

An aerial photograph of a narrow asphalt road winding through a thick forest of green trees. A yellow cab-over-engine truck is driving away from the camera on the road. The background is filled with the tops of many trees.

Shortest route

to success

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Public

ORTEC

Together we increase our impact on the world



About ORTEC

- Flag icon: Founded in 1981
- Building icon: Offices in 13 countries
- Envelope icon: 1.200 customers
- People icon: > 1.000 employees



ORTEC



At ORTEC... we make drivers happy!

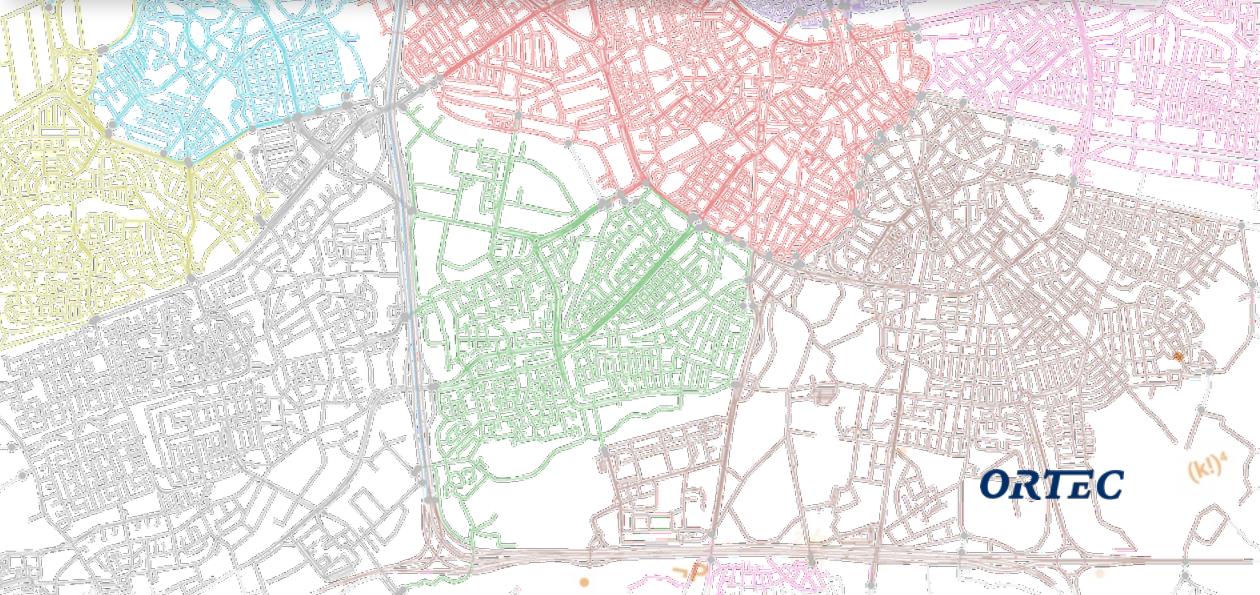
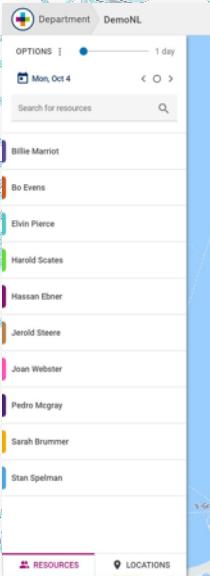
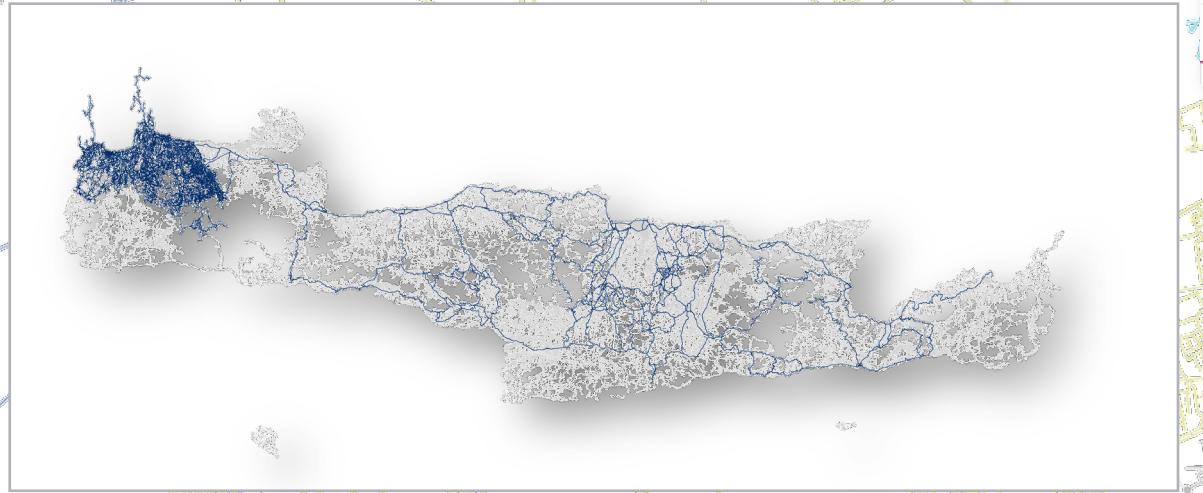




What does that mean?

“
*We plan routes over roads
We take into account traffic
We don’t make drivers wait
(but we do give them breaks)*
”

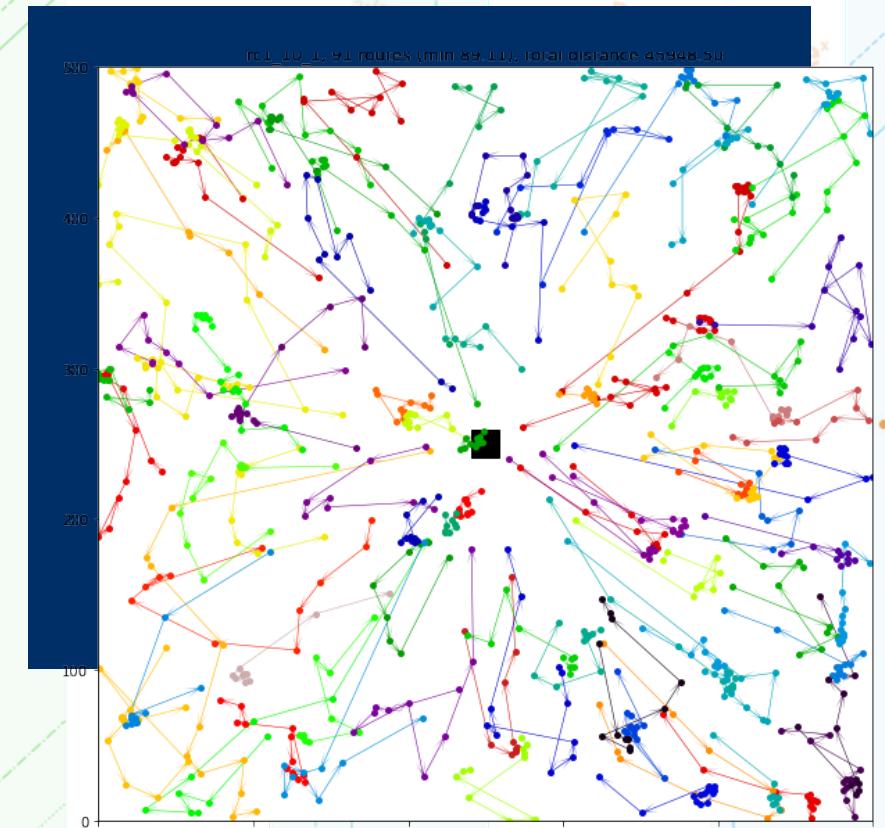
Routing @ ORTEC



In the VRPTW challenge

- We drive as the crow flies
- There is no traffic
- We wait a lot
- (maybe that's why we don't take breaks)

