國立中正大學 111 學年度碩士班招生考試

試 題

[第1節]

科目名稱	數學
系所組別	資訊工程學系-甲組、乙組

-作答注意事項-

- ※作答前請先核對「試題」、「試卷」與「准考證」之<u>系所組別、科目名稱</u>是否相符。
- 1. 預備鈴響時即可入場,但至考試開始鈴響前,不得翻閱試題,並不得書寫、 畫記、作答。
- 2. 考試開始鈴響時,即可開始作答;考試結束鈴響畢,應即停止作答。
- 3.入場後於考試開始 40 分鐘內不得離場。
- 4.全部答題均須在試卷(答案卷)作答區內完成。
- 5.試卷作答限用藍色或黑色筆(含鉛筆)書寫。
- 6. 試題須隨試卷繳還。



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科目名稱:數學

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系所組別:資訊工程學系-甲組、乙組

- (10%) Let $\mathbf{u} = (2, 0, 1)$ and $\mathbf{a} = (1, 2, 3)$. Find the vector component of \mathbf{u} along \mathbf{a} and the vector
- (10%) Find a vector that is orthogonal to both $\mathbf{u} = (0, 2, -2)$ and $\mathbf{v} = (1, 3, 0)$. [6] = 67-21-2k => Ans = [(1-2,-2)]
- (10%) Find the coordinate vector of $\mathbf{x} = \{3, 4, 3\}$ relative to the basis $S = \{(3,2,1), (-2,1,0), (5,0,0)\}$. Ah: Shi 20 20n-1-2 Shi 241 241-1 -10 20-16782 8191 8192 8191 8191 0 [(383]]
- (10%) Find A^{13} , where $A^{13} = \begin{bmatrix} -14 & 0 3 & 0 \\ -3 & 0 1 & 1 \\ 7 & 8 & 7 \end{bmatrix} A^{13} = \begin{bmatrix} -14 & 0 3 & 0 \\ -3 & 0 1 & 1 \\ -3 & 0 1 & 1 \\ -3 & 0 1 & 1 \end{bmatrix} A = \begin{bmatrix} 0 & 0 & -2 \\ 1 & 2 & 1 \\ 1 & 0 & 3 \end{bmatrix}$
- (10%) Let the vector space P_2 have the inner product

$$\langle \mathbf{p}, \mathbf{q} \rangle = \int_{-1}^{1} p(x) q(x) dx$$

Apply the Gram-Schmidt process to transform the standard basis $\{1, x, x^2\}$ for P_2 into an orthogonal

- basis $\{\varphi_1(x), \varphi_2(x), \varphi_3(x)\}$.

 (10%) Show that if n is an integer and $n^3 + 5$ is odd, then n is even using
 - a) a proof by contraposition. (5%) (Set | c= event | =) n= event 3 event 3 event 1+5 =) and

b) a proof by contradiction. (5%)

if h is old, h to isold, two, then h=2 lett, h is old =) (2kt $\sqrt{15}$ (10%) Prove whether the given pair of graphs G_1 and G_2 represented by incidence matrices is isomorphic or not.

omorphic or not.
$$G_{1} = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 & 1 \\ 0 & 0 & 0 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}, G_{2} = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 1 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 \end{bmatrix}.$$

(10%) Show that the set of positive rational numbers is countable.

Courtable

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科目名稱:數學

本科目共2頁第2頁

An= (x2h

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- (10%) Consider the recurrence relation $a_n = 2a_{n-1} + 3n$.
 - (a) (2%) Write the associated homogeneous recurrence relation.
 - (b) (2%) Find the general solution to the associated homogeneous recurrence relation.
 - (c) (2%) Find a particular solution to the given recurrence relation. N= Cx2+ 2h
 - (d) (2%) Write the general solution to the given recurrence relation.
 - (d) (2%) Write the general solution to the given recurrence relation when $a_0 = 1$. (e) (2%) Find the particular solution to the given recurrence relation when $a_0 = 1$.

10. (10%)

- a) (5%) Draw all non-isomorphic trees with 5 vertices.
- b) (5%) Draw all non-isomorphic rooted trees with 4 vertices.





