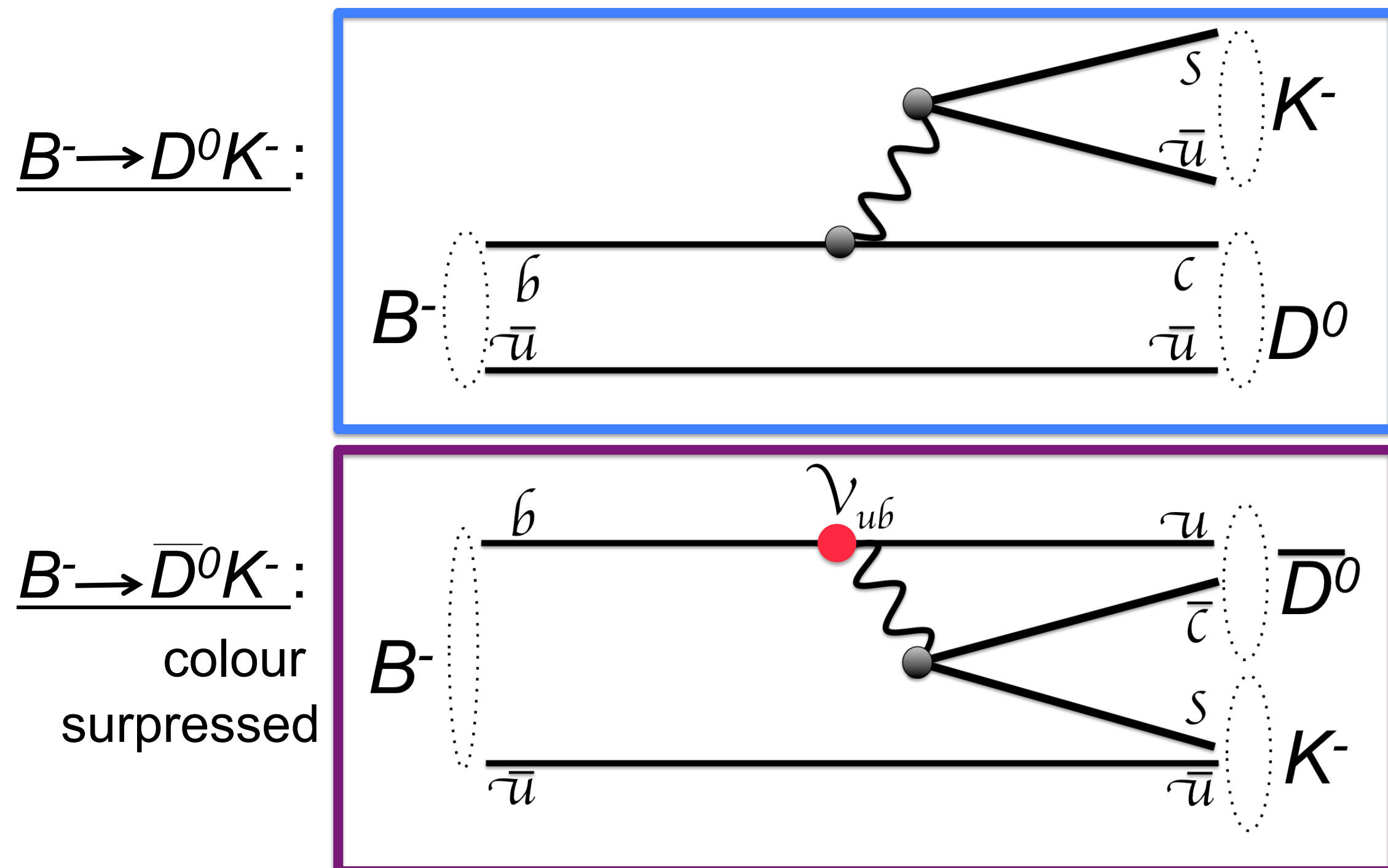
