# Different parameter settings

## 1. DATA N

origin

```
By sampling: Model1 data, correct selection 9/10
     Model2 data, correct selection 5/10
By summing: Model1 data, correct selection 7/10
          Model2 data, correct selection 7/10
                                                DATA N = 50
   DATA N increases
```

```
By sampling: Model1 data, correct selection 9/10
          Model2 data, correct selection 9/10
By summing: Model1 data, correct selection 9/10
          Model2 data, correct selection 9/10
```

DATA N = 100

SD = 4

由大數法則可知,隨著試驗次數的增加,事件發生的頻率會趨於一個穩定 值。所以 DATA\_N 的增加能讓模型參數的估計更加穩定,使得正確區分模型 的能力提高。

#### 2. sampleRepeatNum

origin

```
By sampling: Model1 data, correct selection 9/10
           Model2 data, correct selection 5/10
By summing: Model1 data, correct selection 7/10
           Model2 data, correct selection 7/10
```

sampleRepeatNum = 2000000

sampleRepeatNum decreases

```
By sampling: Model1 data, correct selection 6/10
           Model2 data, correct selection 4/10
By summing: Model1 data, correct selection 8/10
           Model2 data, correct selection 5/10
```

sampleRepeatNum = 200

## mu\_prior\_params - standard deviation

origin

```
By sampling: Model1 data, correct selection 9/10
          Model2 data, correct selection 5/10
By summing: Model1 data, correct selection 7/10
          Model2 data, correct selection 7/10
```

SD increases

```
By sampling: Model1 data, correct selection 9/10
        Model2 data, correct selection 7/10
   By summing: Model1 data, correct selection 8/10
        Model2 data, correct selection 8/10 SD = 8
       SD decreases
    By sampling: Model1 data, correct selection 7/10
        Model2 data, correct selection 4/10
    By summing: Model1 data, correct selection 5/10
       Model2 data, correct selection 5/10
                                               SD = 2
   我認為過於嚴格(標準差小)有可能會限制模型,造成表現變差;反之如果
   標準差較大的話,有助於模型靈活調整參數,提升推論效果。
4. sigma_prior_param_a
   • origin
    By sampling: Model1 data, correct selection 9/10
       Model2 data, correct selection 5/10
    By summing: Model1 data, correct selection 7/10
      Model2 data, correct selection 7/10
                                               a = 0.5
   a increases
    By sampling: Model1 data, correct selection 10/10
      Model2 data, correct selection 8/10
    By summing: Model1 data, correct selection 8/10
      Model2 data, correct selection 8/10
   a decreases
    By sampling: Model1 data, correct selection 9/10
       Model2 data, correct selection 5/10
    By summing: Model1 data, correct selection 7/10
     Model2 data, correct selection 5/10
                                               a = 0.4
5. sigma_prior_param_b
   origin
    By sampling: Model1 data, correct selection 9/10
      Model2 data, correct selection 5/10
    By summing: Model1 data, correct selection 7/10
        Model2 data, correct selection 7/10
```

b increases

```
By sampling: Model1 data, correct selection 9/10
        Model2 data, correct selection 7/10
By summing: Model1 data, correct selection 8/10
   Model2 data, correct selection 8/10
                                              b = 8
```

b decreases

```
By sampling: Model1 data, correct selection 7/10
      Model2 data, correct selection 4/10
By summing: Model1 data, correct selection 5/10
    Model2 data, correct selection 5/10
```

Gamma 分布的概率密度函數是:

$$f(x;a,b)=rac{1}{\Gamma(a)b^a}x^{a-1}e^{-x/b}\quad ext{for }x>0$$

其中:

• a 是形狀參數 (shape)

• b 是尺度參數 (scale)

Γ(a) 是 Gamma 函數

平均值:  $\mathbb{E}[X] = a \cdot b$ 變異數:  $Var(X) = a \cdot b^2$ 

所以當 a, b 變大時,變異數也會變大,模型選擇的效果會變好;反之 a, b 變小,效果變差。

## Extra Credit

根據作業提供的相關公式來計算 2-component 的 Maximum likelihood, 並 且使用 Expectation-Maximization Algorithm 來實作

$$\mathbf{P}[x_i | M_2, \mathbf{\mu}_2, \mathbf{\sigma}_2] \ = \ (1 - b) \, \mathcal{N}(x_i; \mathbf{\mu}_{2a}, \mathbf{\sigma}_{2a}) + (b) \, \mathcal{N}(x_i; \mathbf{\mu}_{2b}, \mathbf{\sigma}_{2b})$$

參考: https://chih-sheng-huang821. medium. com/機器學習-em-演算法expectation-maximization-algorithm-em-高斯混合模型-gaussianmixture-model-gmm-和 gmm-em 詳細推導-c6f634410483

```
Data generated with two components
generating data with: m; (\mu 1, \sigma 1); (\mu 2, \sigma 2) = 0.078; (-1.11, 1.63); (-0.83, 3.15)
1-component maximum likelihood: 3.29161e-70
2-component mixture maximum likelihood: 8.63218e-55
Integrals by sampling= (6.588e-58,9.03338e-58) by summing: (3.07579e-58,8.55344e-58)
```

Write in Gaussian poolOrNotl.c

Github: https://github.com/Yun0921/prob\_model\_class/tree/main/HW2