



# Week 12

## Friction and Collisions

### Topics for this week

1. Displacement of friction
2. Modelling collisions

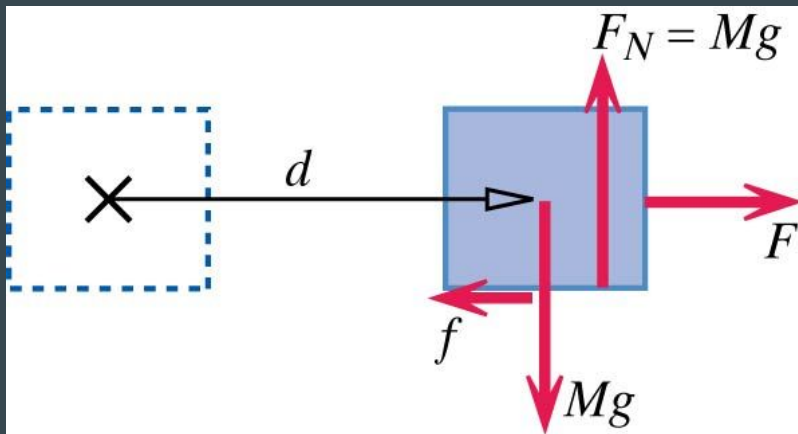
### By the end of the week

1. Be able to make energy predictions involving friction
  2. Analyze the collision of two neutron stars
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# Clicker Question 3

A block of mass  $M$  is pulled at constant speed with force  $F$  a distance  $d$  across a surface. Using the energy principle, what can you say about the change in thermal energy of the block?

- A.  $\Delta E_{\text{thermal}} > 0$
- B.  $\Delta E_{\text{thermal}} = 0$
- C.  $\Delta E_{\text{thermal}} < 0$



# Clicker Question 3 - Solution

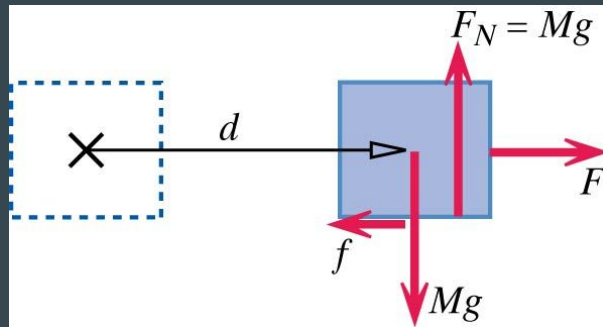
- Apply the energy principle to the center of mass (point particle)

$$\Delta K_{trans} = (F - f)d$$

- Apply the energy principle to the extended system (real system)

$$\Delta K_{trans} + \Delta E_{therm} = (F - f)d$$

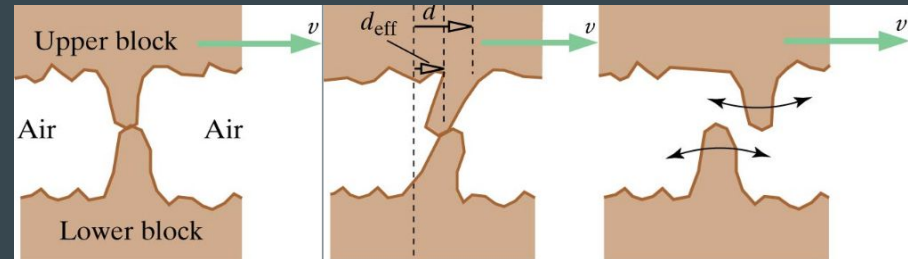
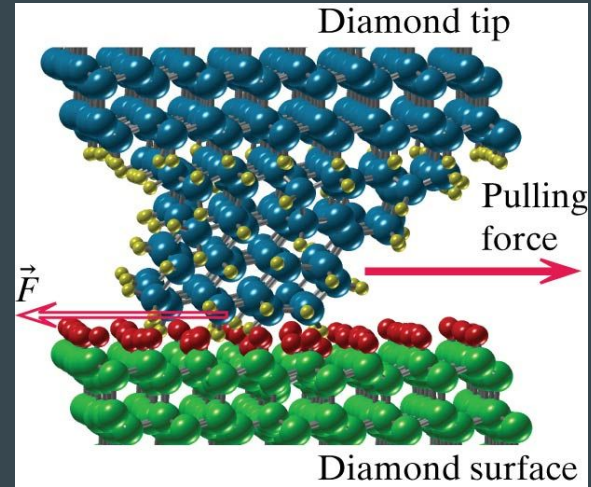
$$\Delta E_{therm} = 0$$





