

Binary Search II

Find Local Minimum (Medium)

Given an unsorted integer array, return any of the local minimum's index.

An element at index i is defined as local minimum when it is smaller than all its possible two neighbors $a[i - 1]$ and $a[i + 1]$

(you can think $a[-1] = +\infty$, and $a[a.length] = +\infty$)

Assumptions:

- The given array is not null or empty.
- There are no duplicate elements in the array.
- There is always one and only one result for each case.

```
// return an index of local minimum
int localMin(vector<int>& arr){
    if(arr.empty())
        return -1;
    int left = 0;
    int right = arr.size() - 1;
    while(left <= right){
        int mid = left + (right - left) / 2;
        if((mid == 0 || arr[mid - 1] > arr[mid]) && (mid == arr.size()-1 ||
arr[mid] < arr[mid + 1]))
            return mid;
        else if(mid > 0 && arr[mid] > arr[mid - 1])
            right = mid - 1;
        else
            left = mid + 1;
    }
}
```

Time Complexity: $O(\log n)$, same as binary search.

Search In Shifted Sorted Array I(Medium)

Given a target integer T and an integer array A, A is sorted in ascending order first, then shifted by an arbitrary number of positions.

For Example, A = {3, 4, 5, 1, 2} (shifted left by 2 positions). Find the index i such that A[i] == T or return -1 if there is no such index.

Assumptions

- There are no duplicate elements in the array.

Examples

- A = {3, 4, 5, 1, 2}, T = 4, return 1
- A = {1, 2, 3, 4, 5}, T = 4, return 3
- A = {3, 5, 6, 1, 2}, T = 4, return -1

Corner Cases

- What if A is null or A is of zero length? We should return -1 in this case.

```
// search an element in a sorted array using binary search
int search(vector<int>& arr, int target){
    if(arr.empty())
        return -1;
    int left = 0;
    int right = arr.size() - 1;
    while(left <= right){
        int mid = left + (right - left) / 2;
        if(arr[mid] == target)
            return mid;
        else if(arr[mid] >= arr[left]){ // mid is on the left side of tuning point
            if(target >= arr[left] && target < arr[mid])
                right = mid - 1;
            else
                left = mid + 1;
        }
        else{ // mid is on the right side of tuning point
            if(target <= arr[right] && target > arr[mid])
                left = mid + 1;
            else
                right = mid - 1;
        }
    }
    return -1;
}
```

Time Complexity: O(logn), same as binary search.

K Closest In Sorted Array (Medium)

Given a target integer T , a non-negative integer K and an integer array A sorted in ascending order, find the K closest numbers to T in A .

Assumptions

- A is not null
- K is guaranteed to be ≥ 0 and K is guaranteed to be $\leq A.length$

Return

- A size K integer array containing the K closest numbers(not indices) in A , sorted in ascending order by the difference between the number and T .

Examples

- $A = \{1, 2, 3\}$, $T = 2$, $K = 3$, return $\{2, 1, 3\}$ or $\{2, 3, 1\}$
- $A = \{1, 4, 6, 8\}$, $T = 3$, $K = 3$, return $\{4, 1, 6\}$

```
// Find closest element to integer target in array arr using binary search
// Same code in homework 2
int findClosest(vector<int>& arr, int target){
    if(arr.empty())
        return -1;
    int left = 0;
    int right = arr.size() - 1;
    while(left < right - 1){
        int mid = left + (right - left) / 2;
        if(arr[mid] == target)
            return mid;
        else if(arr[mid] < target)
            left = mid;
        else
            right = mid;
    }
    // post-processing
    if(abs(arr[left] - target) <= abs(arr[right] - target))
        return left;
    else
        return right;
}

vector<int> findClosestElements(vector<int>& arr, int k, int target) {
    int n = arr.size() - 1;
    if(target <= arr[0])
        return vector<int> (arr.begin(), arr.begin() + k);
```

```

else if(target >= arr[n])
    return vector<int> (arr.end() - k, arr.end());
int index = findClosest(arr, target);
int left = max(0, index - k + 1);
int right = min(n, index + k - 1);
while(right - left + 1 > k){
    if(abs(arr[left] - target) <= abs(arr[right] - target))
        right--;
    else
        left++;
}
return vector<int> (arr.begin() + left, arr.begin() + right + 1);
}

```

Time Complexity: $O(\log n)$ for function `findClosest()`, $O(2k)$ for the rest part of function `findClosestElements`. Overall, it takes $O(\log n + k)$.

Array

2 Sum Closest (Medium)

Find the pair of elements in a given array that sum to a value that is closest to the given target number. Return the values of the two numbers.

Assumptions

- The given array is not null and has length of at least 2

Examples

- $A = \{1, 4, 7, 13\}$, target = 7, closest pair is $1 + 7 = 8$, return [1, 7].

```
// same code in homework2
int partition(vector<int>& arr, int left, int right){
    int i = left;
    int j = right - 1;
    int& pivot = arr[right];
    while(i<=j){
        if(arr[i] < pivot)
            i++;
        else{
            swap(arr[i], arr[j]);
            j--;
        }
    }
    swap(arr[i], pivot);
    return i;
}

void quickSort(vector<int>& arr, int left, int right){
    if(left < right) {
        int pos = partition(arr, left, right);
        quickSort(arr, left, pos - 1);
        quickSort(arr, pos + 1, right);
    }
}

// Find the pair of elements in arr that sum to a value that is closest to target
vector<int> twoSumClosest(vector<int>& arr, int target){
    vector<int> result;
    int n = arr.size() - 1;
    // sort the array arr using quick sort
    quickSort(arr, 0, n);
    int left = 0, right = n;
```

```

while(left < right - 1){
    int sum = arr[left] + arr[right];
    if(sum > target) {
        if(abs(sum - target) < abs(arr[left] + arr[right - 1] - target))
            break;
        right--;
    }
    else {
        if(abs(sum - target) < abs(arr[left + 1] + arr[right] - target))
            break;
        left++;
    }
}
result.push_back(arr[left]);
result.push_back(arr[right]);
return result;
}

```

Time Complexity: $O(n \log n)$ for quick sort, $O(n)$ for the rest part of function `twoSumClosest()`. Overall, it takes $O(n \log n)$.

2 Sum Smaller (Medium)

Determine the number of pairs of elements in a given array that sum to a value smaller than the given target number.

Assumptions

- The given array is not null and has length of at least 2

Examples

- $A = \{1, 2, 2, 4, 7\}$, target = 7, number of pairs is 6($\{1, 2\}$, $\{1, 2\}$, $\{1, 4\}$, $\{2, 2\}$, $\{2, 4\}$, $\{2, 4\}$)

```
int twoSumSmaller(vector<int>& arr, int target){
    int n = arr.size() - 1;
    // sort the array arr using quick sort
    quickSort(arr, 0, n);
    int left = 0, right = n;
    int count = 0;
    while(left < right){
        int sum = arr[left] + arr[right];
        if(sum < target){
            count += (right - left);
            left++;
        }
        else
            right--;
    }
    return count;
}
```

Time Complexity: $O(n \log n)$ for quick sort, $O(n)$ for the rest part of function twoSumSmaller(). Overall, it takes $O(n \log n)$.