6



We need
something
special

ORTEC

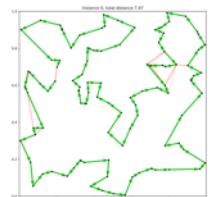
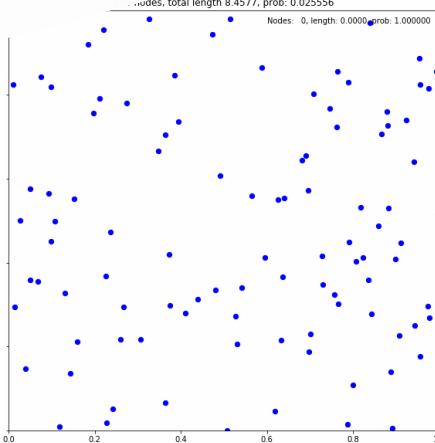
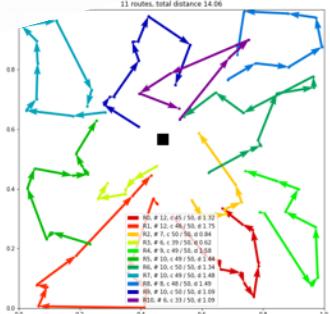
Meet academic me

ATTENTION, LEARN TO SOLVE ROUTING PROBLEMS!

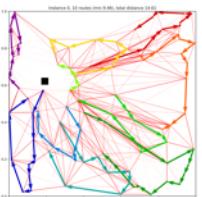
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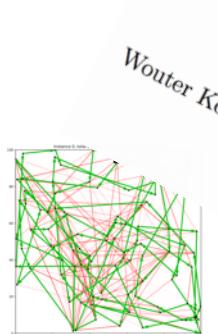
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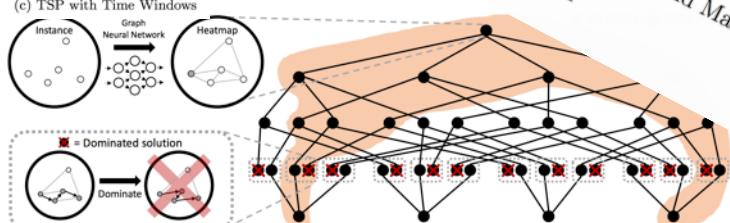
(a) Travelling Salesman Problem



(b) Vehicle Routing Problem



(c) TSP with Time Windows





What you get for 25 000 000 \$

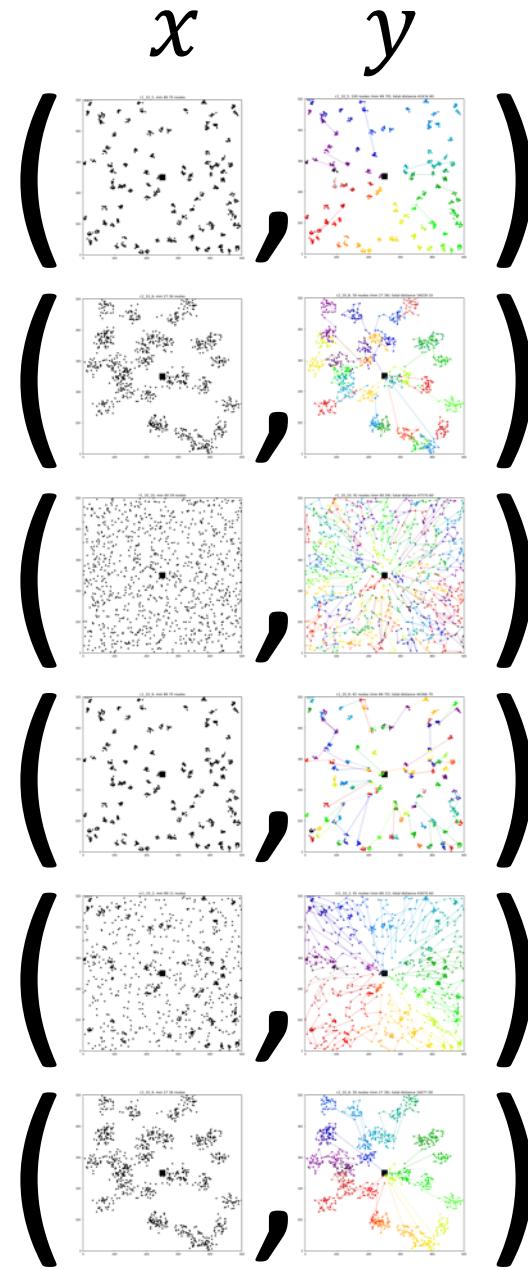
!!

