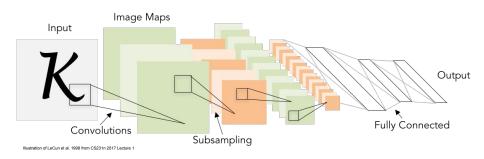
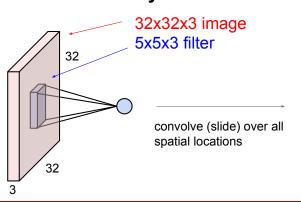
### Topic 14: TRAINING NEURAL NETWORKS

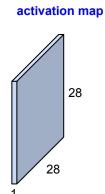
CMSC 35400/STAT 37710 Machine Learning Risi Kondor, The University of Chicago

### **Convolutional Neural Networks**



### **Convolutional Layer**



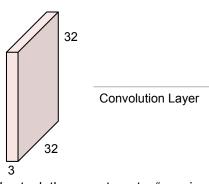


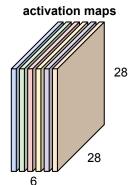
Fei-Fei Li & Justin Johnson & Serena Yeung

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For example, if we had 6 5x5 filters, we'll get 6 separate activation maps:

### **Convolutional Layer**

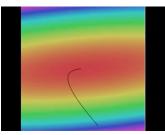




We stack these up to get a "new image" of size 28x28x6!

### Learning network parameters through optimization





```
# Vanilla Gradient Descent

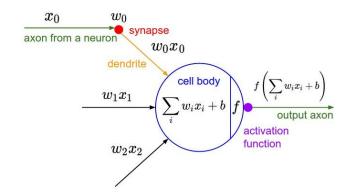
while True:
    weights_grad = evaluate_gradient(loss_fun, data, weights)
    weights += - step_size * weights_grad # perform parameter update
```

Landscape image is <u>CC0 1.0</u> public domain <u>Walking man image i</u>s <u>CC0 1.0</u> public domain

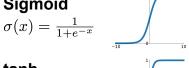
## Mini-batch SGD

### Loop:

- 1. Sample a batch of data
- 2. **Forward** prop it through the graph (network), get loss
- 3. **Backprop** to calculate the gradients
- 4. Update the parameters using the gradient



# Sigmoid

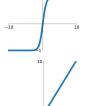


#### tanh

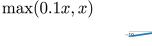
tanh(x)

# ReLU

 $\max(0,x)$ 



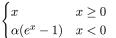
# Leaky ReLU



### Maxout

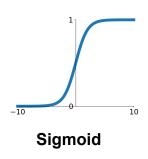
 $\max(w_1^T x + b_1, w_2^T x + b_2)$ 

### ELU



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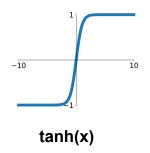


$$\sigma(x) = 1/(1 + e^{-x})$$

- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating "firing rate" of a neuron

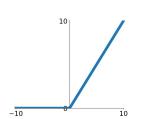
#### 3 problems:

 Saturated neurons "kill" the gradients



- Squashes numbers to range [-1,1]
- zero centered (nice)
- still kills gradients when saturated :(

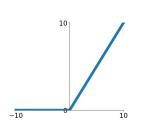
[LeCun et al., 1991]



**ReLU** (Rectified Linear Unit)

- Computes f(x) = max(0,x)
  - Does not saturate (in +region)
- Very computationally efficient
- Converges much faster than sigmoid/tanh in practice (e.g. 6x)
- Actually more biologically plausible than sigmoid

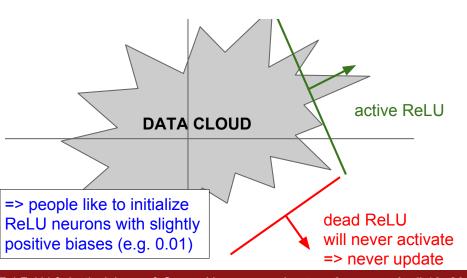
[Krizhevsky et al., 2012]



**ReLU** (Rectified Linear Unit)

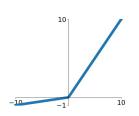
- Computes f(x) = max(0,x)
  - Does not saturate (in +region)
- Very computationally efficient
- Converges much faster than sigmoid/tanh in practice (e.g. 6x)
- Actually more biologically plausible than sigmoid
- Not zero-centered output
- An annoyance:

hint: what is the gradient when x < 0?



