

User manual for LIME

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Quantum dynamics

1.1 Adiabatic Nuclear Quantum Dynamics

CHAPTER 1. QUANTUM DYNAMICS 1.1. ADIABATIC NUCLEAR
QUANTUM DYNAMICS

Exact methods:

1.1.1 Split-operator method

Discrete variable representation Semiclassical methods:

1.1.2 Quantum trajectory method

b. Non-adiabatic molecular dynamics

Exact nonadiabatic quantum dynamic with multiple electronic surfaces.

Split-operator method in the diabatic representation Mixed quantum-classical methods

Surface-hopping method

1.1.3 Discrete Variable Representation

Consider a finite basis set $|\varphi_j\rangle, j = 0, 1, \dots, n-1$. The usual spectral method amounts to constructing the kinetic energy operator \hat{T} and potential energy operator $V(x)$,

$$V_{jk} = \int dx \varphi_j^*(x) V(x) \varphi_k(x). \quad (1.1)$$

Orthogonal polynomials

For a given range $x \in [a, b]$, and for a weight function $w(x)$, the orthogonal polynomials, we want to require

$$\int_a^b dx w(x) p_m(x) p_n(x) = \delta_{mn} \quad (1.2)$$

where $p_n(x)$ is n -degree polynomial. Several orthogonal polynomials for different ranges are known.

If we have a OP, then we can construct basis set

$$\phi_n(x) = \sqrt{w(x)} p_n(x) \quad (1.3)$$

We can apply Gaussian quadrature $\{x_\alpha, w_\alpha\}, \alpha = 1, \dots, N$ for the integration

$$\delta_{mn} = \int_a^b dx \phi_m^*(x) \phi_n(x) = \sum_\alpha \frac{w_\alpha}{w(x_\alpha)} \phi_m^*(x_\alpha) \phi_n(x_\alpha) \quad (1.4)$$

we also have

$$X_{mn} = \sum_\alpha w_\alpha \frac{\phi_m^*(x_\alpha) x_\alpha \phi_n(x_\alpha)}{w(x_\alpha)} \quad (1.5)$$

define $U_{\alpha j} = \sqrt{\frac{w_\alpha}{w(x_\alpha)}} \phi_j(x_\alpha)$, U is the unitary from Eq. (1.4). From Eq. (1.5), it leads to

$$\mathbf{U} \mathbf{X} \mathbf{U}^\dagger = \mathbf{X}^{\text{DVR}} \quad (1.6)$$

Thus, the quadrature points can be determined by the diagonalizing the coordinate matrix elements. The eigenstates reads

$$\varphi_\alpha(x) = \sum_j U_{\alpha j}^* \phi_j(x) \quad (1.7)$$

Vibronic model

How do we diagonalize a vibronic Hamiltonian in adiabatic representation?

$$H_M = T_n + H_{\text{BO}}(\mathbf{R}) \quad (1.8)$$

The basis set is $|\alpha(\mathbf{R}), \mathbf{R}\rangle$ where $\alpha(\mathbf{R})$ is the adiabatic electronic states. to construct the Hamiltonian matrix elements

$$\langle \beta(\mathbf{R}'), \mathbf{R}' | H | \alpha(\mathbf{R}), \mathbf{R} \rangle = \quad (1.9)$$

Quantum chemistry

Quantum chemistry solves the electronic structure given the nuclear geometry. This has been an active field of research for many decades, and sophisticated programs like Gaussian, Qchem, Psi4, Pyscf, Molpro have been widely used in the scientific community. We will take advantage of these remarkable developments. On one hand, we will apply existing methods to interesting molecules and materials. On the other hand, we will develop new techniques based on these programs as well since many functions and modules such as Coulomb integrals are the same irrespective of what your method is.

Currently, we primarily use Pyscf and Molpro for Quantum Chemistry computations.

3. Polaritonic dynamics Quantum dynamics of molecules coupled to the electromagnetic photon modes confined inside an optical cavity.

4. Stochastic Schrödinger equation Generate white and colored noise to simulate stochastic dynamics, e.g., stochastic Schrödinger equations.

5. Band structure of solids Compute band structure from tight-binding Hamiltonians.

Open quantum systems

Quantum systems are rarely isolated from their surrounding environment. For an isolated quantum system, dynamics can be described by the time-dependent Schrödinger equation (TDSE). One straightforward approach simulating the open quantum system dynamics is to include the environment degrees of freedom directly into the TDSE. While conceptually simple, this is not always the optimal choice when the environment is complex. Alternatively, we can solve a quantum master equation describing the equation of motion for the reduced density matrix.

Assuming the system-bath Hamiltonian reads

$$H_{\text{SB}} = \sum_{\alpha} A_{\alpha} B_{\alpha} \quad (3.1)$$

The following methods are currently implemented.

3.1 Redfield equations

CHAPTER 3. OPEN QUANTUM SYSTEMS 3.1. REDFIELD EQUATIONS

3.2 Lindblad quantum master equations

CHAPTER 3. OPEN QUANTUM SYSTEMS 3.2. LINDBLAD QUANTUM MASTER EQUATIONS

3.3 Hierarchical equation of motion

CHAPTER 3. OPEN QUANTUM SYSTEMS 3.3. HIERARCHICAL EQUATION OF MOTION

3.4 second-order time-convolutionless equation

CHAPTER 3. OPEN QUANTUM SYSTEMS3.4. SECOND-ORDER
TIME-CONVOLUTIONLESS EQUATION

CHAPTER 4. PERIODICALLY DRIVEN QUANTUM
SYSTEMS

Chapter 4

Periodically driven quantum systems

Quasienergy levels of a periodically driven quantum system using Floquet theorem

Nonlinear molecular spectroscopy

Time-independent approach to optical signals via sum-over-states expressions
Absorption

5.1 Transient absorption spectroscopy

CHAPTER 5. NONLINEAR MOLECULAR SPECTROSCOPY 5.1.
TRANSIENT ABSORPTION SPECTROSCOPY

Photo echo Time-dependent approach to coherent signals via explicitly solving the dynamics of matter interacting with laser pulses employed in the spectroscopic experiment. For example, pump and probe pulses in pump-probe experiments.

5.2 Transient absorption

CHAPTER 5. NONLINEAR MOLECULAR SPECTROSCOPY 5.2.
TRANSIENT ABSORPTION

Quantum transport

This module is to compute the current of nano-structures under a finite bias using the non-equilibrium Green's function (NEGF) method.

6.1 NEGF for time-independent transport

CHAPTER 6. QUANTUM TRANSPORT 6.1. NEGF FOR TIME-INDEPENDENT TRANSPORT

Uncategorized

7.1 Schmdit decomposition

CHAPTER 7. UNCATEGORIZED7.1. SCHMDIT DECOMPOSITION