*Training machine
learning models takes
a lot of time and effort*

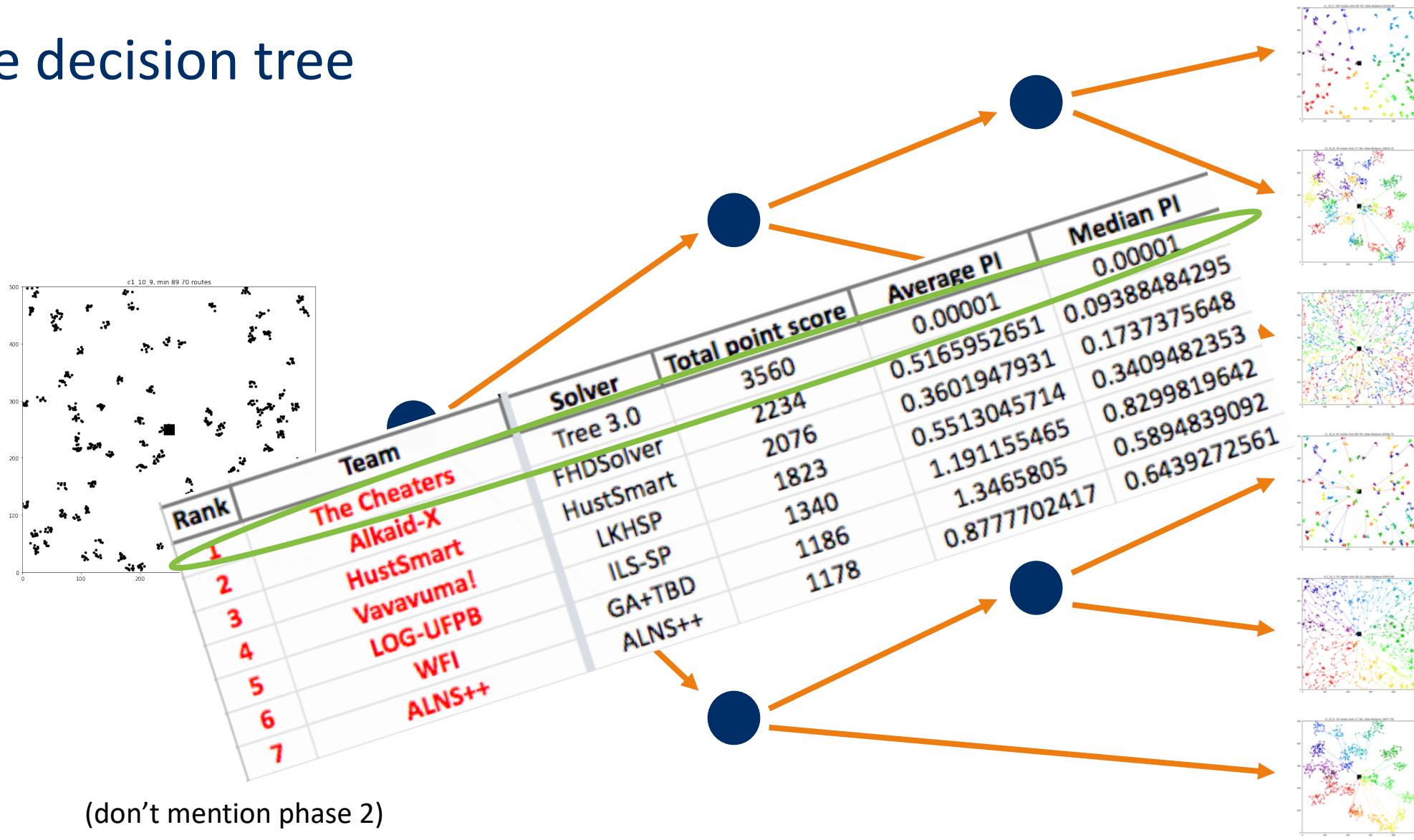
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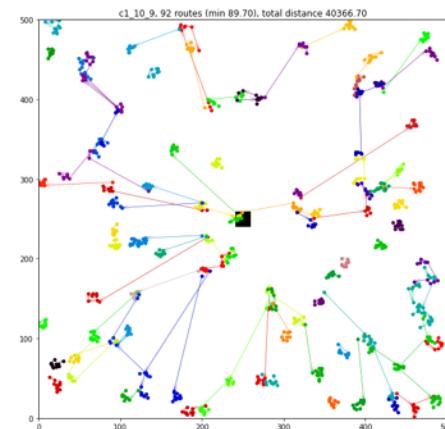
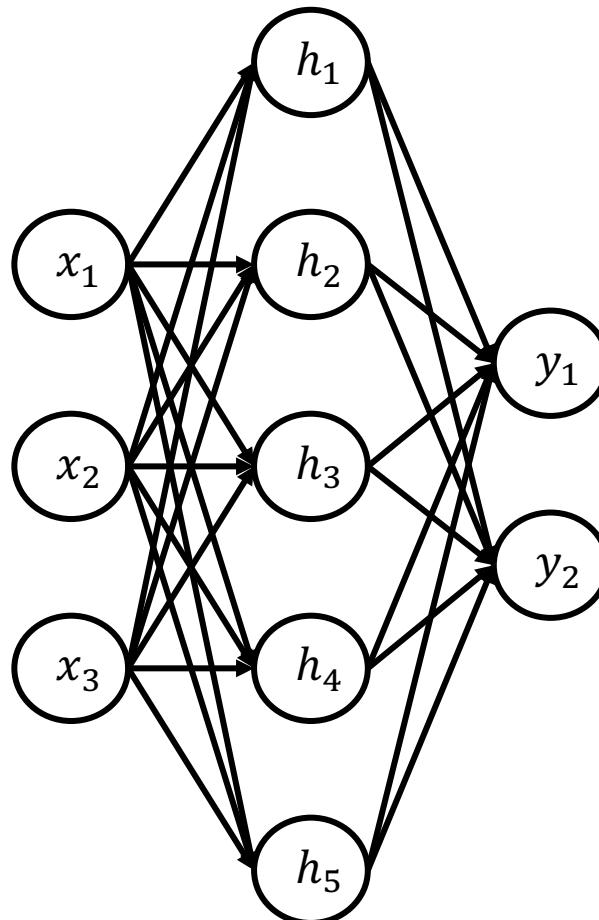
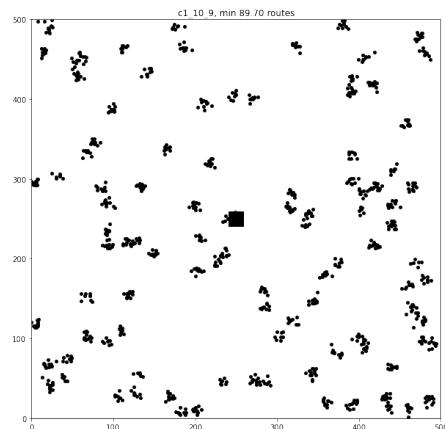
The dataset



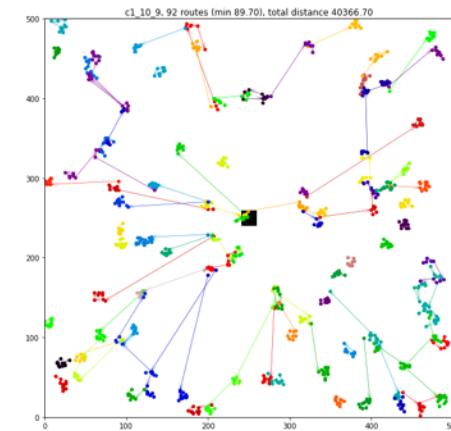
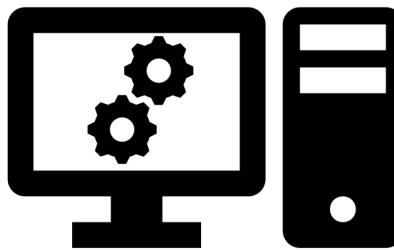
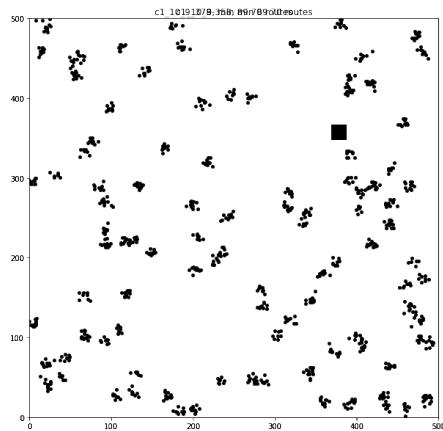
The decision tree



The neural network



The heavily tuned algorithm



Conclusion

A photograph of two people, a man and a woman, looking at a large screen displaying complex data. The man is wearing glasses and a yellow hoodie, pointing at the screen. The woman is wearing a white shirt and blue-rimmed glasses. In the foreground, a person's hands are visible on a keyboard.

