

# ACM 模板

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#### **FastIO**

```
namespace fastio {
     const static int buf_size = 8388608;//about 8Mb
     static char buf[buf_size];
     char *ps = buf + buf_size, *pe = buf + buf_size;
     int pos;
     bool eof = false;
     inline void read_next() {
          pe = buf + fread(buf, 1, buf_size, stdin);
          ps = buf;
          if(ps == pe) eof = true;
    }
     inline bool blank(char x) {
          return x == ' ' || x == '\n' || x == '\t' || x == '\r';
    }
     inline char nc() {
          if(ps == pe) read_next();
          return *ps++;
     }
     template<typename T>
     inline void read_num(T& res) {
          bool neg = false;
          char now = nc();
          while(blank(now)) now = nc();
          if(now == '-') {
               neg = true;
               now = nc();
          }
          T ret = 0;
          while(!blank(now)) {
               ret = ret * 10 + now - '0';
               now = nc();
          res = (neg ? -ret : ret);
     }
     template<typename T>
     inline void put_num(T x) {
          if(x < 0) {
```

```
putchar('-');
               x = -x;
          }
          if(x == 0) {
                putchar('0');
          }
          char tmp[32];
          int cnt = 0;
          while(x) {
               tmp[cnt++] = x \% 10 + '0';
               x /= 10;
          }
          while(cnt > 0) {
                putchar(tmp[cnt - 1]);
               --cnt;
          }
     }
}
```

## 计算几何基础

```
const double eps = 1e-7;
int cmp(double x, double y)
{
     if(fabs(x - y) < eps) return 0;
     return (x < y)? -1:1;
}
struct Point {
     double x, y;
     Point(double _{x} = 0, double _{y} = 0) : x(_{x}), y(_{y}) {}
     friend istream& operator>>(istream& is, Point& p)
          is >> p.x >> p.y;
          return is;
     }
};
struct Vector {
     double x, y;
     Vector(double _x = 0, double _y = 0) : x(_x), y(_y) {}
     Vector(Point s, Point t) : x(t.x - s.x), y(t.y - s.y) {}
```

```
Vector operator+(Vector other)
     {
          return Vector(x + other.x, y + other.y);
     }
     Vector operator-(Vector other)
          return Vector(x - other.x, y - other.y);
     }
     Vector operator*(double k)
     {
          return Vector(x * k, y * k);
     }
     friend Vector operator*(double k, Vector other)
     {
          return other * k;
     }
     friend double dot(Vector lhs, Vector rhs)
     {
          return lhs.x * rhs.x + lhs.y * rhs.y;
     }
     friend double cross(Vector lhs, Vector rhs)
     {
          return lhs.x * rhs.y - rhs.x * lhs.y;
     }
     friend istream& operator>>(istream& is, Vector& v)
     {
          cin >> v.x >> v.y;
          return is;
     }
struct Line {
     Point o;
     Vector dir;
     Line(Point x, Point y): o(x), dir(x, y) {}
     Line(Point _o, Vector _d) : o(_o), dir(_d) {}
```

**}**;

```
friend Point getCrossPoint(Line lhs, Line rhs)
     {
          assert(cmp(cross(lhs.dir, rhs.dir), 0.0) != 0);
          Vector u(rhs.o, lhs.o);
          double t = cross(rhs.dir, u) / cross(lhs.dir, rhs.dir);
          Vector dt = lhs.dir * t;
          return Point(lhs.o.x + dt.x, lhs.o.y + dt.y);
     }
};
bool sameDir(Vector a, Vector b)
{
     return cmp(dot(a, b), 0) > 0 && cmp(cross(a, b), 0) == 0;
}
bool onSeg(Point a, Point b, Point c)
     return c.x >= min(a.x, b.x) && c.y >= min(a.y, b.y) && c.x <= max(a.x, b.x) && c.y <= max(a.y, b.x)
b.y) &&
     cmp(cross(Vector(c, a), Vector(c, b)), 0) == 0;
}
                                               并查集
namespace UFS {
     const int N = 1e5 + 10;
     inline void init() { memset(fa, 0xff, sizeof(fa)); }
     inline int id(int u) {
          int rt = u;
          while(fa[rt] > 0) rt = fa[rt];
          while(fa[u] > 0) { int tmp = fa[u]; fa[u] = rt; u = tmp; }
          return rt;
     }
     inline void join(int u, int v) {
          int uf = id(u);
          int vf = id(v);
          if(uf != vf) {
                if(fa[uf] < fa[vf]) { fa[uf] += fa[vf]; fa[vf] = uf; }
                else { fa[vf] += fa[uf]; fa[uf] = vf; }
          }
     }
```

