SP-Jan-23

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```
library(stringr)
library(tidyverse)
## -- Attaching packages ---
                                                       ----- tidyverse 1.3.2 --
## v ggplot2 3.4.0 v purrr 1.0.0

## v tibble 3.1.8 v dplyr 1.0.10

## v tidyr 1.2.1 v forcats 0.5.2
## v readr
            2.1.3
## -- Conflicts -----
                                           ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                     masks stats::lag()
data<-read.csv(file = "A1_Bond_data.csv", header = T)</pre>
data_23 <- data %>%
  select(name, Coupon, days, c_since_days, c_next_days, Jan_23)
data_23<- data_23%>%
  mutate(dirty_price = ((c_since_days + 7)/365)*100*Coupon + Jan_23,
         FV=100 + 0.5*100*Coupon)
c_0 = 0.5*data_23$Coupon[1]*100
t_0 = (data_23$days[1] -7) /365
r_0 = (-\log(data_23\$dirty_price[1]/data_23\$FV[1]))/t_0
print(r_0)
## [1] 0.04259156
c_0.5 = 0.5*data_23$Coupon[2]*100
t_{sp} = (data_{23}c_{next_days}[2]-7) / 365
t_0.5 = (data_23$days[2]-7)/365
ct_0.5 = c_0.5*exp(-r_0*t_sp)
r_0.4 = -(\log((data_23\$dirty_price[2] - ct_0.5)/data_23\$FV[2])/(t_0.5))
k=(r_0 - r_0.4)/(t_0 - t_0.5)
b = r_0 - k*t_0
r_0.5 = k*(t_0 + 0.5) + b
print(r 0.5)
## [1] 0.04468829
c 1 = 0.5*data 23$Coupon[3]*100
ct_1 = c_1*(exp(-r_0*t_0)+exp(-r_0.5*(t_0+0.5)))
r_1 = -(\log((data_23\$dirty_price[3] - ct_1)/data_23\$FV[3])/(t_0+1))
print(r_1)
```

