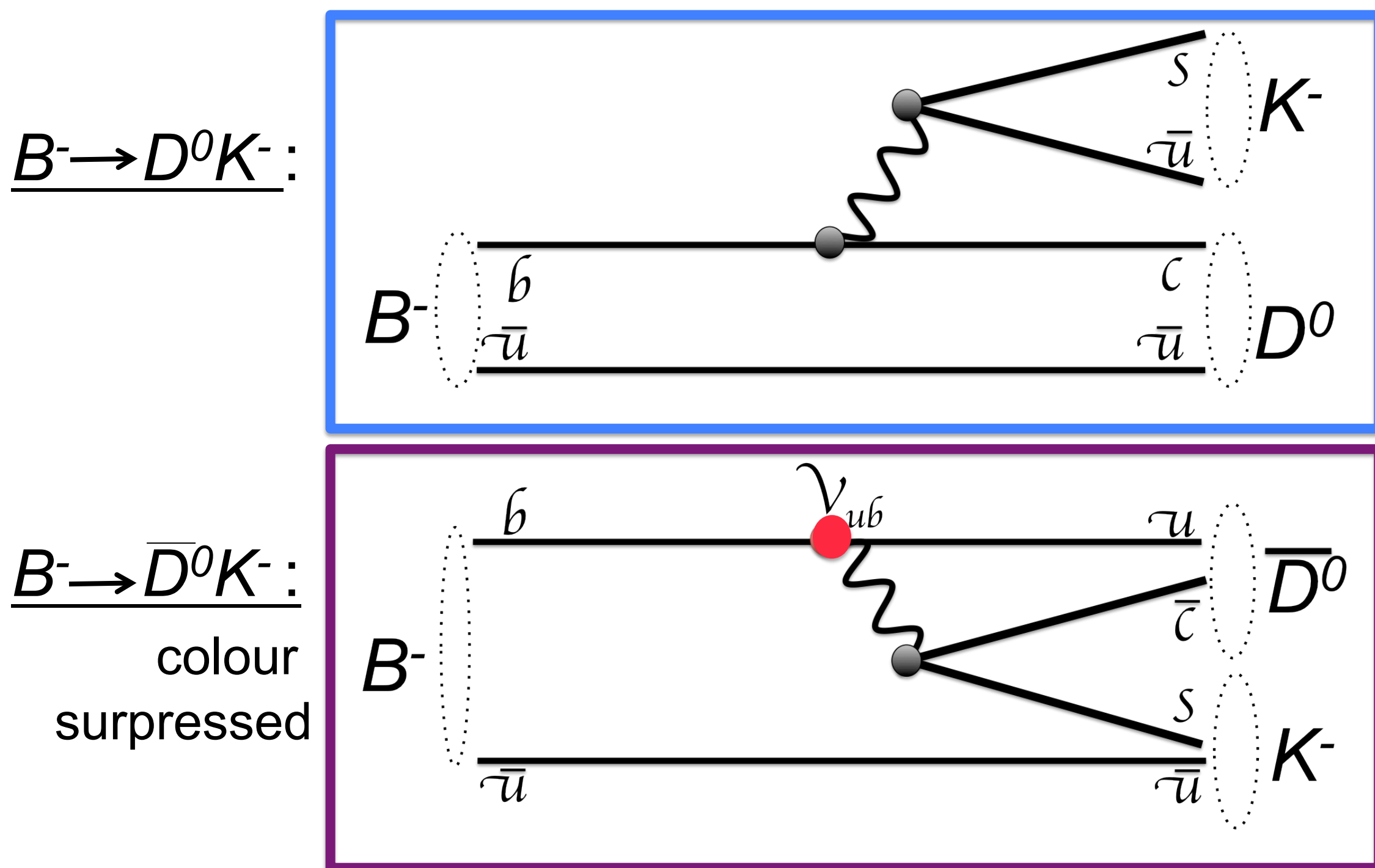