inline int size(int u) { return -fa[id(u)]; }

**}**;

### ST 表

```
struct ST {
     //1 base, query O(1)
     int dp[50005][20];
     int n;
     int arr[50005];
     void make(int _n) {
           assert(n < 50005);
           n = _n;
           for(int i = 1; i <= n; ++i) {
                 dp[i][0] = arr[i];
           for(int j = 1; (1 << j) <= n; ++j) {
                 for(int i = 1; (i + (1 << (j - 1))) <= n; ++i) {
                      dp[i][j] = min(dp[i][j-1], dp[i+(1 << (j-1))][j-1]);
                 }
           }
     }
     int query(int I, int r) {
           int k = 31 - \underline{\quad }builtin_clz(r - l + 1);
           return min(dp[l][k], dp[r - (1 << k) + 1][k]);
     }
} st;
```

## 链表

```
template<typename T>
struct ACM_list {
    static const int MAXN = 100005;
    static const int BEG = 0;
    static const int END = MAXN - 1;
    struct Node {
        T data;
        int next;
        int pre;
    } node[MAXN];
    int free[MAXN], fp;
    int sz;
```

```
void init() {
     node[BEG] = \{T\{\}, END, -1\};
     node[END] = \{T\{\}, -1, BEG\};
     fp = MAXN - 3;
     for(int i = 0; i \le fp; ++i) {
          free[i] = i + 1;
     }
     sz = 0;
}
int ins_back(int idx, T val) {
     node[free[fp]].next = node[idx].next;
     node[free[fp]].data = val;
     node[free[fp]].pre = idx;
     node[idx].next = free[fp];
     node[node[free[fp]].next].pre = free[fp];
     ++sz;
     return free[fp--];
}
int ins_pre(int idx, T val) {
     idx = node[idx].pre;
     return ins_back(idx, val);
}
void del(int idx) {
     assert(idx != BEG && idx != END);
     node[node[idx].pre].next = node[idx].next;
     node[node[idx].next].pre = node[idx].pre;
     free[++fp] = idx;
     --SZ;
}
Node& operator[](int idx) {
     return node[idx];
}
int begin() const {
     return node[BEG].next;
}
int end() const {
     return END;
}
```

```
int size() const {
          return sz;
}

};

ACM_list<int> li;
```