No machine learning here ☹
Use good old **human** intelligence?

The recipe (by culinary me)

1 open-source repo

A screenshot of a GitHub repository page for "HGS-CVRP: A modern implementation of the Hybrid Genetic Search for the CVRP". The page shows the repository structure, recent commits, and a detailed description of the algorithm. It includes sections for "Contributors" (Thibaut Vidal) and "References".

1+ excellent paper

A hybrid genetic algorithm with adaptive diversity management for a large class of vehicle routing problems with time-windows

Thibaut Vidal Teodor Gabriel Crainic^a, Michel Gendreau^b, Christian Prins^a

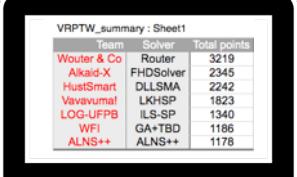
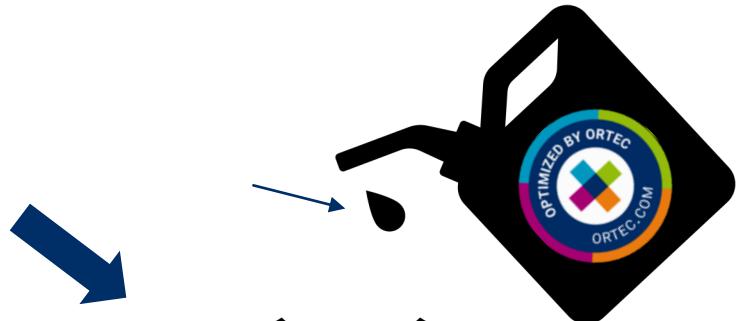
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Available online 31 July 2012
Keywords: Vehicle routing problems Time windows Hybrid genetic algorithm Diversity management Neighborhood search Decomposition
ABSTRACT
The paper presents an efficient Hybrid Genetic Search with Advanced Diversity Control for a large class of time-constrained vehicle routing problems, introducing several new features to manage the diversity of solutions. New local search techniques are introduced, accounting for improved infeasible solutions with respect to time-windows and duration constraints and allowing for evaluated moves from any classical neighbourhood based on arc or node constraints in amortized constant time. Furthermore, geometric and combinatorial problem decompositions are developed to address efficiently large planning problems. The proposed algorithms perform a turn-of-the-century performance on classical literature benchmark instances for any combination of periodic, multi-depot, site-dependent, and duration-constrained vehicle routing problem with time windows.
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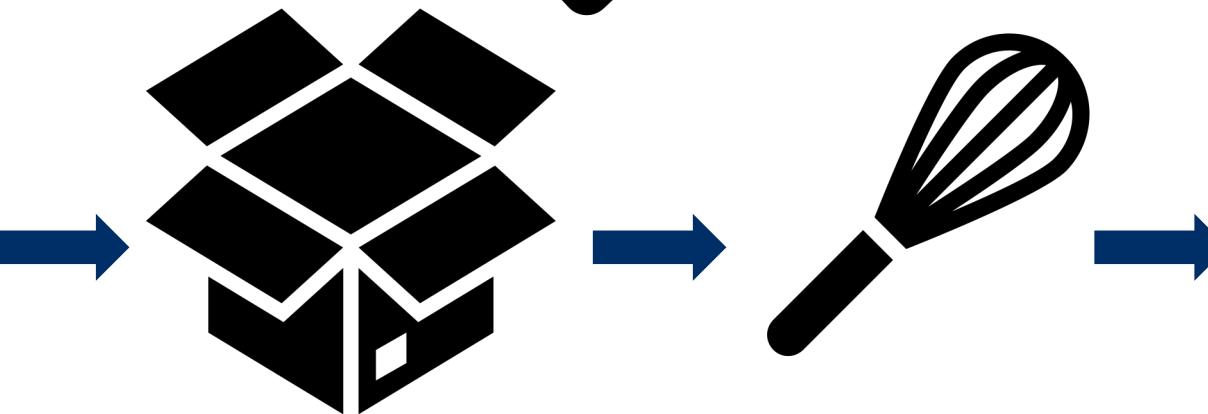
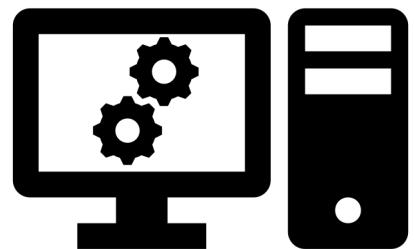
6 intelligent colleagues



