$$p_{1}(i) = \beta_{1}(c_{i}, t_{i}) + \sum_{f=1}^{n_{\omega 1}} L_{\omega 1}(c_{i}, f)\omega_{1}(s_{i}, f) + \sum_{f=1}^{n_{\varepsilon 1}} L_{\varepsilon 1}(c_{i}, f)\varepsilon_{1}(s_{i}, f, t_{i}) + \sum_{f=1}^{n_{\eta 1}} L_{1}(c_{i}, f)\eta_{1}(v_{i}, f) + \sum_{p=1}^{n_{p}} \gamma_{1}(c_{i}, t_{i}, p)X(x_{i}, t_{i}, p) + \sum_{k=1}^{n_{k}} \lambda_{1}(k)Q(i, k)$$

$$(1)$$

$$p_{2}(i) = \beta_{2}(c_{i}, t_{i}) + \sum_{f=1}^{n_{\omega 2}} L_{\omega 2}(c_{i}, f) \omega_{2}(s_{i}, f) + \sum_{f=1}^{n_{\varepsilon 2}} L_{\varepsilon 2}(c_{i}, f) \varepsilon_{2}(s_{i}, f, t_{i})$$

$$+ \sum_{f=1}^{n_{\eta 2}} L_{2}(c_{i}, f) \eta_{2}(v_{i}, f) + \sum_{p=1}^{n_{p}} \gamma_{2}(c_{i}, t_{i}, p) X(x_{i}, t_{i}, p) + \sum_{k=1}^{n_{k}} \lambda_{2}(k) Q(i, k)$$

$$(2)$$

Part I

(iv)

$$p_1(i) = \beta_1(t_i) + \omega_1(s_i) + \varepsilon_1(s_i, t_i)$$
(3)

$$p_2(i) = \beta_2(t_i) + \omega_2(s_i) + \varepsilon_2(s_i, t_i)$$
(4)

Part III (i) $p_1(i) = \beta_1(t_i) + \omega_1(s_i) + \varepsilon_1(s_i, t_i) + \lambda_1 Q(i) \tag{5}$

$$p_2(i) = \beta_2(t_i) + \omega_2(s_i) + \varepsilon_2(s_i, t_i) + \lambda_2 Q(i)$$
(6)

.....

(ii)
$$p_1(i) = \beta_1(t_i) + \omega_1(s_i) + \varepsilon_1(s_i, t_i) + \eta_1(v_i)$$
 (7)

$$p_2(i) = \beta_2(t_i) + \omega_2(s_i) + \varepsilon_2(s_i, t_i) + \eta_2(v_i)$$
(8)

(iii)

$$p_1(i) = \beta_1(c_i, t_i) + \sum_{f=1}^{n_{\omega 1}} L_{\omega 1}(c_i, f)\omega_1(s_i, f) + \sum_{f=1}^{n_{\varepsilon 1}} L_{\varepsilon 1}(c_i, f)\varepsilon_1(s_i, f, t_i)$$
(9)

$$p_2(i) = \beta_2(c_i, t_i) + \sum_{f=1}^{n_{\omega 2}} L_{\omega 2}(c_i, f) \omega_2(s_i, f) + \sum_{f=1}^{n_{\varepsilon 2}} L_{\varepsilon 2}(c_i, f) \varepsilon_2(s_i, f, t_i)$$
(10)

.....

 $p_1(i) = \beta_1(t_i) + \omega_1(s_i) + \varepsilon_1(s_i, t_i) + \sum_{p=1}^{n_p} \gamma_1(t_i, p) X(x_i, t_i, p)$ (11)

$$p_2(i) = \beta_2(t_i) + \omega_2(s_i) + \varepsilon_2(s_i, t_i) + \sum_{p=1}^{n_p} \gamma_2(t_i, p) X(x_i, t_i, p)$$
(12)