# Displacement of friction forces

- From observation, we know that the thermal energy increases
  - It must be that the applied force and the friction force do not move through the same displacement!
- At the atomic level surfaces are not flat but irregular
  - As few as three asperities make contact
  - The very high loads at these contact regions result in adhesion and deformation
    - The contact force displacement is different from the system
  - Vibration of the asperities results in an increase in thermal energy for the system







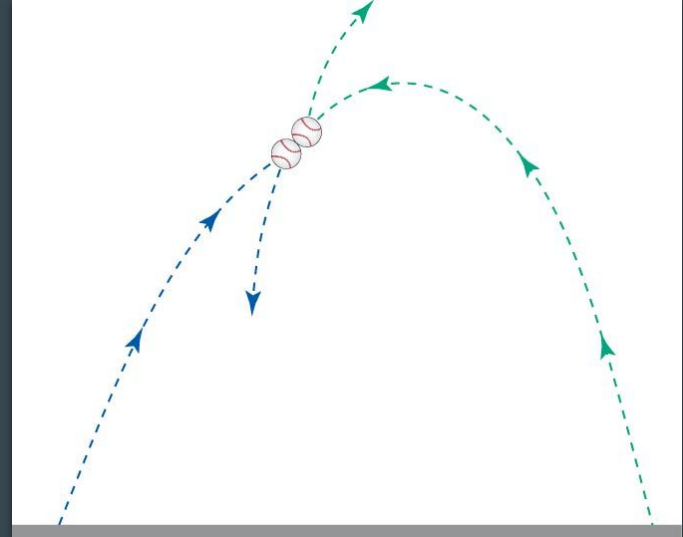
# Collisions

# Collisions

- An interaction between two objects that takes place in a short amount of time
  - The interaction between the two objects is much larger than other interactions with the surroundings
  - The objects do not have to make physical contact
  - Valid at all length scales

$$\Delta \vec{p}_{system} = 0$$

$$\Delta E_{system} = 0$$



# Example: A bounced ball

A ball whose mass is 0.1 kg falls and hits the floor with a speed of 6 m/s, then rebounds upward with a speed of 5 m/s. If the ball was in contact with the floor for approximately  $12 \times 10^{-3}$  seconds, how much larger is the collision force compared to the gravitational force?





# Example: A bounced ball - Solution

- Use the momentum principle to estimate the collision force

$$\Delta \vec{p}_{ball} = \vec{F}_{net} \Delta t$$

$$m(\vec{v}_f - \vec{v}_i) = (F_{contact} - mg)\hat{y}\Delta t$$

$$\frac{m(\vec{v}_f - \vec{v}_i)}{\Delta t} + mg\hat{y} = \vec{F}_{contact}$$

$$|\vec{F}_{contact}| \approx 100 |\vec{F}_{grav}|$$



# Classifying collisions

- By convention we classify collisions based on the change of internal energy for the system of colliding objects
  - Elastic Collision: No change in internal energy for the system
    - The system doesn't change shape, temperature, etc.
    - This is an idealization for macroscopic collisions due to dissipation