Add some oil



Submit & wait for results

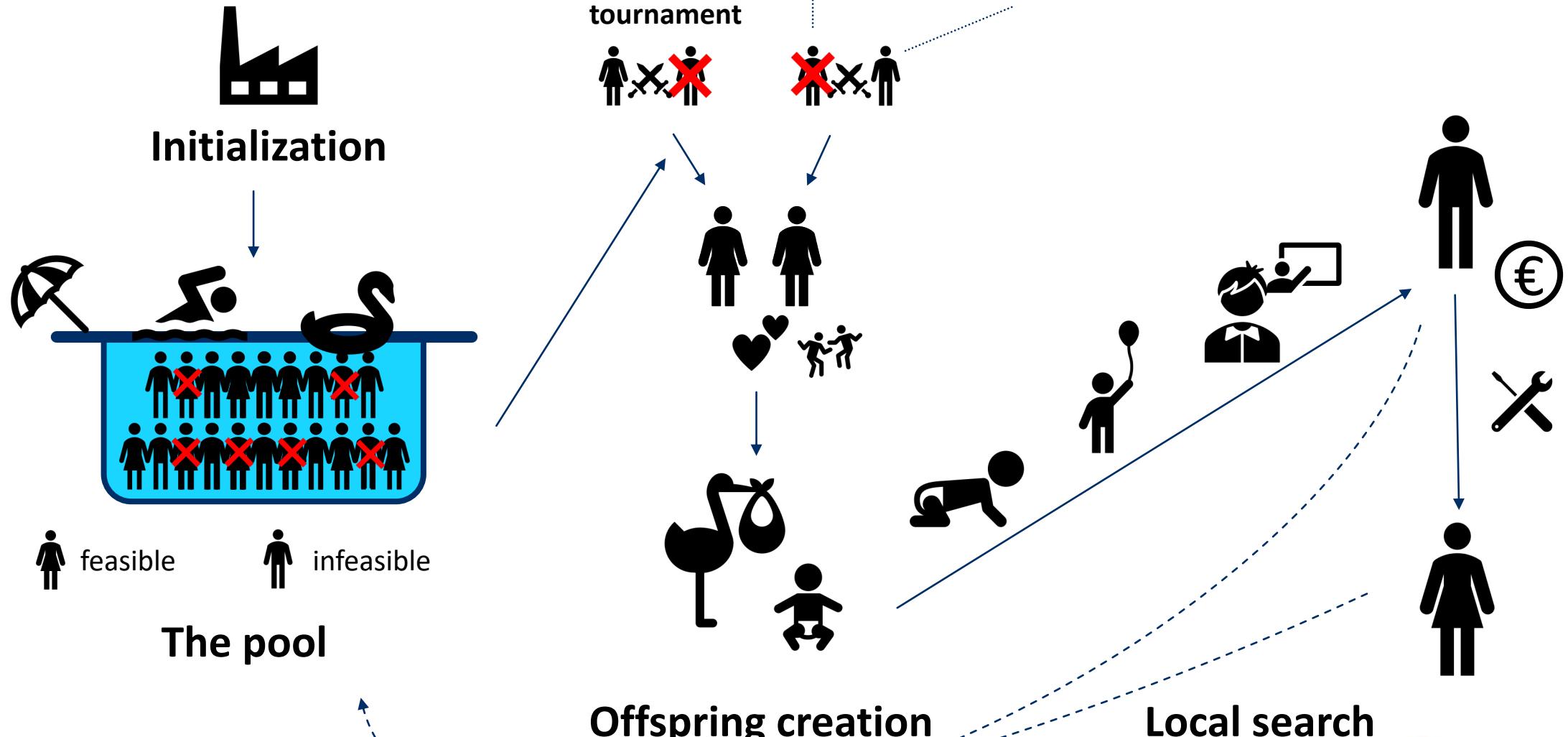


Put in a black box
(a.k.a. online meeting)

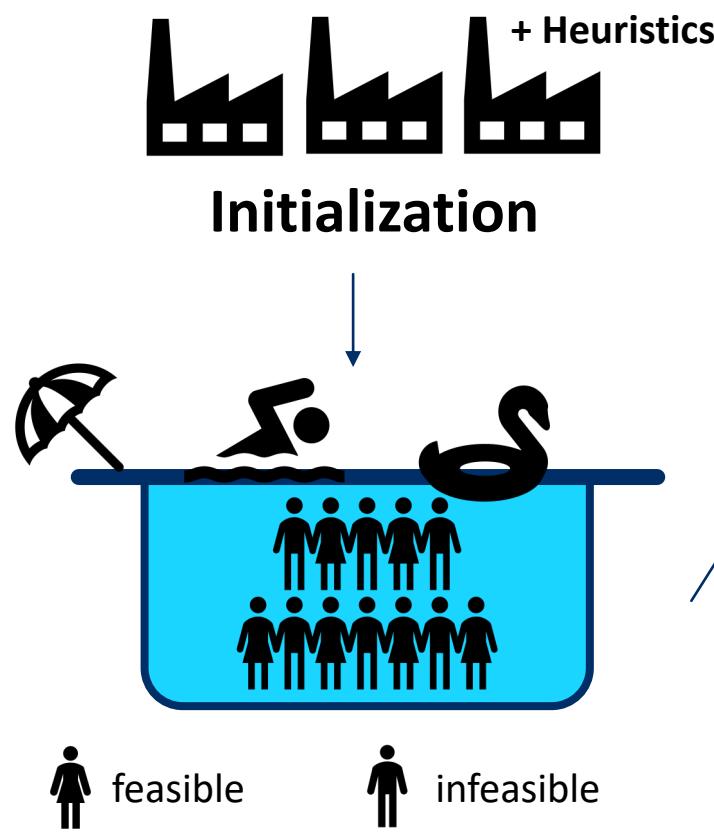
Mix for 1 week

Run algorithm for 3 days

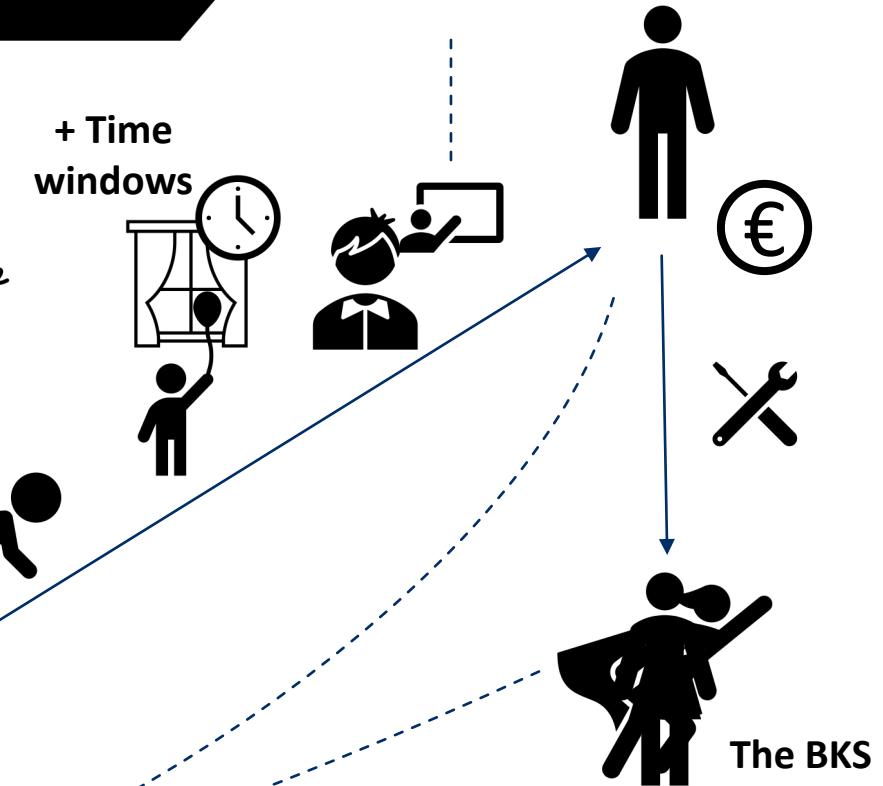
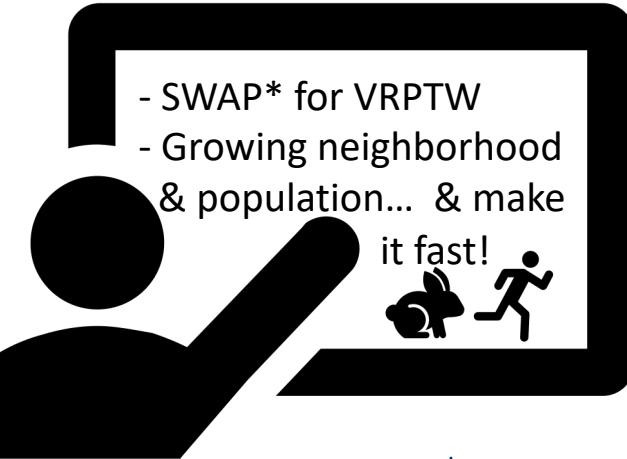
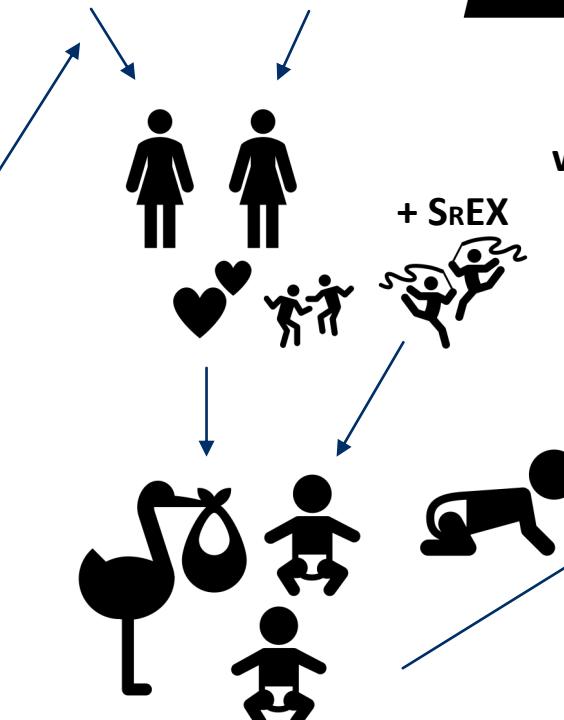
Hybrid Genetic Search



What did we do?



