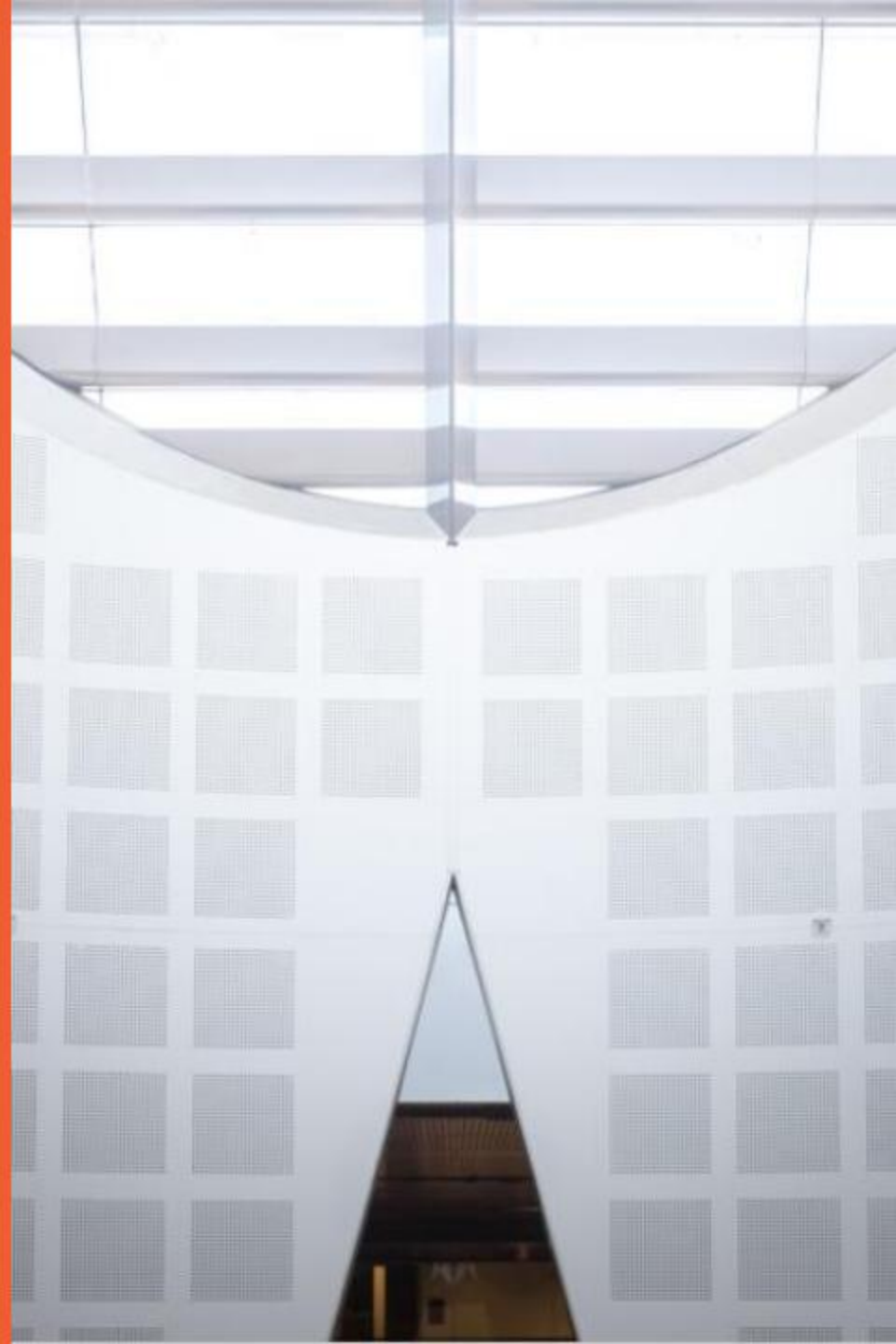


# Biomedical Signal Processing Package Usage

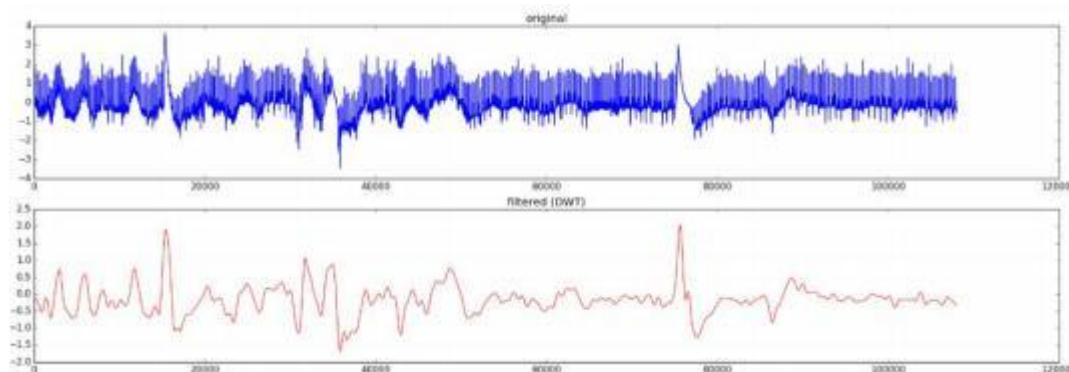
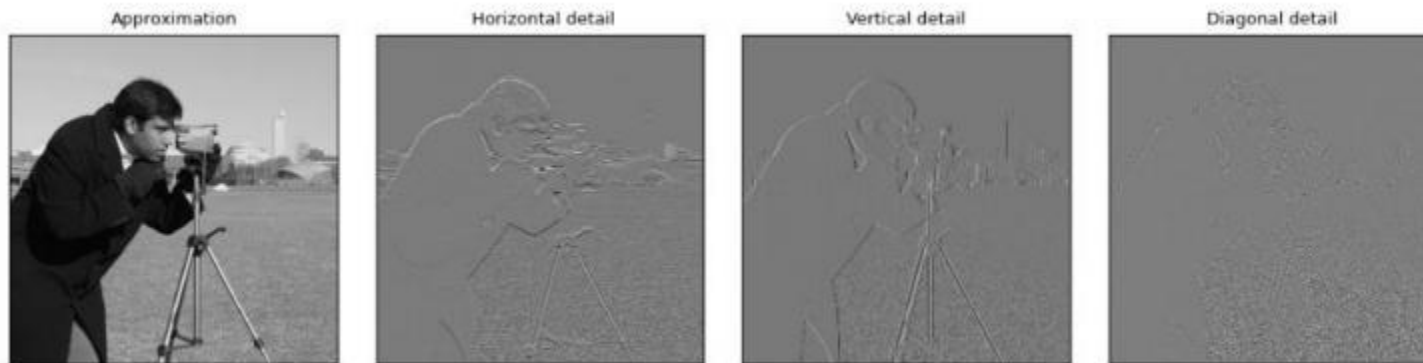
Reference: Healthcare Data Analytics



# Discrete Wavelet Transform (DWT) for Filtering

# Discrete Wavelet Transform for Filtering

- PyWavelets (`pywt`) is a python package for performing Wavelet Transforms
  - The documentations can be found at [PyWavelets - Wavelet Transforms in Python — PyWavelets Documentation](https://pywavelets.com/stable/)
  - With the package, various 1-D, 2-D DWT can be performed



# Discrete Wavelet Transform for Filtering

- PyWavelets (pywt) is a python package for Wavelet Transforms
- The code to import PyWavelets package in python is

```
import pywt
```

- The two key functions in the package are
  - `pywt .wavedec`
    - For performing the 1-D DWT Transform
  - `pywt .waverec`
    - For performing the 1-D I-DWT Transform

# Discrete Wavelet Transform for Filtering

```
pywt.wavedec(data, wavelet, mode='symmetric', level=None, axis=-1)
```

Multilevel 1D Discrete Wavelet Transform of data.

**Parameters:** **data: array\_like**

Input data

**wavelet :** *Wavelet object or name string*

Wavelet to use

**mode :** *str, optional*

Signal extension mode, see [Modes](#).

**level :** *int, optional*

Decomposition level (must be  $\geq 0$ ). If level is None (default) then it will be calculated using the `dwt_max_level` function.

**axis:** *int, optional*

Axis over which to compute the DWT. If not given, the last axis is used.

