

Appendix

A. Coordinates set-up

1. **(Forward Kinematics)** Consider the robot shown in Fig. 1, where the system has six degrees of freedom as $\mathbf{q} = [q_1 \ q_2 \ q_3 \ q_4 \ q_5 \ q_6]^T$.

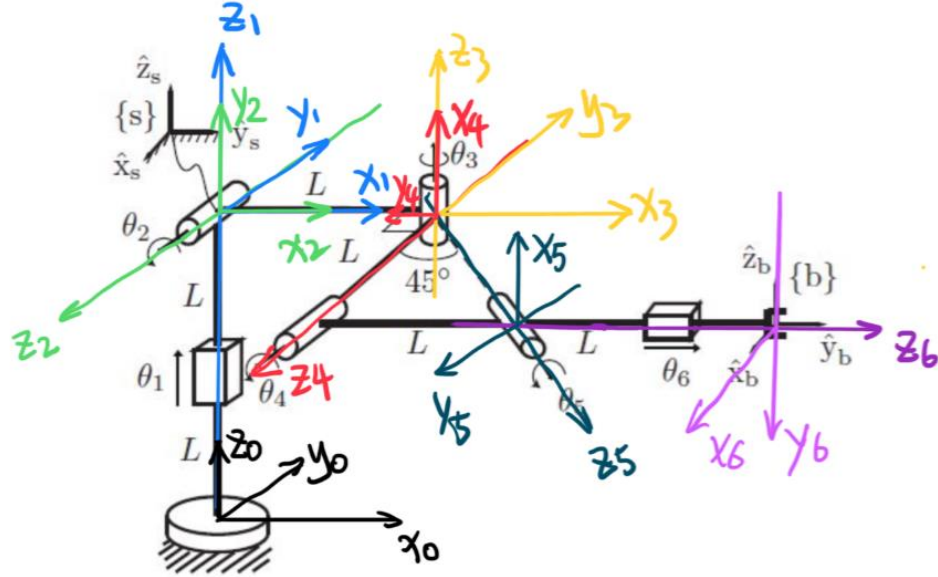


Figure 1: A PRRRRP robot

B. Some corner cases to verify DH table and the implementation of Matlab code/script.

If $\mathbf{q}_c = [0 \ 0 \ 0 \ 0 \ 0 \ 0]$, the manipulator should be the same as the configuration shown in Figure. 1 in the question sheet. The frame of end effector is

$$\begin{bmatrix} -0.0000 & 1.0000 & 0.0000 & 1.5000 \\ -1.0000 & -0.0000 & 0.0000 & -0.5000 \\ 0.0000 & -0.0000 & 1.0000 & 1.0000 \\ 0 & 0 & 0 & 1.0000 \end{bmatrix}$$

, which is right.

If $\mathbf{q}_c = [0 \ 90^\circ \ 0 \ 0 \ 0 \ 0]$, The frame of end effector is

$$\begin{bmatrix} -0.0000 & 0.0000 & -1.0000 & 0.0000 \\ -1.0000 & -0.0000 & 0.0000 & -0.5000 \\ -0.0000 & 1.0000 & 0.0000 & 2.5000 \\ 0 & 0 & 0 & 1.0000 \end{bmatrix}$$

, which is also right.

If $q_c = [0 \ 0 \ 90^\circ \ 0 \ 0 \ 0]$, The frame of end effector is

$$\begin{bmatrix} 1.0000 & 0.0000 & -0.0000 & 1.0000 \\ -0.0000 & 1.0000 & 0.0000 & 1.0000 \\ 0.0000 & -0.0000 & 1.0000 & 1.0000 \\ 0 & 0 & 0 & 1.0000 \end{bmatrix}$$

, which is also right.

If $q_c = [0 \ 0 \ 0 \ 90^\circ \ 0 \ 0]$, The frame of end effector is

$$\begin{bmatrix} -0.0000 & 0.0000 & -1.0000 & 0.5000 \\ -1.0000 & -0.0000 & 0.0000 & -0.5000 \\ -0.0000 & 1.0000 & 0.0000 & 2.0000 \\ 0 & 0 & 0 & 1.0000 \end{bmatrix}$$

, which is also right.

In all, the DH params should be correct.

C. Simulate the forward kinematics for 5 seconds with a 1 Hz sinusoid movement for joint 2 and joint 5 (Amp = 45° , Phase = 0) and a 1 Hz sinusoid movement at joint 1 and joint 6 (Amp = 0.2 meters, Phase = 0). Joint 3 keeps 45° and Joint 4 keeps at 60° . (I just attach the result or figure here and please check the MATLAB code for detail.)