## 树状数组

```
struct Bit {
     //1 Base
     int arr[300005];
     int n;
     int lowbit(int x) { return x & (-x); }
     void add(int i, int x) {
          int pos = i;
          while(pos <= n) {
                arr[pos] += x;
                pos += lowbit(pos);
          }
     }
     int sum(int i) {
          int pos = i, ans = 0;
          while(pos) {
                ans += arr[pos];
                pos -= lowbit(pos);
          return ans;
     }
     void init(int _n) {
          n = _n;
          for(int i = 1; i <= n; ++i) {
                arr[i] += sum(i - 1) - sum(i - lowbit(i));
          }
     }
} bit;
```

```
const int VN = 50000, EN = 100000;
struct ST {
     //1 base, query O(1)
     int dp[VN << 1][20];
     int n;
     int arr[VN << 1];
     void make(int _n) {
           n = _n;
           for(int i = 1; i <= n; ++i) {
                 dp[i][0] = i;
           for(int j = 1; (1 << j) <= n; ++j) {
                 for(int i = 1; (i + (1 << (j - 1))) <= n; ++i) {
                      int I = dp[i][j-1], r = dp[i+(1 << (j-1))][j-1];
                      dp[i][j] = arr[l] < arr[r] ? I : r;</pre>
                }
           }
     }
     int query(int I, int r) {
           int k = 31 - \underline{\qquad} builtin_clz(r - l + 1);
           int Ii = dp[I][k], ri = dp[r - (1 << k) + 1][k];
           return arr[li] < arr[ri] ? li : ri;
     }
} st;
struct edge {
     int to, cost, next;
     edge() {}
     edge(int _to, int _cost, int _next) : to(_to), cost(_cost), next(_next) {}
} eg[EN];
int head[VN], dis[VN], id[VN], la[VN << 1], lacnt, tot;
bool vis[VN];
void init() {
     memset(head, 0xff, sizeof(head));
     memset(vis, 0x00, sizeof(vis));
     tot = lacnt = 1;
}
void addedge(int from, int to, int cost) {
     eg[tot] = edge(to, cost, head[from]);
```

```
head[from] = tot++;
}
void dfs(int v, int height) {
     vis[v] = true;
     id[v] = lacnt;
     st.arr[lacnt] = height;
     la[lacnt++] = v;
     for(int i = head[v]; i != -1; i = eg[i].next) {
          if(!vis[eg[i].to]) {
                dis[eg[i].to] = dis[v] + eg[i].cost;
                dfs(eg[i].to, height + 1);
                st.arr[lacnt] = height;
                la[lacnt++] = v;
          }
     }
}
int lca(int u, int v) {
     int I = min(id[u], id[v]), r = max(id[u], id[v]);
     return la[st.query(l, r)];
}
                                                 SCC
namespace SCC {
     //id 1 to n
     const int VN = 10005, EN = 100005;
     struct edge {
          int to, next;
          edge() {}
          edge(int _to, int _next) : to(_to), next(_next) {}
     } se[EN], re[EN];
     int shead[VN], rhead[VN], vs[VN], cmp[VN], vidx, stot, rtot, n;
     bool vis[VN];
     void init(int _n) {
          n = _n;
          stot = rtot = 0;
          memset(shead, 0xff, sizeof(shead));
          memset(rhead, 0xff, sizeof(rhead));
          vidx = 0;
     }
```

```
void addedge(int from, int to) {
           se[stot] = edge(to, shead[from]);
           shead[from] = stot++;
           re[rtot] = edge(from, rhead[to]);
           rhead[to] = rtot++;
     }
     void dfs(int v) {
           vis[v] = true;
           for(int i = shead[v]; i != -1; i = se[i].next) {
                if(!vis[se[i].to]) {
                      dfs(se[i].to);
                }
           }
           vs[vidx++] = v;
     }
     void rdfs(int v, int k) {
           vis[v] = true;
           cmp[v] = k;
           for(int i = rhead[v]; i != -1; i = re[i].next) {
                if(!vis[re[i].to]) {
                      rdfs(re[i].to, k);
                }
           }
     }
     int scc() {
           memset(vis, 0, sizeof(vis));
           for(int i = 1; i <= n; ++i) {
                if(!vis[i]) dfs(i);
           }
           memset(vis, 0, sizeof(vis));
           int k = 0;
           for(int i = vidx - 1; i >= 0; --i) {
                if(!vis[vs[i]]) rdfs(vs[i], k++);
           }
           return k;
     }
}
```

```
using int64 = long long;
struct edge {
     int to, cost, next;
     edge() {}
     edge(int _to, int _cost, int _next) : to(_to), cost(_cost), next(_next) {}
} e[12500];
int tot;
int head[2505];
void init_graph() {
     tot = 0;
     memset(head, -1, sizeof(head));
}
void addedge(int from, int to, int cost) {
     e[tot] = edge(to, cost, head[from]);
     head[from] = tot++;
}
int64 dis[2505];
bool vis[2505];
int64 dijkstra(int s, int t) {
     using PLI = pair<int64, int>;
     memset(dis, 0x3f, sizeof(dis));
     memset(vis, 0x00, sizeof(vis));
     priority_queue<PLI, vector<PLI>, greater<PLI>> pq;
     pq.push(PLI(0, s));
     dis[s] = 0;
     while(!pq.empty()) {
          PLI now = pq.top();
          pq.pop();
          if(vis[now.second]) continue;
          vis[now.second] = true;
          for(int i = head[now.second]; i != -1; i = e[i].next) {
                if(!vis[e[i].to] && e[i].cost + now.first < dis[e[i].to]) {
                     dis[e[i].to] = e[i].cost + now.first;
                     pq.push(PLI(dis[e[i].to], e[i].to));
                }
          }
     }
     return dis[t];
}
```