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[Mass et al., 2013] [He et al., 2015]

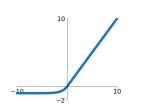
- Does not saturate
- Computationally efficient
- Converges much faster than sigmoid/tanh in practice! (e.g. 6x)
- will not "die".

### Leaky ReLU

$$f(x) = \max(0.01x, x)$$

[Clevert et al., 2015]

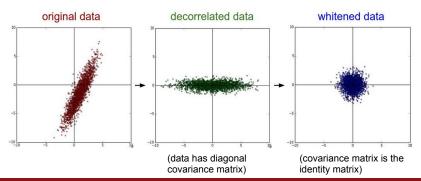
### **Exponential Linear Units (ELU)**



- All benefits of ReLU
- Closer to zero mean outputs
- Negative saturation regime compared with Leaky ReLU adds some robustness to noise
- $f(x) = \begin{cases} x & \text{if } x > 0 \\ \alpha (\exp(x) 1) & \text{if } x \le 0 \end{cases}$
- Computation requires exp()

### Step 1: Preprocess the data

In practice, you may also see PCA and Whitening of the data



First idea: Small random numbers
 (gaussian with zero mean and 1e-2 standard deviation)

$$W = 0.01* \text{ np.random.randn(D,H)}$$

Works ~okay for small networks, but problems with deeper networks.

"you want zero-mean unit-variance activations? just make them so."

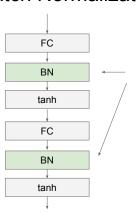
consider a batch of activations at some layer. To make each dimension zero-mean unit-variance, apply:

$$\widehat{x}^{(k)} = \frac{x^{(k)} - \mathbb{E}[x^{(k)}]}{\sqrt{\text{Var}[x^{(k)}]}}$$

this is a vanilla differentiable function...

### **Batch Normalization**

[loffe and Szegedy, 2015]



Usually inserted after Fully Connected or Convolutional layers, and before nonlinearity.

$$\widehat{x}^{(k)} = \frac{x^{(k)} - E[x^{(k)}]}{\sqrt{\text{Var}[x^{(k)}]}}$$

### **Batch Normalization**

### [loffe and Szegedy, 2015]

**Input:** Values of x over a mini-batch:  $\mathcal{B} = \{x_{1...m}\}$ ; Parameters to be learned:  $\gamma$ ,  $\beta$ 

Output:  $\{y_i = BN_{\gamma,\beta}(x_i)\}$ 

 $\hat{x}_i \leftarrow \frac{x_i - \mu_B}{\sqrt{\sigma_a^2 + \epsilon}}$ 

 $y_i \leftarrow \gamma \widehat{x}_i + \beta \equiv BN_{\gamma,\beta}(x_i)$ 

$$\mu_{\mathcal{B}} \leftarrow \frac{1}{m} \sum_{i=1}^m x_i$$
 // mini-batch mean 
$$\sigma_{\mathcal{B}}^2 \leftarrow \frac{1}{m} \sum_{i=1}^m (x_i - \mu_{\mathcal{B}})^2$$
 // mini-batch variance

// normalize

# Note: at test time BatchNorm layer functions differently:

The mean/std are not computed based on the batch. Instead, a single fixed empirical mean of activations during training is used.

(e.g. can be estimated during training with running averages)

### Hyperparameters to play with:

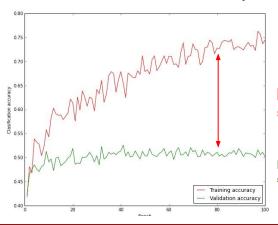
- network architecture
- learning rate, its decay schedule, update type
- regularization (L2/Dropout strength)

neural networks practitioner music = loss function



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### Monitor and visualize the accuracy:



#### big gap = overfitting

=> increase regularization strength

### no gap

=> increase model capacity?