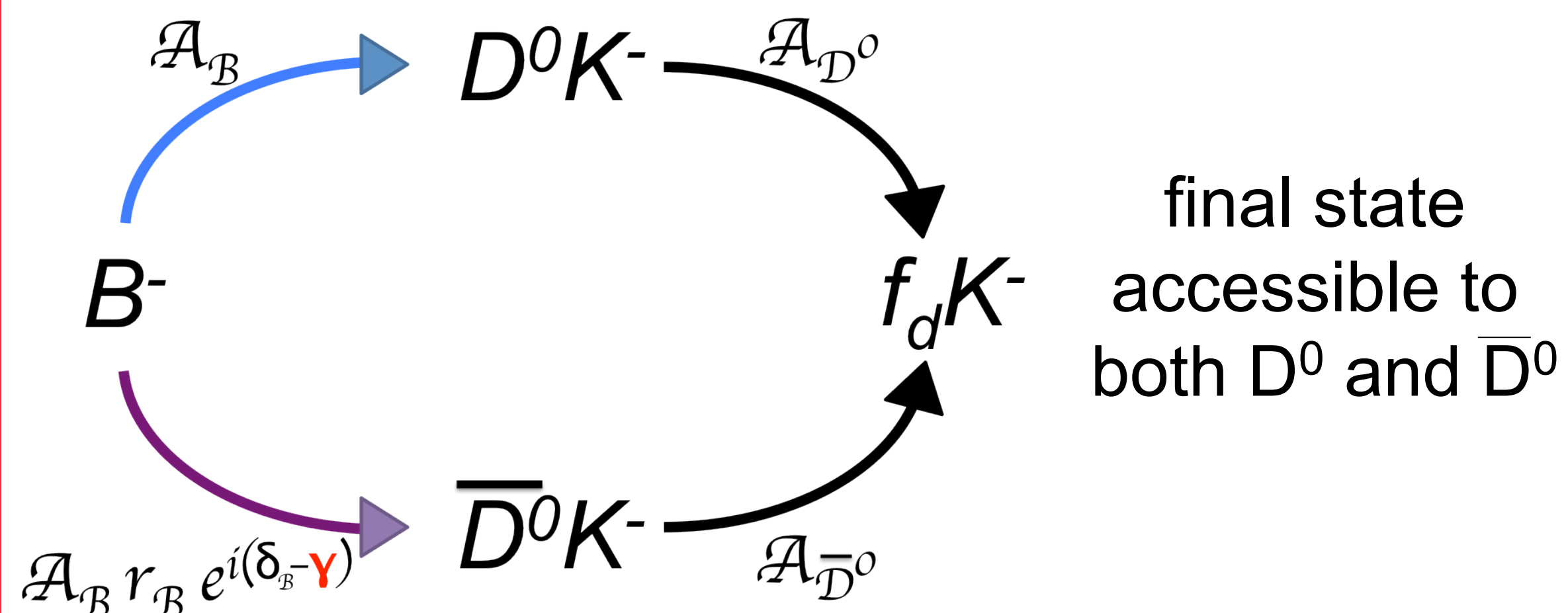