The binary tournament



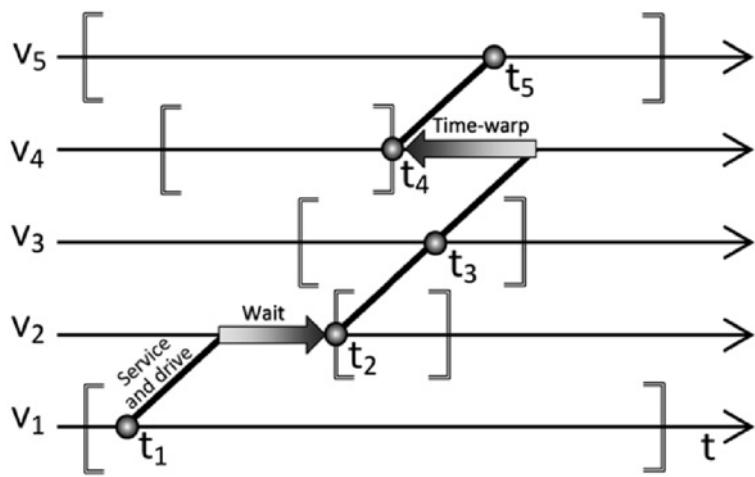


Fig. 1. Illustration of waiting times and time warps.

Proposition 1 (Concatenation of two sequences). Let $\sigma = (\sigma_i, \dots, \sigma_j)$ and $\sigma' = (\sigma'_i, \dots, \sigma'_{j'})$ be two subsequences of visits. The concatenated subsequence $\sigma \oplus \sigma'$ is characterized by the following data:

$$D(\sigma \oplus \sigma') = D(\sigma) + D(\sigma') + \delta_{\sigma_j \sigma'_i} + \Delta_{WT} \quad (5)$$

$$TW(\sigma \oplus \sigma') = TW(\sigma) + TW(\sigma') + \Delta_{TW} \quad (6)$$

$$E(\sigma \oplus \sigma') = \max\{E(\sigma') - \Delta, E(\sigma)\} - \Delta_{WT} \quad (7)$$

$$L(\sigma \oplus \sigma') = \min\{L(\sigma') - \Delta, L(\sigma)\} + \Delta_{TW} \quad (8)$$

$$C(\sigma \oplus \sigma') = C(\sigma) + C(\sigma') + c_{\sigma_j \sigma'_i} \quad (9)$$

$$Q(\sigma \oplus \sigma') = Q(\sigma) + Q(\sigma') \quad (10)$$

where $\Delta = D(\sigma) - TW(\sigma) + \delta_{\sigma_j \sigma'_i}$, $\Delta_{WT} = \max\{E(\sigma') - \Delta - L(\sigma), 0\}$ and $\Delta_{TW} = \max\{E(\sigma) + \Delta - L(\sigma'), 0\}$.

Supporting time windows

- Use time-warp principle
- Cache computation for prefix and postfix of routes
- Use two-level hierarchy for fast queries in middle of route
- Penalty booster: increase penalty by 100% if no feasible solution found

Initial heuristics

- 85% random:
 - Randomly order nodes
 - Split into routes using SPLIT algorithm (Vidal, 2012)
- 5% farthest, 5% nearest insertion:
 - Insert the node with shortest detour (given this is feasible)
 - If no feasible insertion, start new route with farthest/nearest node from depot
- 5% sweep:
 - Sort by angle to depot and add until capacity violated
 - For each route, sort customers with short time windows by time
 - For each route, insert customers with long time windows by shortest detour

Offspring generation

Selective Route Exchange (SREX)

540 Y. Nagata and S. Kobayashi

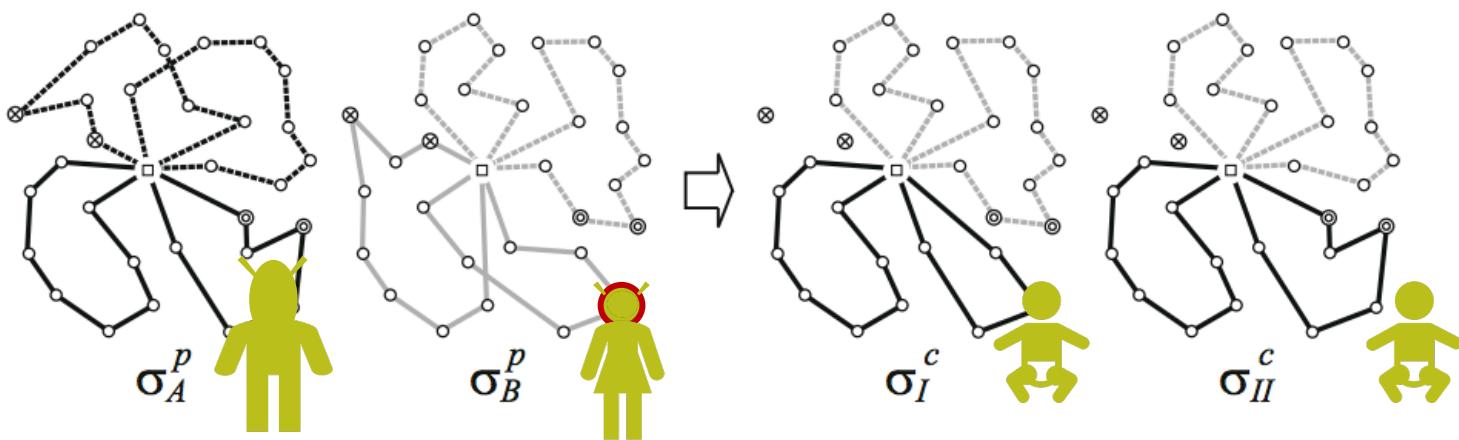


Fig. 1. Illustration of the SREX. σ_A^p and σ_B^p are parents. Routes S_A and S_B are represented as dotted lines, customer nodes $V_{A \setminus B}$ are represented by circles with x-mark, and the customer nodes in $V_{B \setminus A}$ are represented by double circles. σ_I^c and σ_{II}^c are intermediate offspring solutions obtained after Step 2.