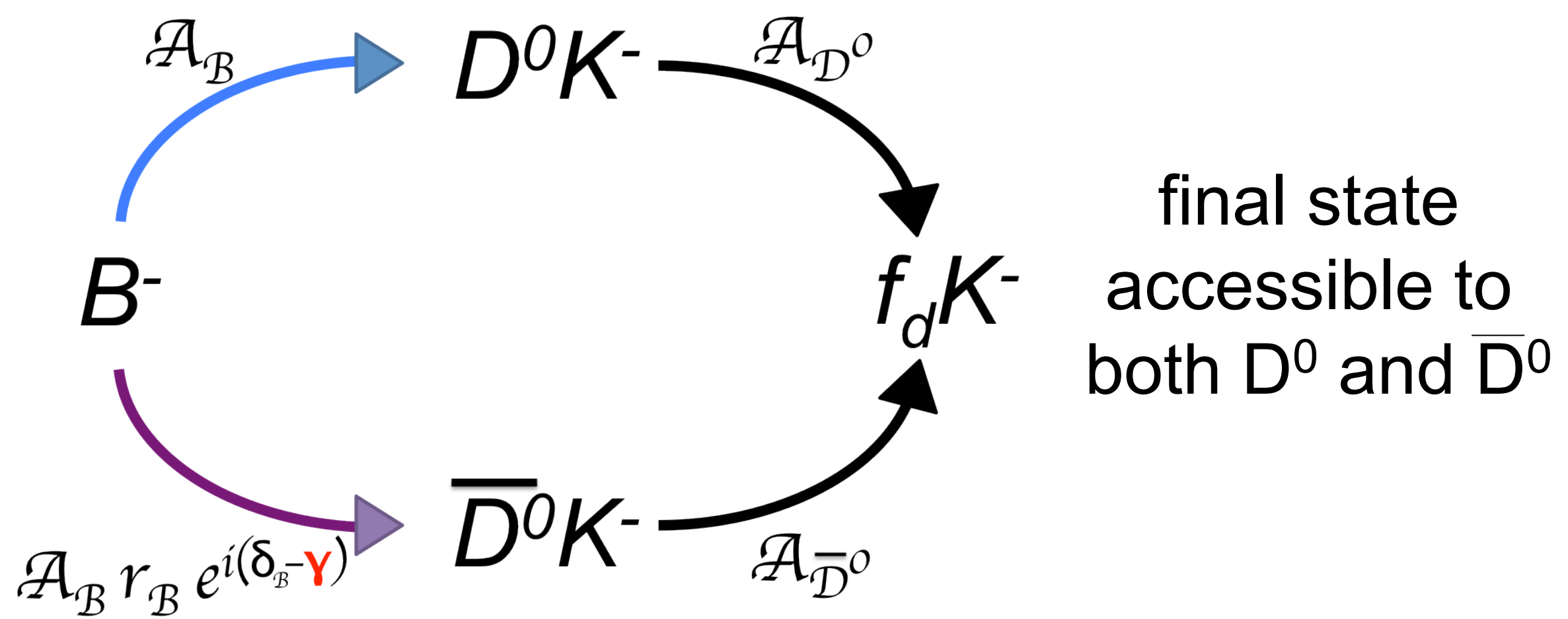