# Towards a model-independent measurement of $\gamma$ through $B^\pm \rightarrow D(\rightarrow 4\pi)K^\pm$ decays with LHCb and CLEO-c

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## Measurement of CKM angle $\gamma$ through interference in $B^\pm \rightarrow D(\rightarrow f_D)K^\pm$



### Partial decay width

$$d\Gamma(B \rightarrow D^0(\rightarrow f_D)K^-) \propto A_B^2 \cdot \left( A_{D^0}^2 + r_B^2 A_{\bar{D}^0}^2 + 2r_B \Re(A_{D^0} A_{\bar{D}^0}^* e^{-i(\delta_B - \gamma)}) \right) dp$$

$\gamma$  becomes an observable in the interference term

## Reconstruction of the D mesons in self-conjugate final state $f_D = \pi^+(p_1) \pi^+(p_2) \pi^-(p_3) \pi^-(p_4)$

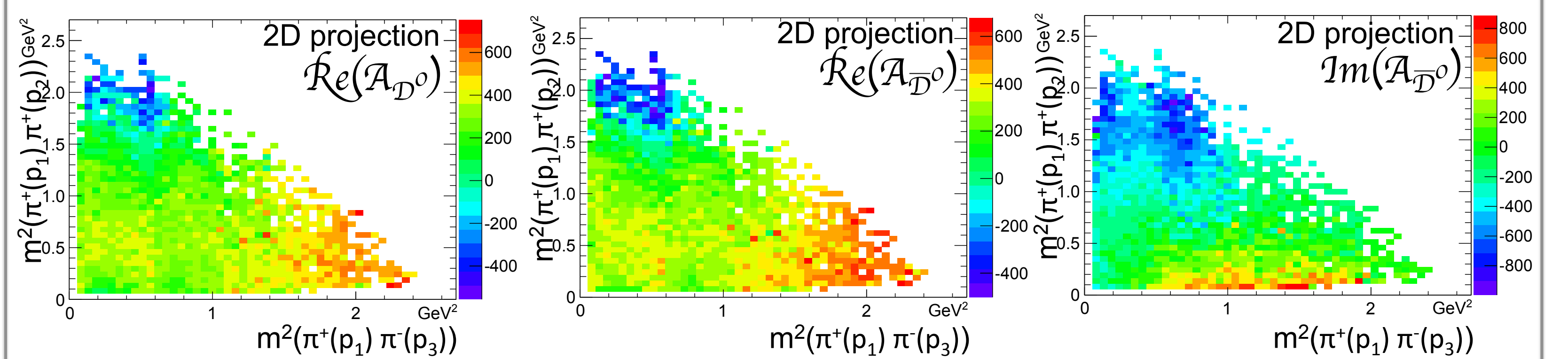
CP-conjugation\*

$$A_{\bar{D}^0}(\pi^+(p_1)\pi^+(p_2)\pi^-(p_3)\pi^-(p_4)) \stackrel{\text{CP-conjugation}^*}{=} A_{D^0}(\pi^+(-p_3)\pi^+(-p_4)\pi^-(-p_1)\pi^-(-p_2))$$

$$\frac{A_{D^0}(\pi^+(p_1)\pi^+(p_2)\pi^-(p_3)\pi^-(p_4))}{A_{\bar{D}^0}(\pi^+(p_1)\pi^+(p_2)\pi^-(p_3)\pi^-(p_4))} = \frac{|A_{D^0}(\pi^+(p_1)\pi^+(p_2)\pi^-(p_3)\pi^-(p_4))|}{|A_{\bar{D}^0}(\pi^+(p_1)\pi^+(p_2)\pi^-(p_3)\pi^-(p_4))|} e^{i\Delta\delta(\pi^+(p_1)\pi^+(p_2)\pi^-(p_3)\pi^-(p_4))}$$

strong phase difference between  $A_{D^0}$  and  $A_{\bar{D}^0}$

All amplitudes and phases depend on the point in phase space  
→ **Dalitz plot analysis in 5 dimensions**



In order to extract  $\gamma$  the analysis has to be performed in bins of phase space.

Binned decay width:

$$d\Gamma_i \propto 2r_B \left[ c_i \cos(\delta_B - \gamma) + s_i \sin(\delta_B - \gamma) \right]$$

$$c_i = \frac{1}{N} \int_{p_i}^{p_i + \Delta p} dp \frac{d\Phi}{dp} A_{D^0} \overline{A_{D^0}} \cos(\Delta\delta)$$

amplitude-weighted average of  $\cos(\Delta\delta)$

$$s_i = \frac{1}{N} \int_{p_i}^{p_i + \Delta p} dp \frac{d\Phi}{dp} A_{D^0} \overline{A_{D^0}} \sin(\Delta\delta)$$

amplitude-weighted average of  $\sin(\Delta\delta)$

(\*) Assuming no CP-V in the D decays and neglecting 2<sup>nd</sup> order effects from charm mixing.