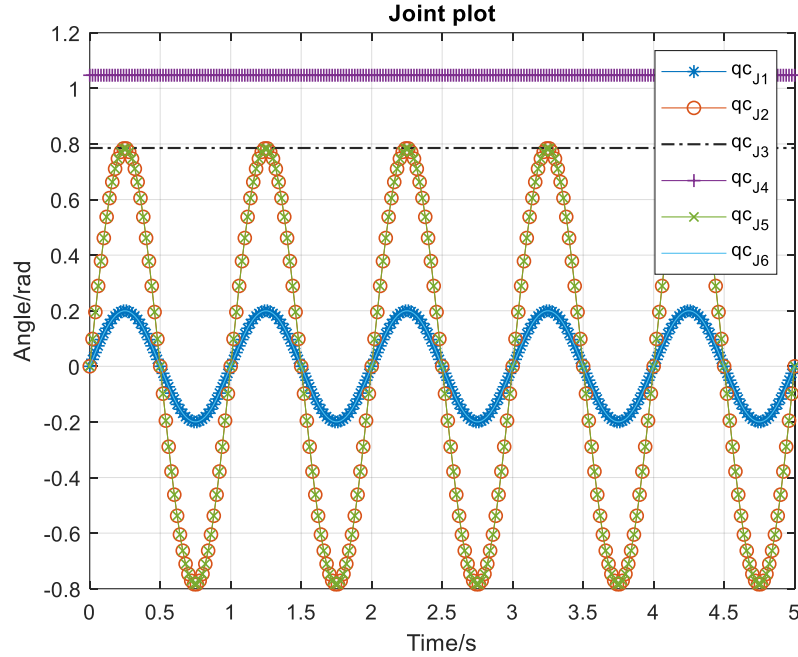


Fig. 1 Joint angles

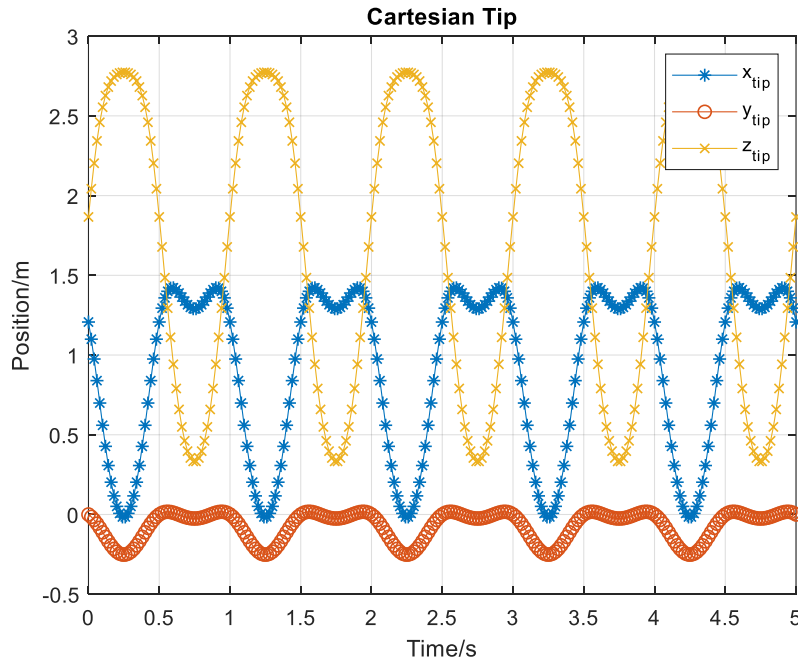


Fig. 2 Cartesian Trajectory

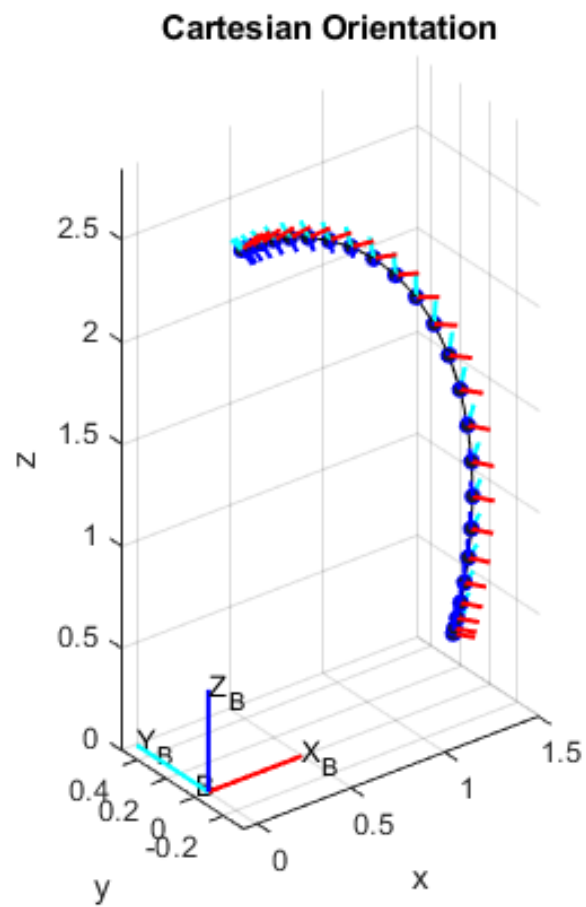


Fig. 3 Cartesian Orientation