# Towards a model independent measurement of $\gamma$ through $B^\pm \rightarrow D(\rightarrow 4\pi)K^\pm$ decays with LHCb and CLEO-c

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## Measurement of CKM angle $\gamma$ through interference in $B^\pm \rightarrow D(\rightarrow f_D)K^\pm$



### Partial decay width

$$d\Gamma(B \rightarrow D^0(\rightarrow f_D)K^-) \propto A_B^2 \cdot \left( A_{D^0}^2 + r_B^2 A_{\bar{D}^0}^2 + 2r_B \mathbb{R}(A_{D^0} A_{\bar{D}^0}^* e^{-i(\delta_B - \gamma)}) \right) dp$$

$\gamma$  becomes an observable in the interference term

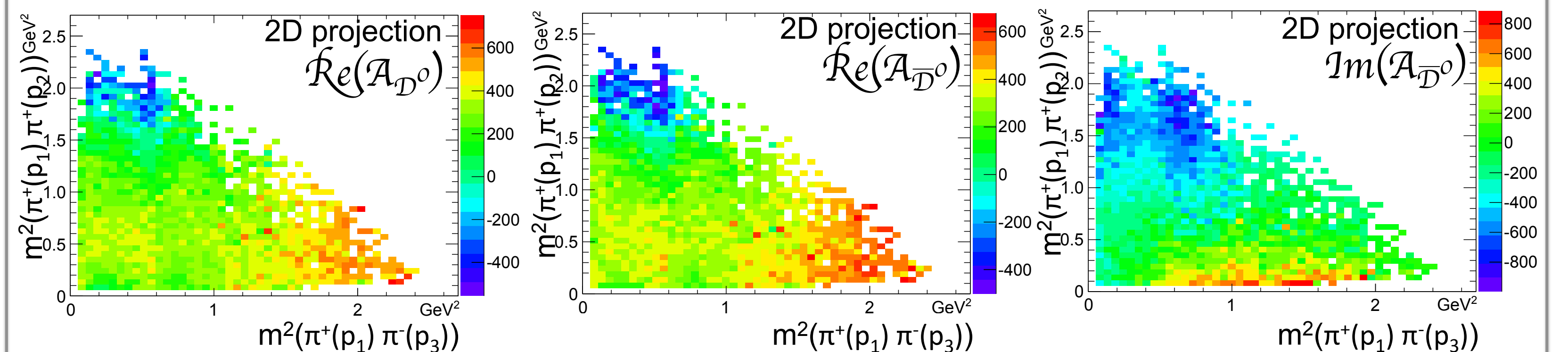
## Reconstruction of the D mesons in self-conjugate

final state  $f_D = \pi^+(p_1) \pi^+(p_2) \pi^-(p_3) \pi^-(p_4)$

$$\begin{aligned} A_{\bar{D}^0}(\pi^+(p_1) \pi^+(p_2) \pi^-(p_3) \pi^-(p_4)) &\stackrel{\text{CP-conjugation}^*}{=} e^{i\Delta\delta(p_1, p_2, p_3, p_4)} A_{D^0}(\pi^+(-p_3) \pi^+(-p_4) \pi^-(-p_1) \pi^-(-p_2)) \\ &\equiv e^{i\Delta\delta} \overline{A_{D^0}} \end{aligned}$$

strong phase difference between  $A_{D^0}$  and  $A_{\bar{D}^0}$

All amplitudes and phases depend on the point in phase space  
→ Dalitz plot analysis in 5 dimensions



In order to extract  $\gamma$  the analysis has to be performed in bins of phase space.

$$\text{Binned decay width: } \frac{d\Gamma}{dp_i + \Delta p} \propto 2r_B \left[ c_i \cos(\delta_B - \gamma) + s_i \sin(\delta_B - \gamma) \right]$$



$$\begin{aligned} c_i &= \frac{1}{N} \int_{p_i}^{p_i + \Delta p} dp \frac{d\Phi}{dp} A_{D^0} \overline{A_{D^0}} \cos(\Delta\delta) \\ s_i &= \frac{1}{N} \int_{p_i}^{p_i + \Delta p} dp \frac{d\Phi}{dp} A_{D^0} \overline{A_{D^0}} \sin(\Delta\delta) \end{aligned}$$

$c_i$  : amplitude-weighted average of  $\cos(\Delta\delta)$

$s_i$  : amplitude-weighted average of  $\sin(\Delta\delta)$

(\*) Assuming no CP-V in the D decays and neglecting 2<sup>nd</sup> order effects from charm mixing

## Model independent determination of $c_i$ and $s_i$ with CLEO-c using correlated D meson pairs from $\Psi(3770) \rightarrow DD$

$c_i$  : Reconstruct  $D \rightarrow 4\pi$  as flavour or CP eigenstate by using **opposite side tagging** and combine information of **CP ( $M_i^\pm$ )** and **flavour ( $K_i$ )** Dalitz plots