#### Dinic

```
namespace Dinic {
     const int V = 1000010, E = 8000010, INF = 1e9;
     int vcnt;
     struct edge {
          int to, next, cap, flow;
          edge() {}
          edge(int _to, int _next, int _cap) : to(_to), next(_next), cap(_cap), flow(0) {}
     } eg[E];
     int head[V], cur[V], dis[V], que[V], qf, qe, ecnt, s, t;
     bool vis[V];
     void init(int _vcnt) {
          vcnt = _vcnt;
          memset(head, 0xff, sizeof(head[0]) * (vcnt + 1));
          ecnt = 0;
     }
     void addedge(int from, int to, int cap) {
          eg[ecnt] = edge(to, head[from], cap);
          head[from] = ecnt++;
          eg[ecnt] = edge(from, head[to], 0);
          head[to] = ecnt++;
     }
     bool bfs() {
          memset(vis, 0, sizeof(vis[0]) * (vcnt + 1));
          qf = 0; qe = 0;
          que[qe++] = s;
          dis[s] = 0; vis[s] = true;
          while(qf < qe) {
               int x = que[qf++];
               for(int i = head[x]; i != -1; i = eg[i].next) {
                    const edge& e = eg[i];
                     if(!vis[e.to] && e.cap > e.flow) {
                          vis[e.to] = true;
                          dis[e.to] = dis[x] + 1;
                          que[qe++] = e.to;
                          if(e.to == t) return true;
                    }
               }
          }
          return false;
```

```
}
     int dfs(int x, int a) {
           if(x == t | | a == 0) return a;
           int flow = 0, f;
           for(int& i = cur[x]; i != -1; i = eg[i].next) {
                edge& e = eg[i];
                if(dis[x] + 1 == dis[e.to] && (f = dfs(e.to, min(e.cap - e.flow, a)))) {
                      e.flow += f;
                     eg[i ^ 1].flow -= f;
                     flow += f;
                     a -= f;
                     if(!a) break;
                }
          }
           return flow;
     }
     int solve(int _s, int _t) {
           s = _s; t = _t;
          int flow = 0;
           while(bfs()) {
                memcpy(cur, head, sizeof(cur[0]) * (vcnt + 1));
                flow += dfs(s, INF);
          }
           return flow;
     }
}
```