Source: Nagata et al. 2010

Ordered Crossover (OX)

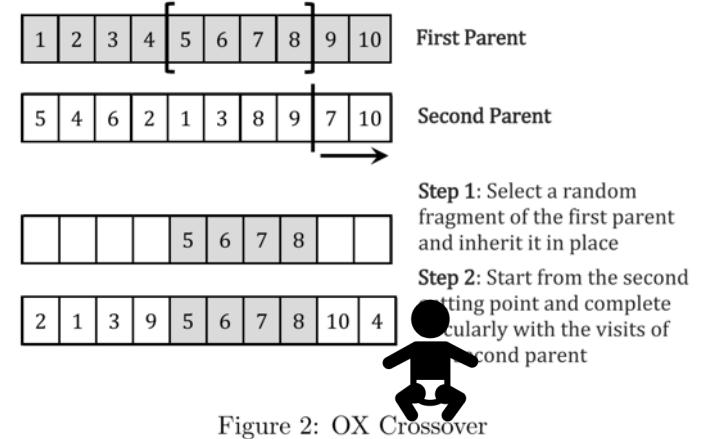


Figure 2: OX Crossover

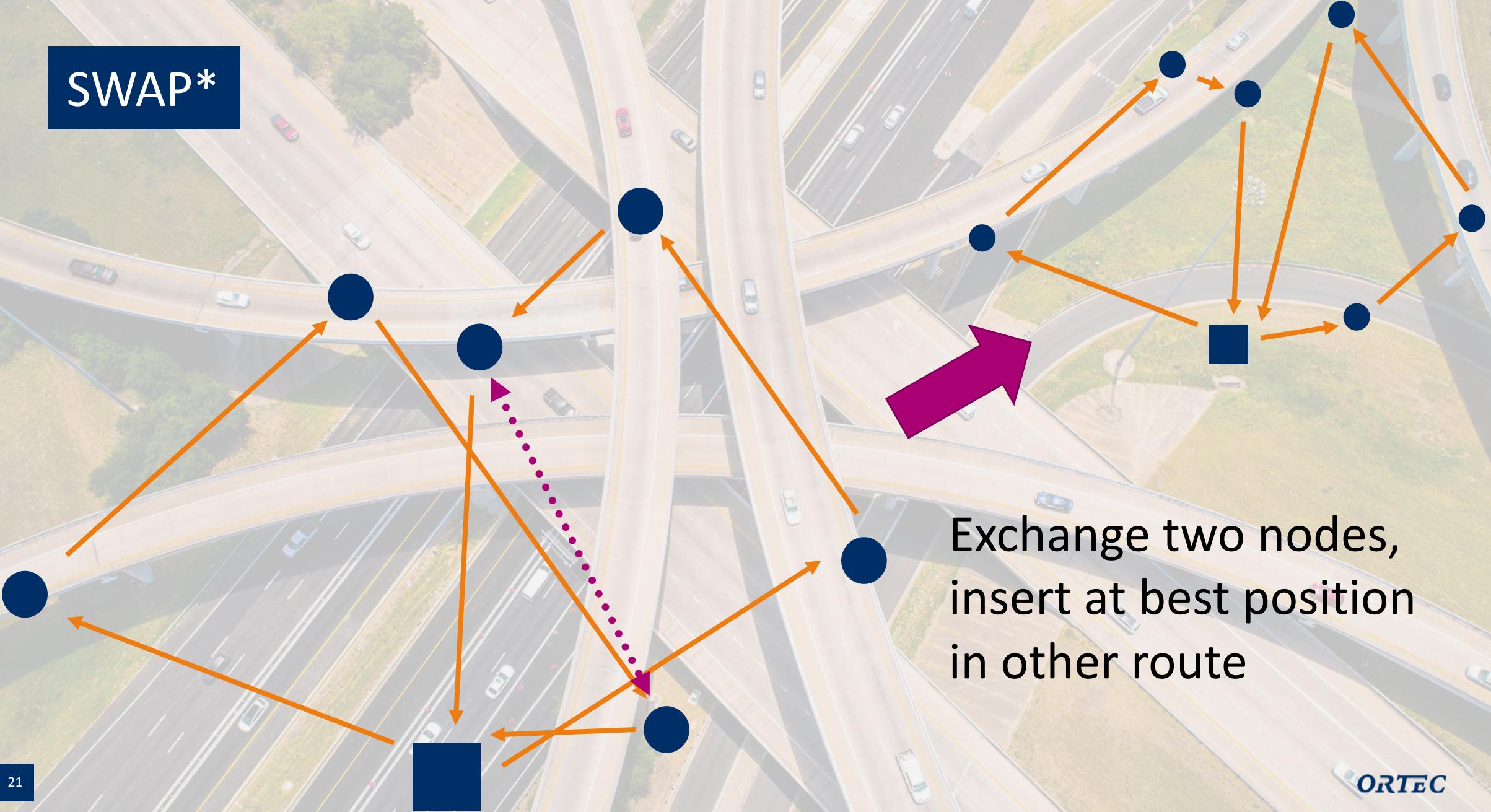
Source: Vidal 2021

Local search

- SWAP, RELOCATE, 2-OPT, 2-OPT*
- Moves between near neighbors
- Smart ‘pre-checks’
- SWAP*, see next slide