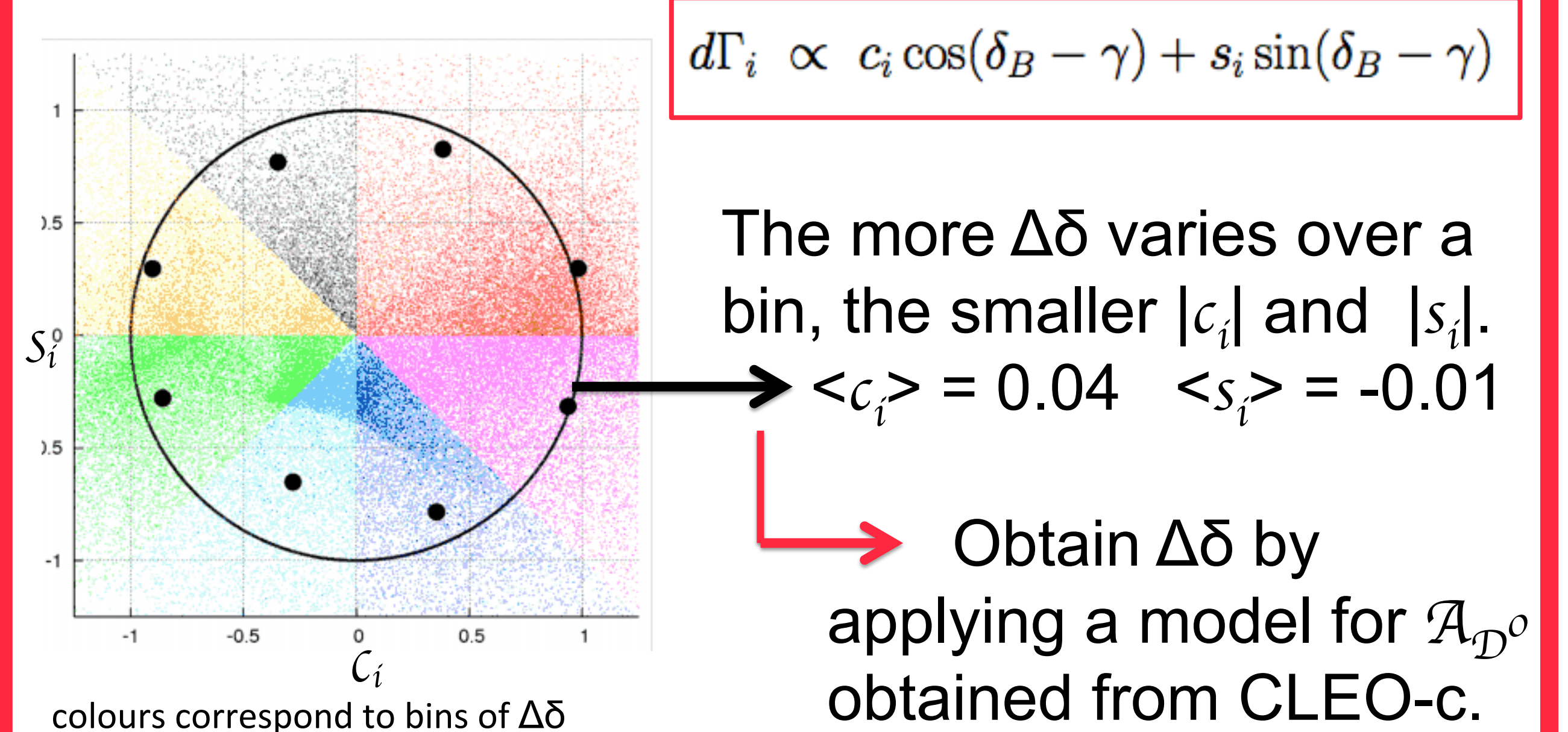
$$\Psi(3770) \rightarrow \left( \pi^+(p_1) \pi^+(p_2) \pi^-(p_3) \pi^-(p_4) \right) \quad M_i^\pm = h_{CP^\pm} \left( K_i \pm 2c_i \sqrt{K_i K_i^*} + K_i^* \right)$$