#### Treap

```
template<typename T, class _Comp = less<T>>
struct Treap {
    const static int NODECNT = _;
    struct Node {
        int ch[2], p, sz;
        T v;
        void make(int _I, int _r, int _p, const T& _v) {
            ch[0] = _I; ch[1] = _r; p = _p; v = _v; sz = 1;
        }
    } node[NODECNT];
    int m_rt, mp[NODECNT], mp_idx, node_idx;
```

```
void maintain(int x) {
     node[x].sz = 1;
     node[x].sz += node[x].ch[0] == -1 ? 0 : node[node[x].ch[0]].sz;
     node[x].sz += node[x].ch[1] == -1 ? 0 : node[node[x].ch[1]].sz;
}
_Comp cmp;
explicit Treap(const _Comp& c): cmp(c) { unsigned seed = 19971023; srand(seed); clear(); }
Treap() : cmp(_Comp()) { unsigned seed = 19971023; srand(seed); clear(); }
void clear() { m_rt = -1; mp_idx = -1; node_idx = 0; }
void ins(const T& val) { _ins(m_rt, val); }
void _ins(int& rt, const T& val) {
     if(rt == -1) {
          if(mp_idx == -1) { node[rt = node_idx++].make(-1, -1, rand(), val); }
          else { node[rt = mp[mp_idx--]].make(-1, -1, rand(), val); }
     } else {
          int type = cmp(node[rt].v, val);
          _ins(node[rt].ch[type], val);
          maintain(rt);
          if(node[rt].p < node[node[rt].ch[type]].p) rotate(rt, type);</pre>
     }
}
void del(const T& val) { _del(m_rt, val); }
void _del(int& rt, const T& val) {
     assert(rt != -1);
     if(node[rt].v == val) {
          if(node[rt].ch[0] == -1) {
               mp[++mp idx] = rt;
               rt = node[rt].ch[1];
          } else if(node[rt].ch[1] == -1) {
               mp[++mp_idx] = rt;
               rt = node[rt].ch[0];
          } else {
               int next = node[node[rt].ch[0]].p < node[node[rt].ch[1]].p;</pre>
               rotate(rt, next);
               _del(node[rt].ch[next ^ 1], val);
               maintain(rt);
          }
     } else {
          _del(node[rt].ch[cmp(node[rt].v, val)], val);
```

```
maintain(rt);
     }
}
int find(const T& val) {
     int rt = m_rt;
     while(rt != -1) {
          if(node[rt].v == val) return rt;
          rt = node[rt].ch[cmp(node[rt].v, val)];
     }
     return -1;
}
void rotate(int& rt, int type) {
     int tmp = node[rt].ch[type];
     node[rt].ch[type] = node[tmp].ch[type ^ 1];
     node[tmp].ch[type ^ 1] = rt;
     maintain(rt); maintain(tmp);
     rt = tmp;
}
int kth(int k) {
     assert(k >= 1 && k <= size());
     int rt = m_rt, res = -1;
     while(rt != -1) {
          int le = node[rt].ch[0] == -1 ? 0 : node[node[rt].ch[0]].sz;
          if(le == k - 1) {
                res = node[rt].v;
                break;
          } else if(le > k - 1) {
                rt = node[rt].ch[0];
          } else {
                k -= le + 1;
                rt = node[rt].ch[1];
          }
     }
     return res;
}
int rank(const T& val) {
     int rt = m_rt, cnt = 0;
     while(rt != -1) {
          int le = node[rt].ch[0] == -1 ? 0 : node[node[rt].ch[0]].sz;
          if(cmp(node[rt].v, val)) {
```

```
cnt += le + 1;
    rt = node[rt].ch[1];
    } else {
        rt = node[rt].ch[0];
    }
    return cnt + 1;
}
int size() { return node[m_rt].sz; }
};
```

## 线段树

```
using II = long long;
struct seg_tree {
     static const int MAXN = 100005;
     struct Node {
          Il sum, tag;
     } node[MAXN << 2];
     Il arr[MAXN];
     int lson(int x) { return x << 1; }</pre>
     int rson(int x) { return (x << 1) + 1; }
     void make(int x, int xl, int xr) {
          if(xl == xr) {
               node[x].sum = arr[xl];
               node[x].tag = 0;
               return;
          }
          int mid = (xl + xr) >> 1;
          make(lson(x), xl, mid);
          make(rson(x), mid + 1, xr);
          node[x].sum = node[lson(x)].sum + node[rson(x)].sum;
          node[x].tag = 0;
     }
     void pushdown(int x, int xl, int xr) {
          node[x].sum += (xr - xl + 1) * node[x].tag;
          if(xl < xr) {
               node[lson(x)].tag += node[x].tag;
               node[rson(x)].tag += node[x].tag;
```

```
}
           node[x].tag = 0;
     }
     void pushup(int x, int xl, int xr) {
           int mid = (xl + xr) >> 1;
           int lcnt = mid - xl + 1, rcnt = xr - mid;
           node[x].sum = node[lson(x)].sum + lcnt * node[lson(x)].tag + node[rson(x)].sum + rcnt *
node[rson(x)].tag;
     }
     Il query(int x, int xl, int xr, int ql, int qr) {
           if(xl > qr \mid \mid xr < ql) return 0;
           if(xl == ql \&\& xr == qr) {
                 return node[x].sum + (xr - xl + 1) * node[x].tag;
           }
           II ans = 0;
           int mid = (xl + xr) >> 1;
           pushdown(x, xl, xr);
           ans += query(lson(x), xl, mid, ql, min(mid, qr));
           ans += query(rson(x), mid + 1, xr, max(ql, mid + 1), qr);
           return ans;
     }
     void update(int x, int xl, int xr, int cl, int cr, ll dt) {
           if(xr < cl \mid \mid xl > cr) return;
           if(cl == xl \&\& cr == xr) {
                node[x].tag += dt;
                return;
           pushdown(x, xl, xr);
           int mid = (xl + xr) >> 1;
           update(lson(x), xl, mid, cl, min(mid, cr), dt);
           update(rson(x), mid + 1, xr, max(cl, mid + 1), cr, dt);
           pushup(x, xl, xr);
     }
} st;
```

