
  - About 50 percent dies due to disease
  - Intervention causes these figures to decrease significantly