

# Theory of Computation Homework 1

313782 Gregory Richard

324944 Damian Kopp

350510 Kim Yujun

March 2022

## Problem 1

We take  $\langle G, k \rangle$  in *CLIQUE*. Then, take a function  $f$  that transform  $G$  such that all non-connected nodes are removed and for every edge, we create an intermediate node. For example, for points  $P, Q$  and edge  $\{P, Q\}$ , we create intermediate node  $R$  and connect all between  $P, Q, R$  with edges. We than don't allow any of these intermediate nodes to lie in  $D$ . Then  $\langle G, k \rangle \in \textit{CLIQUE} \iff f(\langle G, k \rangle) \in \textit{DENSESET}$

## Problem 2

Take the smallest element in  $X$  and add its absolute value  $+1, p$ , to every element in  $X$ , so you shift all elements to lie positive. Then also add  $|X|$  times the value  $p$  into  $X$ . For the other way around, we don't have to do anything because  $\mathbf{N} \subseteq \mathbf{Z}$