

Relative velocity

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Relative velocity - 从一个物品的视角看另一个物品的速度

Vector - direction

Velocity depends on the frame of the reference (relative - compare the object).

When doing the velocity question - always add the direction(bearing)

We can calculate their relative velocity when two thing move in the same straight line but at different speed, or object change its direction and speed.

Change direction = change velocity

Velocity - rate of change of displacement/position

Vector addition: (for calculate the relative velocity that include the direction change)

- Add the vector head to tail (not tail to tail)
- Sum of vector will be from tail of 1st to head last

Using Pythagoras

Example:
A plane travelling with a velocity of 100 km h^{-1} south relative to the air encounters a cross wind of 25 km h^{-1} , west. Calculate the velocity of the plane relative to the ground.

Solution:
 $V_{\text{plane rel to ground}} = V_{\text{plane rel to air}} + V_{\text{air rel to ground}}$

Draw a vector diagram and use Pythagoras to solve.

$$v = \sqrt{100^2 + 25^2} = 103 \text{ kmh}^{-1}$$
$$\text{Angle} = \tan^{-1} \frac{25}{100} = 14^\circ$$

Velocity = 103 km h^{-1} at a bearing of 194°

Subtraction: (When the comparing objects are in the same straight line)

V A relative to B = $V_a - V_b$ / 两个object不同速度的compare $V_{a \text{ rel } b} = V_a - V_b$

V_f = velocity final

V_i = velocity initial

change $V = V_f - V_i$ / one object 两个不同速度的变化 $V = V - U$ change of velocity can be negative because it indicate the direction of velocity is changing.

Change S = bigger S - smaller S - no direction so don't need to define the positive and negative value (speed can only be positive number or zero)

Acceleration - vector

Rate of change always relate with per second/overtime

$$\Delta V = V - U \quad a = \frac{\Delta V}{\Delta t} \quad a = \frac{V - U}{\Delta t}$$

Acceleration increase, change of the velocity increase

Large acceleration, but low velocity - when the object start acceleration at the begin of the motion which velocity is low due to the acceleration is just started

High velocity but low acceleration - when the object in constant speed which the velocity has already increased by the acceleration

Velocity and acceleration are not always the same direction(not always positive)

Speeding up - velocity +, acceleration +

Slowing down - velocity +, acceleration -

When the object change the direction - the velocity change as well

Eg: calculate the acceleration as object change velocity(=change direction)