```
## [1] 0.04220127
  c_{1.5} = 0.5*data_{23}Coupon[4]*100
 ct_1.5 = c_1.5*(exp(-r_0*t_0)+exp(-r_0.5*(t_0+0.5))+exp(-r_1*(t_0+1)))
 r_1.5 = -(\log((data_23\$dirty_price[4] - ct_1.5)/data_23\$FV[4])/(t_0+1.5))
 print(r_1.5)
 ## [1] 0.03801979
 c_2 = 0.5*data_23$Coupon[5]*100
 \mathtt{ct}_2 = \mathtt{c}_2 * (\exp(-\mathtt{r}_0 * \mathtt{t}_0) + \exp(-\mathtt{r}_0 . 5 * (\mathtt{t}_0 + 0.5)) + \exp(-\mathtt{r}_1 * (\mathtt{t}_0 + 1)) + \exp(-\mathtt{r}_1 . 5 * (\mathtt{t}_0 + 1.5)))
r_2 = -(\log((data_23\$dirty_price[5] - ct_2)/data_23\$FV[5])/(t_0+2))
 print(r 2)
 ## [1] 0.03516355
 c 2.5 = 0.5*data 23$Coupon[6]*100
 \mathtt{ct}_2.5 = \mathtt{c}_2.5 * (\exp(-\mathtt{r}_0 * \mathtt{t}_0) + \exp(-\mathtt{r}_0.5 * (\mathtt{t}_0 + 0.5)) + \exp(-\mathtt{r}_1 * (\mathtt{t}_0 + 1)) + \exp(-\mathtt{r}_1.5 * (\mathtt{t}_0 + 1.5)) + \exp(-\mathtt{r}_2 * (\mathtt{t}_0 + 0.5)) + \exp(-\mathtt{r}_1.5 * (\mathtt{t}_
 r_2.5 = -(\log((data_23\$dirty_price[6] - ct_2.5)/data_23\$FV[6])/(t_0+2.5))
 print(r_2.5)
 ## [1] 0.03377027
 c_3 = 0.5*data_23$Coupon[7]*100
 \mathtt{ct\_3} = \mathtt{c\_3*(exp(-r\_0*t\_0)+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_1*(t\_0+1))+exp(-r\_1.5*(t\_0+1.5))+exp(-r\_2*(t\_0+2.5))}
 r_3 = -(\log((data_23*dirty_price[7] - ct_3)/data_23*FV[7])/(t_0+3))
 print(r_3)
 ## [1] 0.03217936
 c_{3.5} = 0.5*data_{23}Coupon[8]*100
 \mathtt{ct\_3.5} = \mathtt{c\_3.5} * (\exp(-\mathtt{r\_0} * \mathtt{t\_0}) + \exp(-\mathtt{r\_0.5} * (\mathtt{t\_0} + 0.5)) + \exp(-\mathtt{r\_1} * (\mathtt{t\_0} + 1)) + \exp(-\mathtt{r\_1.5} * (\mathtt{t\_0} + 1.5)) + \exp(-\mathtt{r\_2} * (\mathtt{t\_0} + 0.5)) + \exp(-\mathtt{r\_1.5} * (\mathtt{t\_0
 r_3.5 = -(log((data_23$dirty_price[8] - ct_3.5)/data_23$FV[8])/(t_0+3.5))
 print(r_3.5)
 ## [1] 0.03067967
 c_4 = 0.5*data_23$Coupon[9]*100
 \mathtt{ct\_4} = \mathtt{c\_4*(exp(-r\_0*t\_0)+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_1*(t\_0+1))+exp(-r\_1.5*(t\_0+1.5))+exp(-r\_2*(t\_0+2.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r\_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t\_0+0.5))+exp(-r_0.5*(t_0-0.5))+exp(-r_0.5*(t_0-0.5))+exp(-r_0.5*(t_0-0.5))+exp(-r_0.5*(t_0-0.5))+exp(-r_0.5*(t_0-0.5))+exp(-r_0.5*(t_0-0.5))+exp(-r_0.5*(t_0-0.5))+exp(-r_0.5*(t_0-0.5))+exp(-r_0.5*(t_0-0
 r_4 = -(\log((data_23\$dirty_price[9] - ct_4)/data_23\$FV[9])/(t_0+4))
 print(r_4)
 ## [1] 0.02957791
 c_{4.5} = 0.5*data_{23}Coupon[10]*100
 \mathtt{ct\_4.5} = \mathtt{c\_4.5} * (\exp(-\mathtt{r\_0} * \mathtt{t\_0}) + \exp(-\mathtt{r\_0.5} * (\mathtt{t\_0} + 0.5)) + \exp(-\mathtt{r\_1} * (\mathtt{t\_0} + 1)) + \exp(-\mathtt{r\_1.5} * (\mathtt{t\_0} + 1.5)) + \exp(-\mathtt{r\_2} * (\mathtt{t\_0} + 0.5)) + \exp(-\mathtt{r\_1} * (\mathtt{t
 r_{4.5} = -(\log((data_23\$dirty_price[10] - ct_{4.5})/data_23\$FV[10])/(t_0+4.5))
 print(r_4.5)
 ## [1] 0.02907397
 c_5 = 0.5*data_23$Coupon[11]*100
 \mathtt{ct\_5} = \mathtt{c\_5*(exp(-r\_0*t\_0) + exp(-r\_0.5*(t\_0+0.5)) + exp(-r\_1*(t\_0+1)) + exp(-r\_1.5*(t\_0+1.5)) + exp(-r\_2*(t\_0+2.5)) + exp(-r\_0.5*(t\_0+0.5)) + e
 r_5 = -(\log((data_23\$dirty_price[11] - ct_5)/data_23\$FV[11])/(t_0+5))
print(r_5)
 ## [1] 0.0287096
```