**Returns:** **[cA\_n, cD\_n, cD\_n-1, ..., cD2, cD1] : list**

Ordered list of coefficients arrays where  $n$  denotes the level of decomposition. The first element (`cA_n`) of the result is approximation coefficients array and the following elements (`cD_n - cD_1`) are details coefficients arrays.

- Numpy array
  - Import numpy as np
  - `Array=np.asarray(python_list)`

# Discrete Wavelet Transform for Filtering

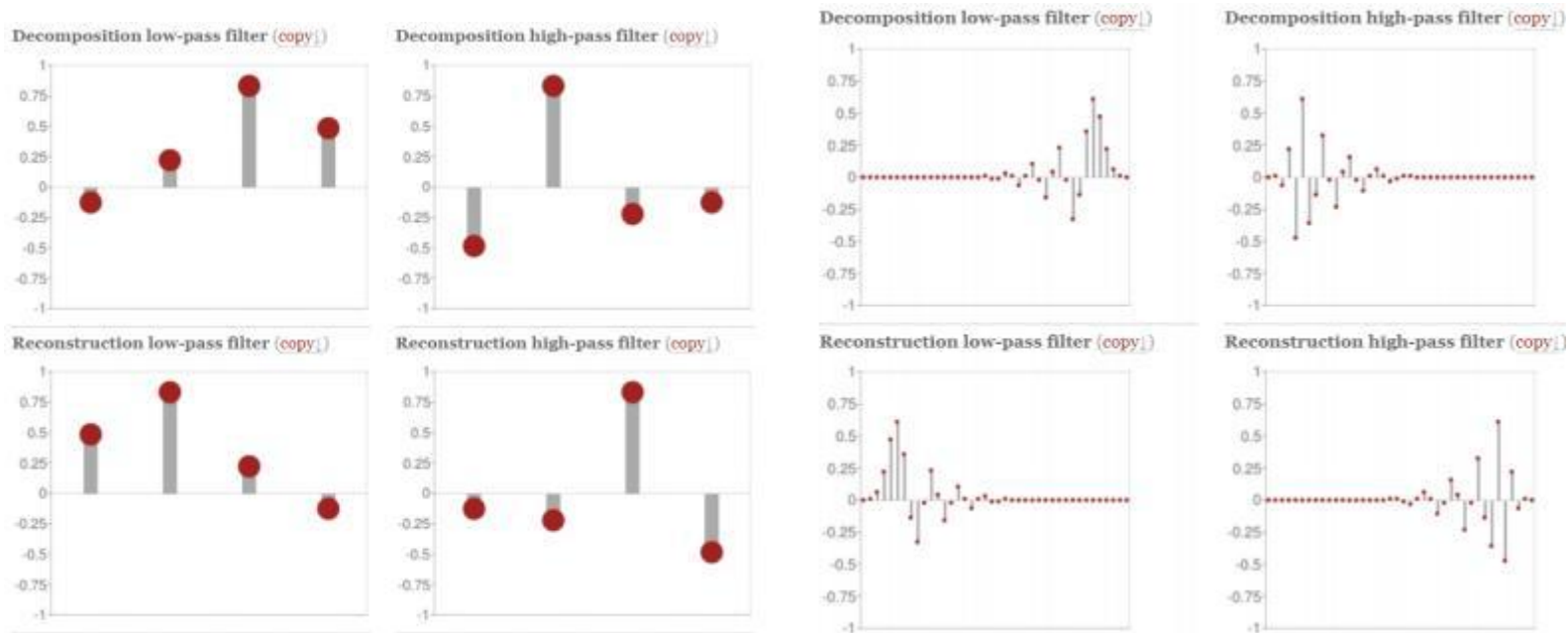
**wavelet** : Wavelet object or name string

Wavelet to use

Wavelet filter type includes: 'db1','db2','db3'... 'db20'

Others can be seen by:

```
print(pywt.wavelist())
```



Daubechies 2  
filter values  
(db2)

Daubechies 20  
filter values  
(db20)

# Discrete Wavelet Transform for Filtering

**mode** : *str, optional*

Signal extension mode, see [Modes](#).