$s_i$  : Reconstruct  $\Psi(3770) \rightarrow (DD) \rightarrow (4\pi)(4\pi')$  and use **interference between both possible decay paths**

$$\begin{aligned} \Psi(3770) \rightarrow \left( \pi^+(p'_1) \pi^+(p'_2) \pi^-(p'_3) \pi^-(p'_4) \right) &\quad \left( \pi^+(p_1) \pi^+(p_2) \pi^-(p_3) \pi^-(p_4) \right) \\ \text{Event rate in } i^{\text{th}} \text{ bin of first and } j^{\text{th}} \text{ bin of second Dalitz plot:} \\ M_{ij} &= h_{corr} \left( K_i K_j^* + K_i^* K_j - 2\sqrt{K_i K_j^* K_i^* K_j} (c_i c_j + s_i s_j) \right) \end{aligned}$$

## Model inspired binning

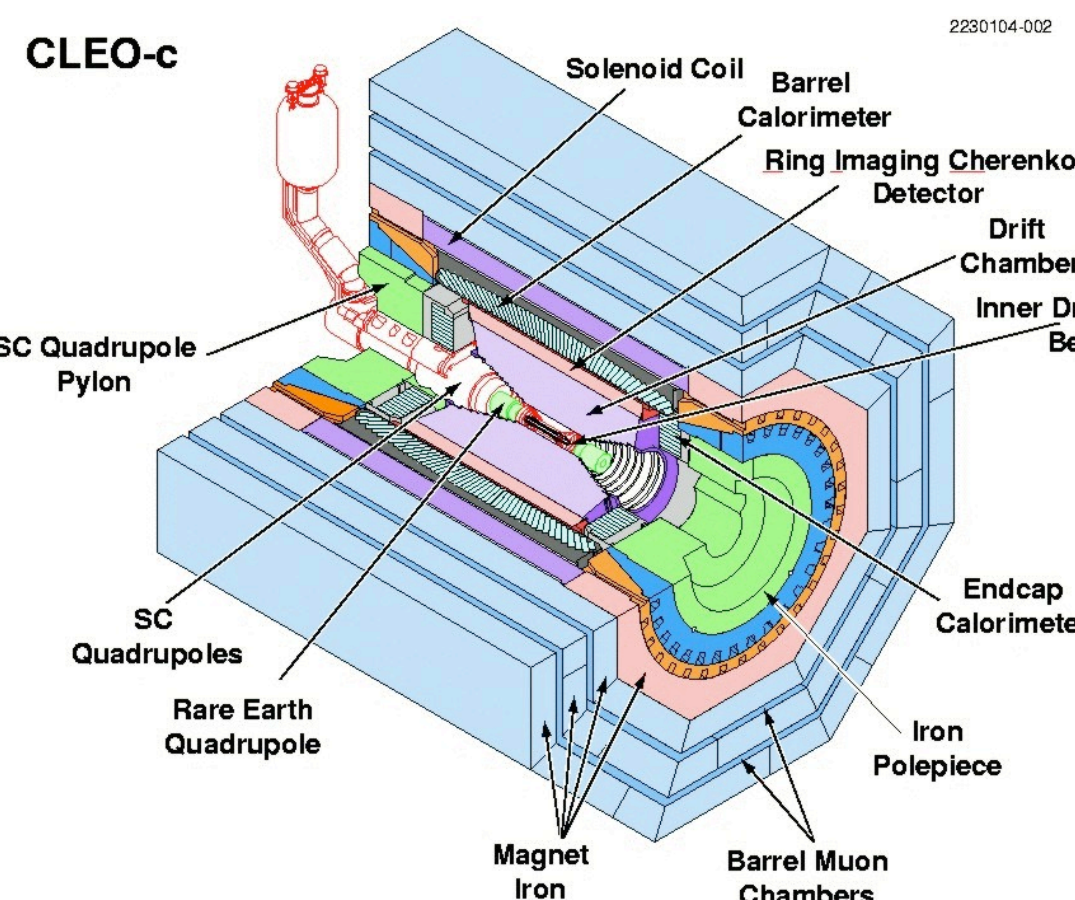
The highest sensitivity to  $\gamma$  can be obtained by using **bins with minimal variation of  $\Delta\delta$** .