## KM 字符串匹配

```
typedef long long II;
typedef unsigned long long ull;
```

```
int km_match(char* pattern, char* str) {
     int plen = strlen(pattern);
     int slen = strlen(str);
     int dt = max(((plen - 1) >> 1), 1);
     int cnt = 0;
     ull phash = 0, shash = 0;
     ull con = 1;
     for(int i = 0; i < plen; ++i) {
           phash = ((phash << 7) + pattern[i]);</pre>
           shash = ((shash << 7) + str[i]);
           con <<= 7;
     }
     con >>= 7;
     for(int i = 0; i < slen - plen + 1; ++i) {
           if(phash == shash) {
                bool flag = true;
                for(int j = 0; j < plen; <math>j += dt) {
                      if(pattern[j] != str[i + j]) {
                           flag = false;
                           break;
                     }
                }
                if(flag) ++cnt;
           }
           shash = (((shash - str[i] * con) << 7) + str[i + plen]);
     }
     return cnt;
}
                                                    LIS
struct LIS {
     // O(nlgn), strictly increase monotonically
     const static int N = 100005;
     int a[N], b[N];
     void input(int n) {
           for(int i = 1; i <= n; ++i) {
                scanf("%d", a + i);
           }
     }
     int solve(int n) {
```

```
int len = 0;
for(int i = 1; i <= n; ++i) {
        int* p = lower_bound(b + 1, b + len + 1, a[i]);
        *p = a[i];
        len = max(len, a[i] = p - b);
    }
    return len;
}
} lis;</pre>
```

## 数值积分

```
namespace Int {
     const double eps = 1e-6;
     template<class Callable>
     double Simpson(double lb, double ub, const _Callable& f) {
          double mid = (lb + ub) * .5;
          return (ub - lb) * (f(lb) + 4 * f(mid) + f(ub)) / 6.;
     }
     template<class _Callable>
     double asr(double lb, double ub, double pre, double eps, const Callable& f) {
          double mid = (lb + ub) * .5;
          double L = Simpson(lb, mid, f), R = Simpson(mid, ub, f);
          if(fabs(L + R - pre) < 15 * eps) return (L + R) + (L + R - pre) / 15.;
          return _asr(lb, mid, L, eps / 2, f) + _asr(mid, ub, R, eps / 2, f);
     }
     template<class _Callable>
     double asr(double lb, double ub, const _Callable& f) {
          return _asr(lb, ub, Simpson(lb, ub, f), eps, f);
     }
}
```

#### **FWT**

```
void FWT(int* a, int n) { for(int d = 1; d < n; d <<= 1) \{ \\ for(int m = d << 1, i = 0; i < n; i += m) \{ \\ for(int j = 0; j < d; ++j) \{ \\ int x = a[i+j], y = a[i+j+d]; \\ a[i+j] = (x+y) \% MOD; \end{cases}
```

```
a[i + j + d] = (x - y + MOD) \% MOD;
                    //xor:a[i+j]=x+y,a[i+j+d]=(x-y+MOD)%MOD;
                    //and:a[i+j]=x+y;
                    //or:a[i+j+d]=x+y;
               }
          }
     }
}
void UFWT(int* a,int n) {
     for(int d = 1; d < n; d <<= 1) {
          for(int m = d \ll 1, i=0; i < n; i += m){
               for(int j = 0; j < d; ++j) {
                    int x = a[i + j], y = a[i + j + d];
                    a[i + j] = 1LL * (x + y) * rev % MOD;
                    a[i + j + d] = (1LL * (x - y) * rev % MOD + MOD) % MOD;
                    //xor:a[i+j]=(x+y)/2,a[i+j+d]=(x-y)/2;
                    //and:a[i+j]=x-y;
                    //or:a[i+j+d]=y-x;
               }
          }
     }
}
```