## Model independent determination of $c_i$ and $s_i$ with CLEO-c using correlated D meson pairs from $\Psi(3770) \rightarrow D\bar{D}$

$c_i$ : Reconstruct  $D \rightarrow 4\pi$  as flavour or CP eigenstate by using **opposite side tagging** → combine information of **CP ( $M_i^\pm$ )** and **flavour ( $K_i$ )** Dalitz plots

$\Psi(3770) \rightarrow D^+ D^-$  (Flavour/CP eigenstate)  $(\pi^+(p_1) \pi^+(p_2) \pi^-(p_3) \pi^-(p_4))$

$$M_i^\pm = h_{CP^\pm} (K_i \pm 2c_i \sqrt{K_i K_i} + K_i)$$

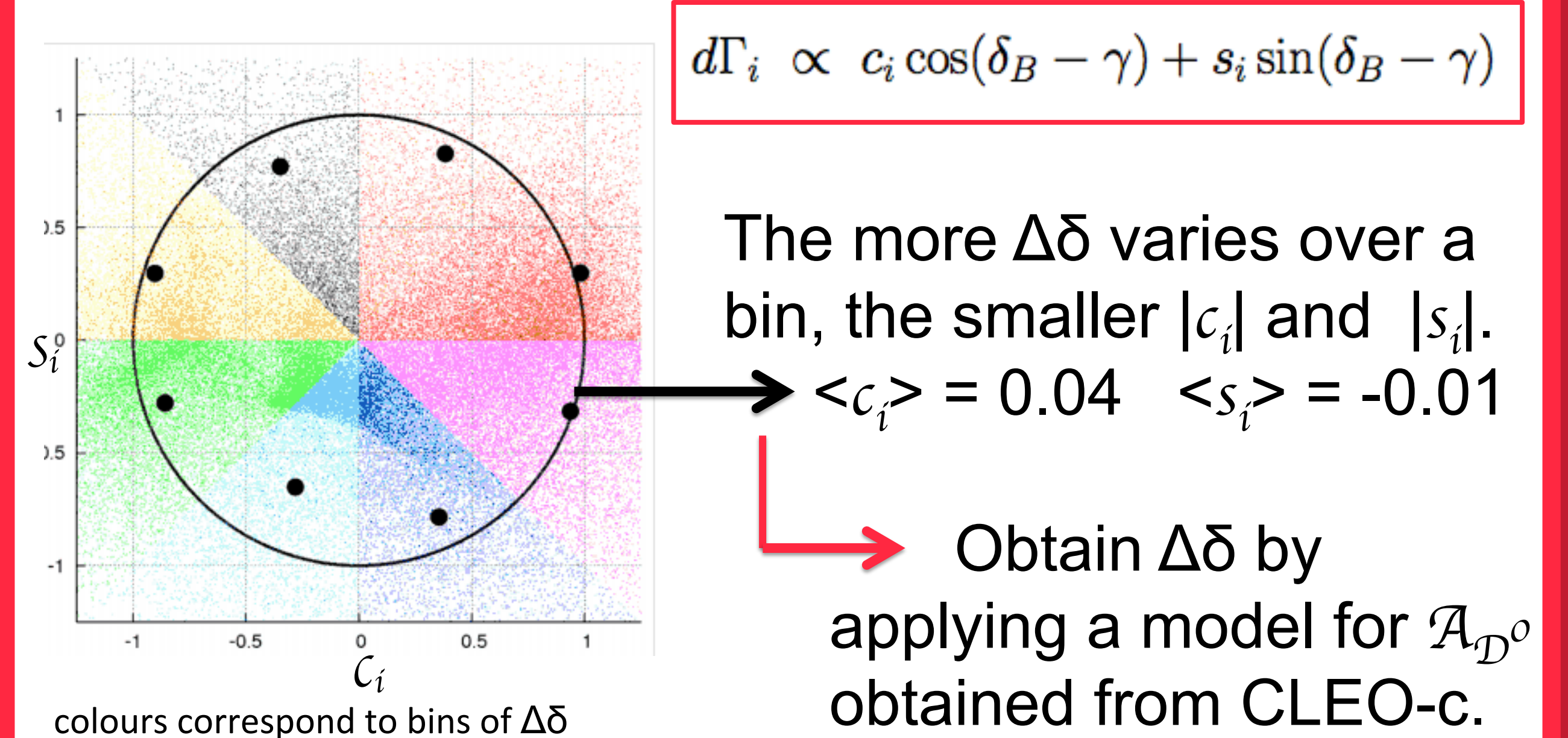
$s_i$ : Reconstruct  $\Psi(3770) \rightarrow (D\bar{D}) \rightarrow (4\pi)(4\pi')$  and use **interference effects between both possible decay paths**