$$\Delta K = 0$$

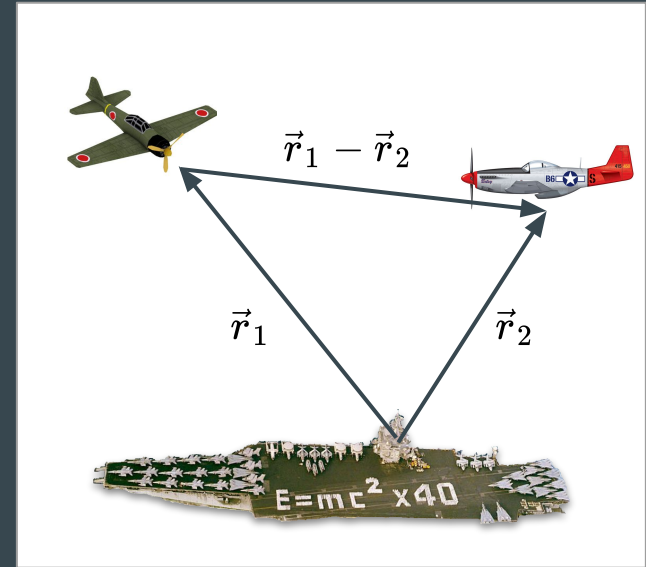
- Inelastic Collision: There is some change in internal energy for the system
    - The system changes shape, temperature, etc.
    - Maximally Inelastic Collisions are when the colliding objects stick together
    - <http://www.youtube.com/watch?v=QfDoQwIAaXg>
- In all types of collisions, momentum and total energy are conserved during the collision of the two objects

# Changing the reference frame

- A frame of reference is a perspective from which a system is observed
  - Collision problem can often be simplified by changing to a moving (inertial) frame of reference
    - An inertial frame is one that is not accelerating
    - Sometimes the center of mass
- Consider tracking the position of two planes about to collide from a stationary ship
  - The ship measures the velocity of each plane  $\vec{v}_1$  and  $\vec{v}_2$
  - The velocity of plane 1 as measured by plane 2:

$$\vec{v}'_1 = \vec{v}_1 - \vec{v}_2$$

$$\vec{v}' = \vec{v}_{stationary} - \vec{v}_{moving}$$



# Example: Super Bounce

A tennis ball of mass  $m$  perched on top of a basketball of mass  $M$  falls from rest towards the Earth from a height  $h$ . The basketball & tennis ball collide with the ground in an elastic collision. The basketball mass is much larger than the tennis ball. How high does the tennis ball bounce?



# Example: Super Bounce Soln.

- How fast are the balls moving when they reach the ground?
  - Both balls and the Earth in the system with energy conservation

$$\Delta K_{trans} + \Delta U_{grav} = 0$$

$$\vec{v}_0 = -\sqrt{2gh}\hat{y}$$

- The tennis ball collides with the Earth first
  - The Earth is much larger and doesn't move
  - The collision happens so fast the tennis ball is still moving down

$$\vec{v}_{basketball} = \sqrt{2gh}\hat{y}$$

$$\vec{v}_{tennis} = -\sqrt{2gh}\hat{y}$$



# Example: Super Bounce Soln.

- The tennis ball collides with the basketball
  - What would a small bug riding on the basketball predict?

- Before the collision

$$\vec{v}' = \vec{v}_{stationary} - \vec{v}_{moving}$$

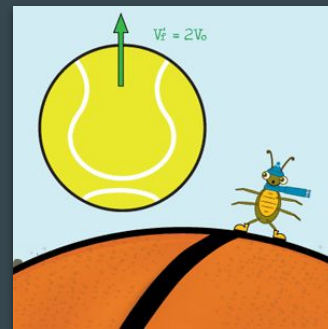
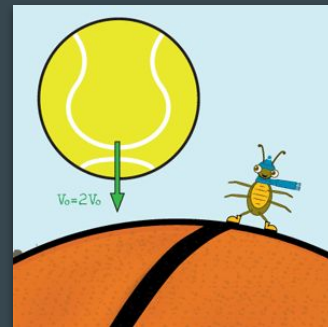
$$\vec{v}' = \vec{v}_{tennis} - \vec{v}_{basketball}$$