SWAP*

Exchange two nodes,
insert at best position
in other route

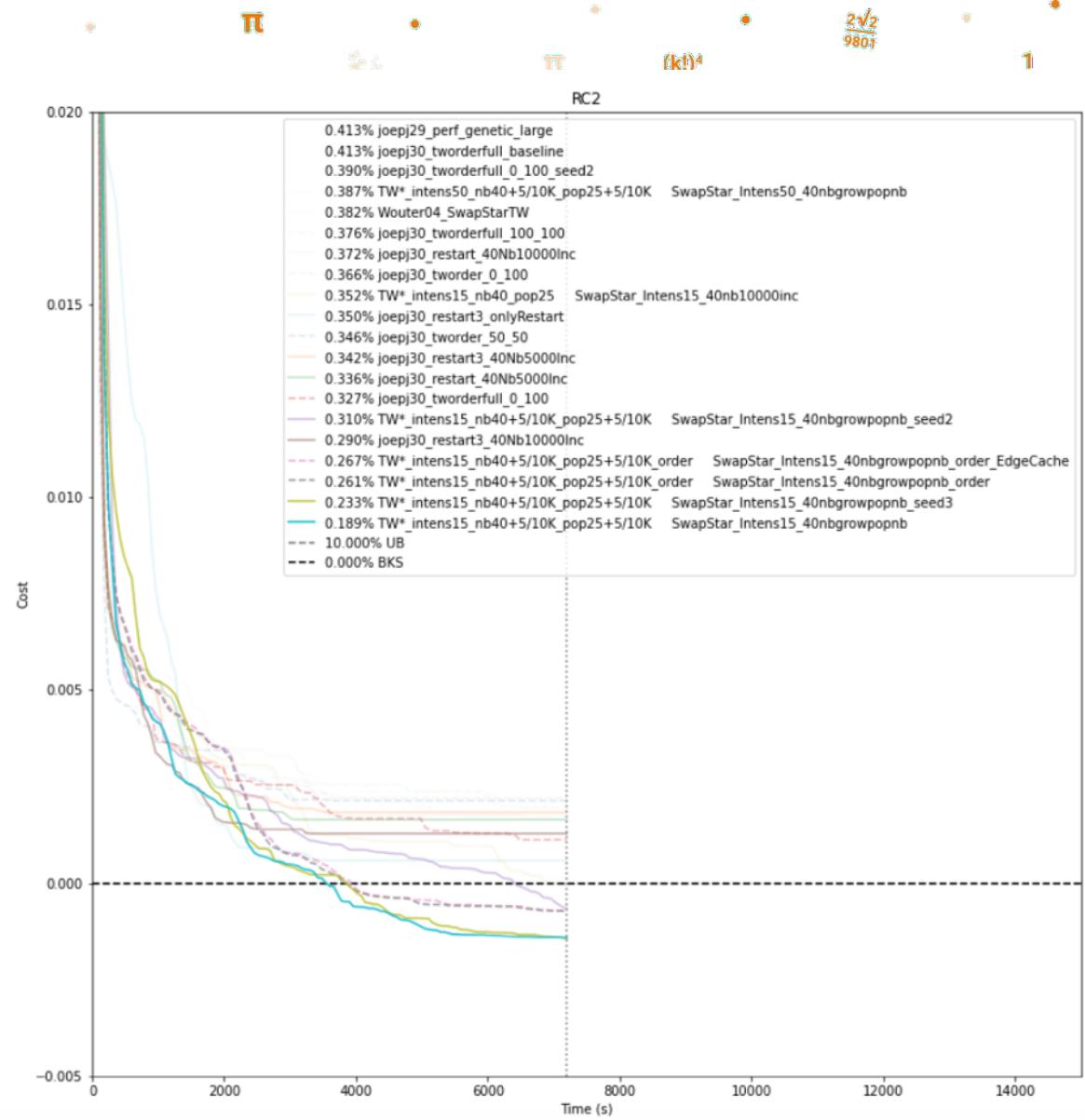
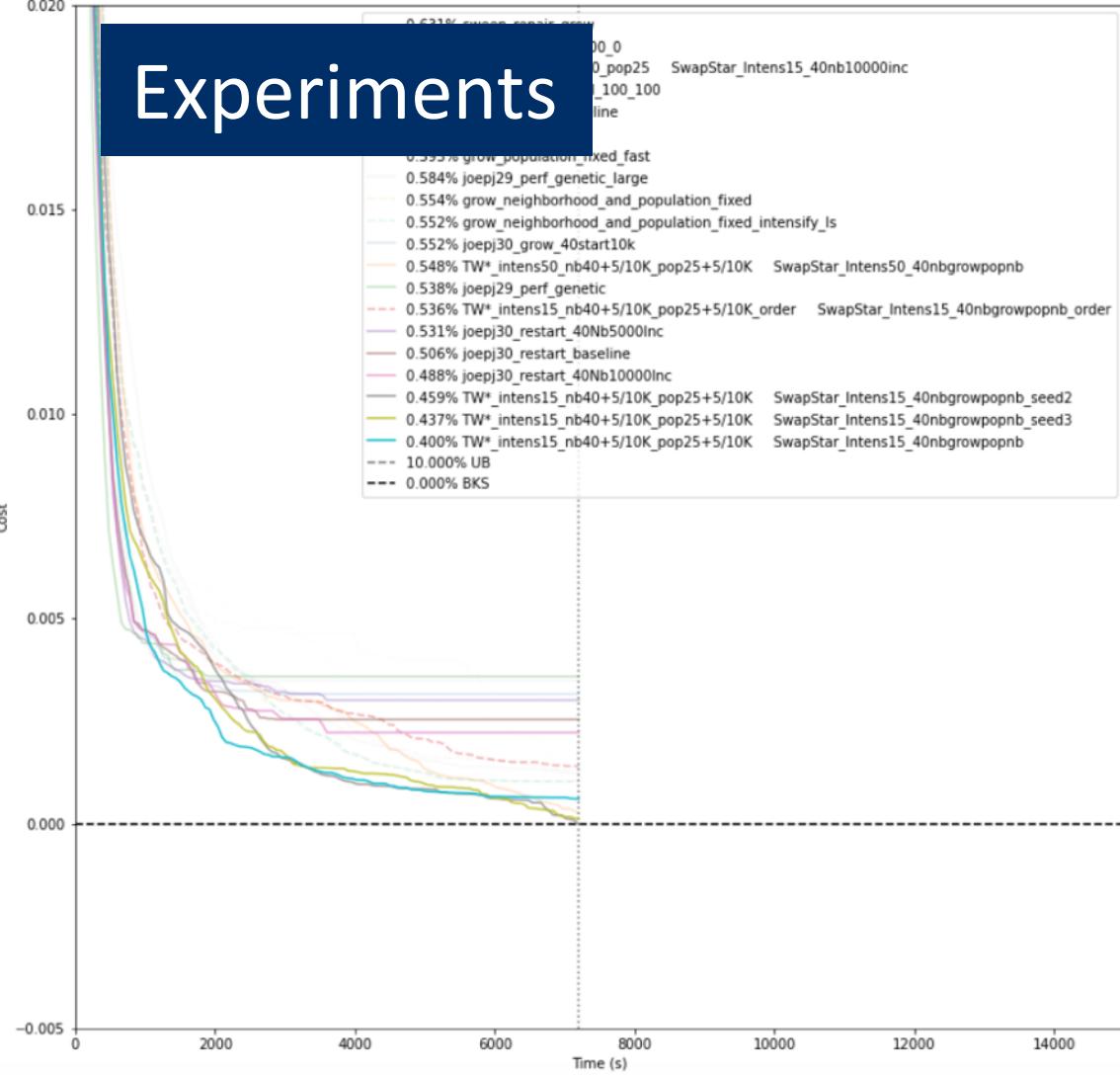


SWAP*

- Cache top 3 insertion positions
- Exact for CVRP
- Approximate for VRPTW

Growing the neighborhood & population

- Every 10K iterations
 - Grow neighborhood by 5
 - Grow population size by 5
- *Slightly different schedule for different instances



Results

Dataset	C1	C2	R1	R2	RC1	RC2	Mean
Solomon	0,000%	0,000%	-0,003%	0,000%	0,000%	0,000%	0,000%
GH200	0,000%	0,004%	0,001%	0,009%	0,016%	0,026%	0,009%
GH400	0,000%	0,000%	-0,019%	-0,028%	0,030%	-0,050%	-0,010%
GH600	-0,014%	0,021%	-0,047%	-0,022%	-0,012%	-0,123%	-0,017%
GH800	0,030%	-0,011%	0,147%	0,090%	0,112%	-0,222%	0,023%
GH1000	0,123%	-0,013%	0,174%	-0,090%	0,094%	-0,158%	0,022%
Mean	0,023%	0,001%	0,060%	0,002%	0,030%	-0,088%	0,004%

(a) Gap to reference solution