Event rate in  $i$ th bin of first and  $j$ th bin of second Dalitz plot:

$$M_{ij} = h_{corr} (K_i K_j + K_i K_j - 2\sqrt{K_i K_j K_i K_j} (c_i c_j + s_i s_j))$$

## Model inspired binning

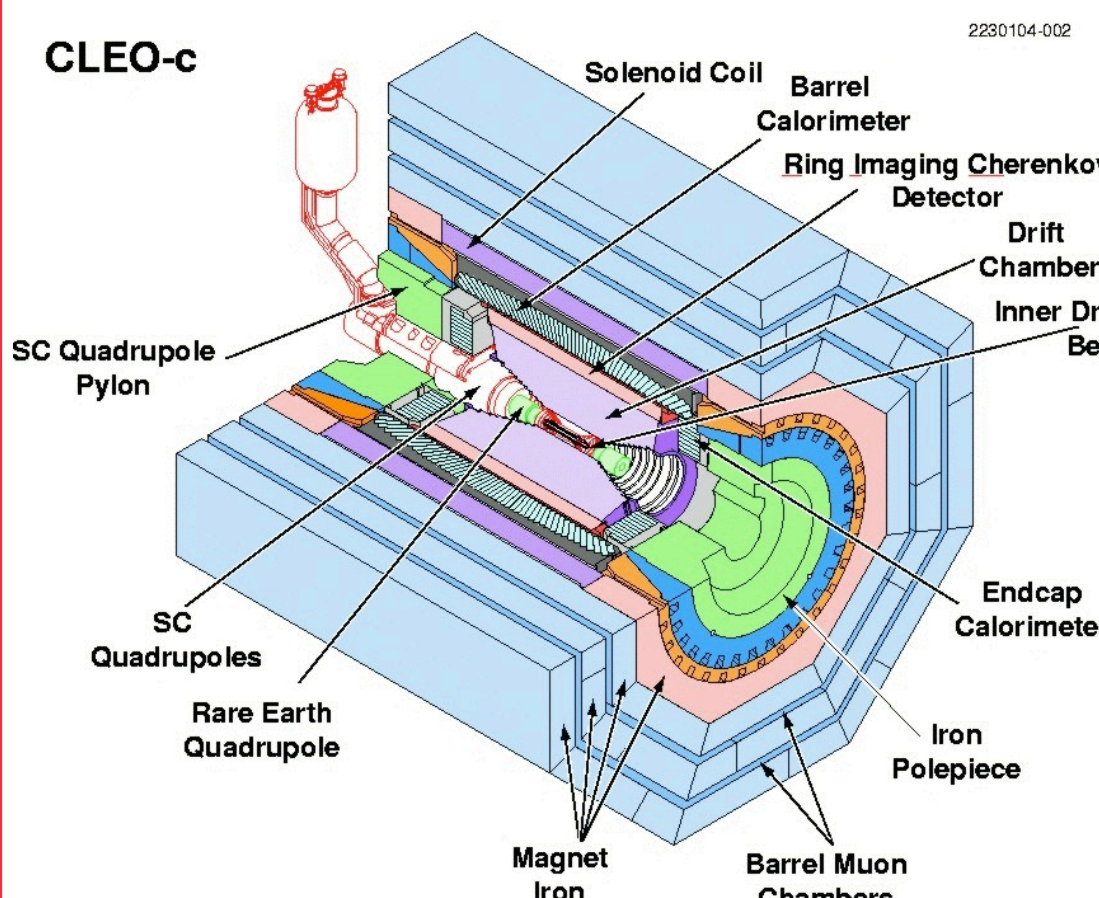
The highest sensitivity to  $\gamma$  can be obtained by using **bins with minimal variation of  $\Delta\delta$** .



