

## Exercise 1 – April 30<sup>th</sup>

For the first exercise of the day, it is proposed that you come back to the demo software: <https://playground.tensorflow.org>, and we will use the spiral dataset again.

On Wednesday we ignored the regularization parameter. Today, we are going to evaluate the role this parameter can play. The input data – or features - will be the two coordinates  $X_1$  and  $X_2$ . The final map will not be displayed in “Discrete Output Mode” in order to better understand how the output of the neural network varies.

We will keep the following hyper-parameters fixed:

- Number of hidden layers (3)
- Number of neurons per layer (8)
- There is a bias term in each neuron calculation.
- Learning rate: 0.03
- ReLU activation

For the first 5 questions we will try to run the network for about 3,500 epochs.

1. How many neural networks parameters are fitted with these hyperparameters?
2. If we take the ratio of training to test equal to 20%, how many training data points do we have? Do you expect over-fitting?
3. Try one run to see what happens with the 20% ratio of training data if we calculate the neural network with no regularization. What do you observe?
4. Now we are going to run the program with different regularization parameters. Write the mathematical expression of the loss function for the two configurations L1 and L2.
5. Recalculate the network for L2 optimization for values of the regularization parameter equal to 0.001, 0.003, 0.01 and 0.03. What do you observe in each case?
6. Now repeat the operation with seven instead of two input data (or features) :  $X_1, X_2, X_1^2, X_2^2, X_1X_2, \sin X_1, \sin X_2$ , keeping all the hyperparameters unchanged. First calculate the network without regularization, then calculate it with a 0.003 regularization coefficient. What do you observe?