

Chapter 1

Library pdf.autorewrite

Reset *Initial*.

Require Import **Arith**.

Variable *Ack* : **nat**→**nat**→**nat**.

Axiom *Ack0* : $\forall m:\mathbf{nat}, \text{Ack } 0 \ m = \mathbf{S} \ m$.

Axiom *Ack1* : $\forall n:\mathbf{nat}, \text{Ack } (\mathbf{S} \ n) \ 0 = \text{Ack } n \ 1$.

Axiom *Ack2* : $\forall n \ m:\mathbf{nat}, \text{Ack } (\mathbf{S} \ n) \ (\mathbf{S} \ m) = \text{Ack } n \ (\text{Ack } (\mathbf{S} \ n) \ m)$.

Hint Rewrite *Ack0 Ack1 Ack2* :*base0*.

Lemma *RseAck0* : *Ack* 3 2 = 29.

autorewrite with *base0* using try reflexivity. Qed.

Require Import **Omega**.

Variable *g* : **nat**→**nat**→**nat**.

Axiom *g0* : $\forall m:\mathbf{nat}, g \ 0 \ m = m$.

Axiom *g1* : $\forall n \ m:\mathbf{nat}, (n > 0) \rightarrow (m > 100) \rightarrow g \ n \ m = g \ (\mathbf{pred} \ n) \ (m - 10)$.

Axiom *g2* : $\forall n \ m:\mathbf{nat}, (n > 0) \rightarrow (m \leq 100) \rightarrow g \ n \ m = g \ (\mathbf{S} \ n) \ (m + 11)$.

Hint Rewrite *g0 g1 g2* using omega:*base1*.

Lemma *Resg0* : *g* 1 110 = 100.

autorewrite with *base1* using first [progress reflexivity | progress simpl]. Qed.

Lemma *Resg1* : *g* 1 95 = 91.

autorewrite with *base1* using reflexivity || simpl. Qed.