Note: The binning only influences the **sensitivity** of the  $\gamma$  measurement but **not the  $\gamma$  value itself**.

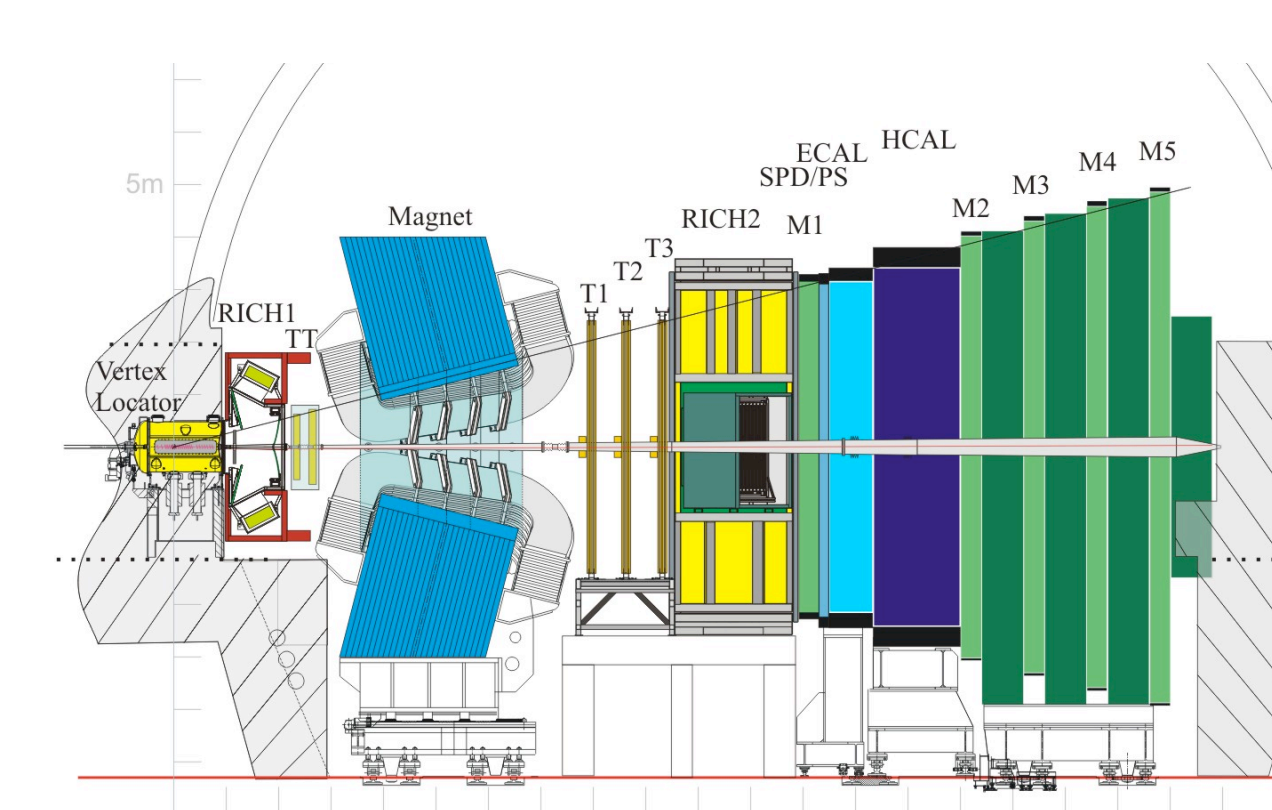
## Analysis procedure for the future:

### 1. CLEO-c



Measurement of  $c_i$  and  $s_i$  using  
~ 9500 flavour tagged  $D(\rightarrow 4\pi)$  events  
~ 1000 CP tagged  $D(\rightarrow 4\pi)$  events  
and performing a 5 dimensional fit for each bin in phase space.

### 2. LHCb



Simultaneous fit of  $r_B$ ,  $\delta_B$  and  $\gamma$  in all bins of phase space using a few  $10^3$   $B^\pm \rightarrow D(\rightarrow 4\pi)K^\pm$  events and the  $c_i$  and  $s_i$  extracted from CLEO-c.