Note: The binning only influences the **sensitivity** of the  $\gamma$  measurement but **not the  $\gamma$  value itself**.

## Analysis procedure for the future:

### 1. CLEO-c



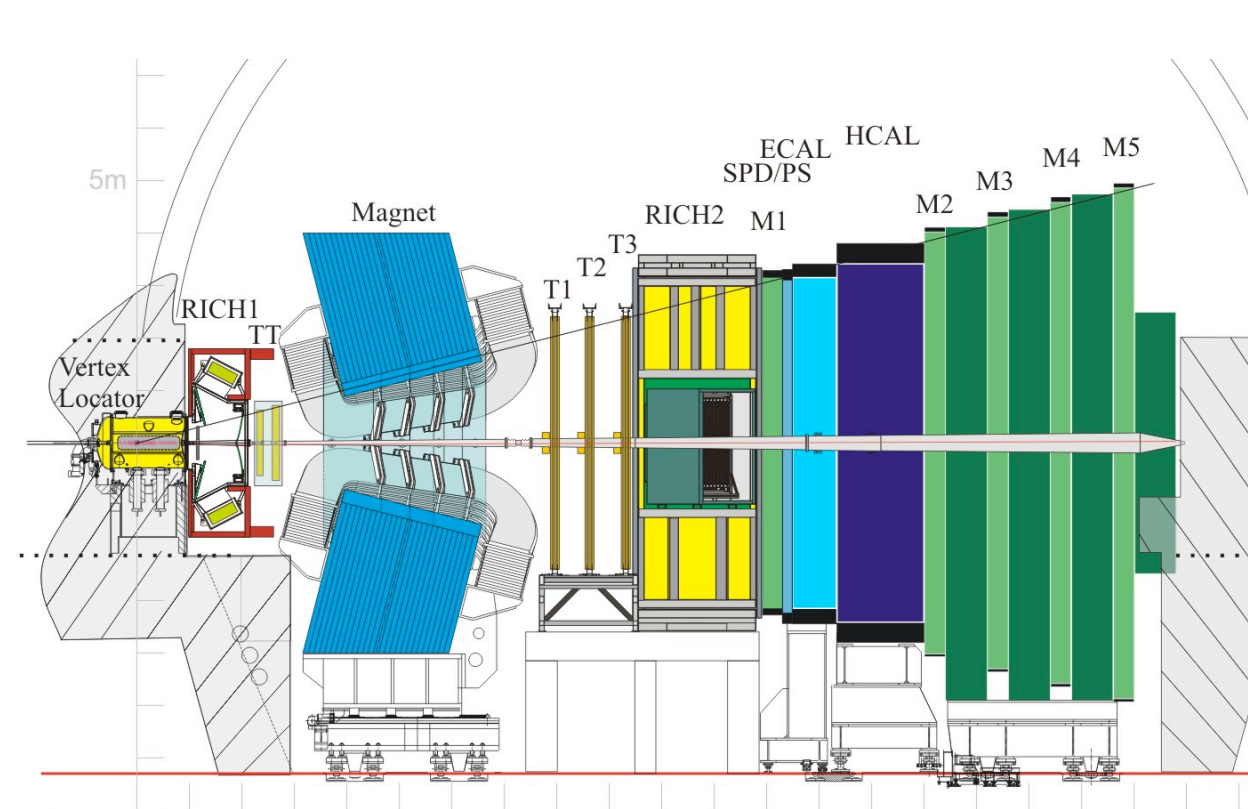
Measurement of  $c_i$  and  $s_i$  using

~ 9500 flavour tagged

~ 1000 CP tagged  $D(\rightarrow 4\pi)$  events

and performing a 5 dimensional fit for each bin in phase space.

### 2. LHCb



Simultaneous fit of  $r_B$ ,  $\delta_B$  and  $\gamma$  in all bins of phase space using

a few  $10^3 B^\pm \rightarrow D(\rightarrow 4\pi)K^\pm$  events

and the  $c_i$  and  $s_i$  extracted from CLEO-c.