$$\vec{v}' = -\sqrt{2gh}\hat{y} - \sqrt{2gh}\hat{y}$$

$$\vec{v}' = -2\sqrt{2gh}\hat{y}$$

- After the collision

$$\vec{v}'_f = 2\sqrt{2gh}\hat{y}$$





# Example: Super Bounce Soln.

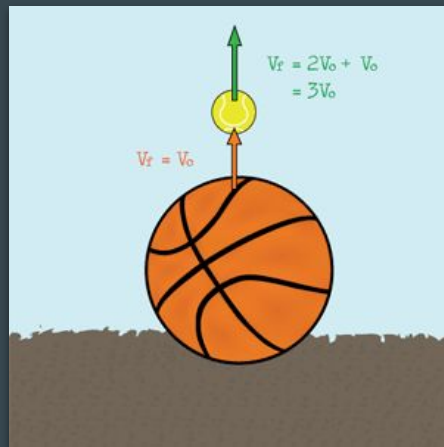
- Determine how fast the tennis ball is moving with respect to the stationary frame (the Earth)

$$\vec{v}_{stationary} = \vec{v}' + \vec{v}_{moving}$$

$$\vec{v}_{tennis,f} = 2\sqrt{2gh}\hat{y} + \sqrt{2gh}\hat{y}$$

$$\vec{v}_{tennis,f} = \sqrt{18gh}\hat{y}$$

- How high does this ball go?
  - Using energy conservation again
  - Final height is 9 times the drop height!
  - What happens if we have three stacked balls?



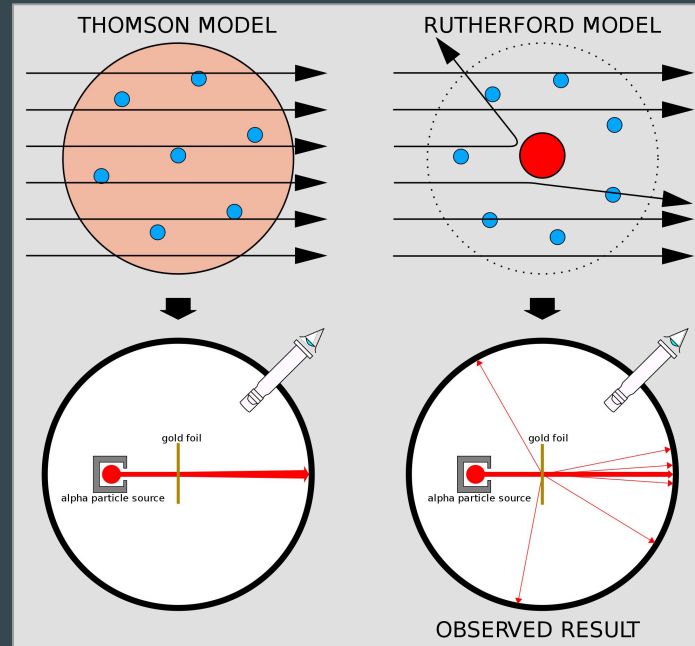
# The Plum Pudding model of matter

- In 1877 JJ Thomson proposed the “plum pudding” model of the atom
  - A positive charged “cake” of uniform density with tiny negative “raisins” distributed throughout
  - Based on Thomson’s earlier experiment demonstrating the existence of point like electrons
- In 1911 Ernest Rutherford and a team of scientist set out to determine the distribution of electrons in the plum pudding model of the atom
  - The Rutherford team decided to bombard gold foil with high energy alpha particles
    - Helium nuclei (2 protons and 2 neutrons)
    - Discovered by Marie and Pierre Curie



# Rutherford's Gold Foil experiment

- Rutherford expected the heavy alpha particles to rip through the gold foil like a bullet through tissue paper!
  - Instead some alpha particles bounced back or were deflected at large angles
  - “It was quite the most incredible event that has ever happened to me in my life.”
  - Rutherford proposed the existence of a nucleus that was massive and much smaller than the atom
- How did Rutherford arrive at this conclusion, and how did he make his estimate for the size of the nucleus?
  - Examining the interaction as an elastic collision



# Computationally modelling the interaction

- We could solve for the final momentum by using conservation of momentum and energy as Rutherford did.
  - It is easier to model this in computationally using the electric force between a gold nucleus and an alpha particle
  - [https://www.glowscript.org/#/user/ed/folder/My\\_Programs/program/Rutherford](https://www.glowscript.org/#/user/ed/folder/My_Programs/program/Rutherford)

