

1b) Balancing the forces in the horizontal and vertical directions

$$F_{\text{net},x} = F_s \cos \theta + F_f \cos \theta - F_N \sin \theta = 0$$

$$= F_s \cos \theta + \mu_s F_N \cos \theta - F_N \sin \theta = 0$$

$$\Rightarrow F_N = \frac{F_s \cos \theta}{\mu_s \cos \theta - \sin \theta}$$

$$F_{\text{net},y} = F_s \sin \theta + F_f \sin \theta + F_N \cos \theta - F_g = 0$$

$$= F_s \sin \theta + F_N (\mu_s \sin \theta + \cos \theta) - mg = 0$$

$$= k s_{\min} \left[\sin \theta - \frac{\cos \theta}{\mu_s \cos \theta - \sin \theta} (\mu_s \sin \theta + \cos \theta) \right] - mg = 0$$

$$\Rightarrow s_{\min} = \frac{mg}{k \left[\sin \theta - \cos \theta \frac{\mu_s \sin \theta + \cos \theta}{\mu_s \cos \theta - \sin \theta} \right]}$$

2b) Balancing the forces in the horizontal and vertical directions

$$F_{\text{net},x} = F_s \cos \theta - F_N \sin \theta - F_f \cos \theta = 0$$

$$= F_s \cos \theta - F_N \sin \theta - \mu_s F_N \cos \theta = 0$$

$$\Rightarrow \left| F_N = \frac{F_s \cos \theta}{\sin \theta + \mu_s \cos \theta} \right|$$

$$F_{\text{net},y} = F_s \sin \theta + F_N \cos \theta - F_f \sin \theta - mg = 0$$

$$= F_s \sin \theta + F_N (\cos \theta - \mu_s \sin \theta) - mg = 0$$

$$= k s_{\text{max}} \left[\sin \theta + \cos \theta \frac{\cos \theta - \mu_s \sin \theta}{\sin \theta + \mu_s \cos \theta} \right] - mg = 0$$

$$\Rightarrow s_{\text{max}} = \frac{mg}{k \left[\sin \theta + \cos \theta \frac{\cos \theta - \mu_s \sin \theta}{\sin \theta + \mu_s \cos \theta} \right]}$$