- Padding types for the input data
  - ['zero', 'constant', 'symmetric', 'periodic', 'smooth', 'periodization', 'reflect', 'antisymmetric', 'antireflect']

- **zero - zero-padding** - signal is extended by adding zero samples:

```
... 0 0 | x1 x2 ... xn | 0 0 ...
```

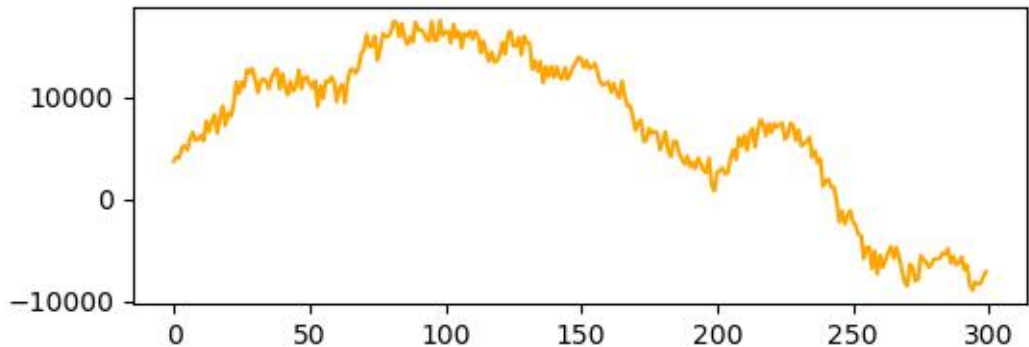
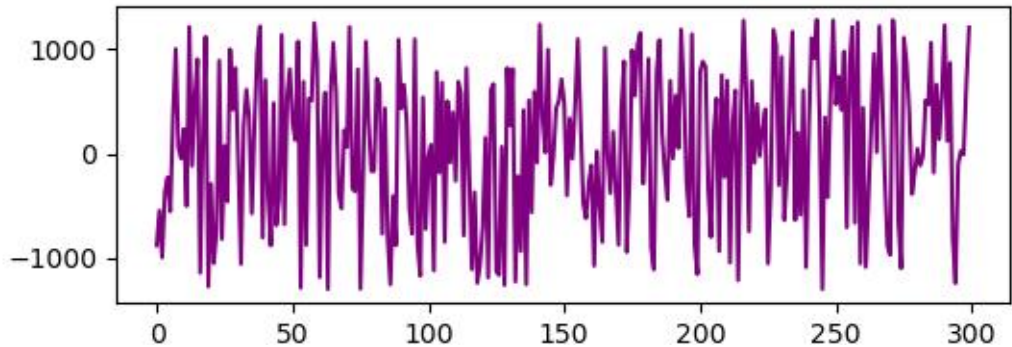
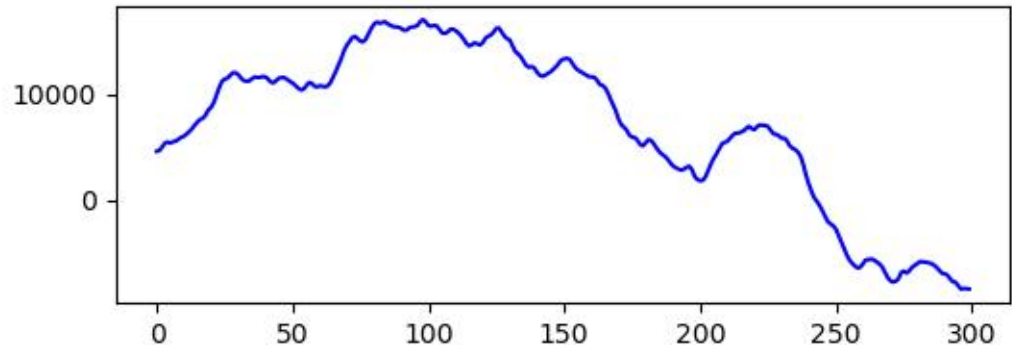
- **constant - constant-padding** - border values are replicated:

```
... x1 x1 | x1 x2 ... xn | xn xn ...
```

- **symmetric - symmetric-padding** - signal is extended by *mirroring* samples. This mode is also known as half-sample symmetric.:

```
... x2 x1 | x1 x2 ... xn | xn xn-1 ...
```

# Discrete Wavelet Transform for Filtering

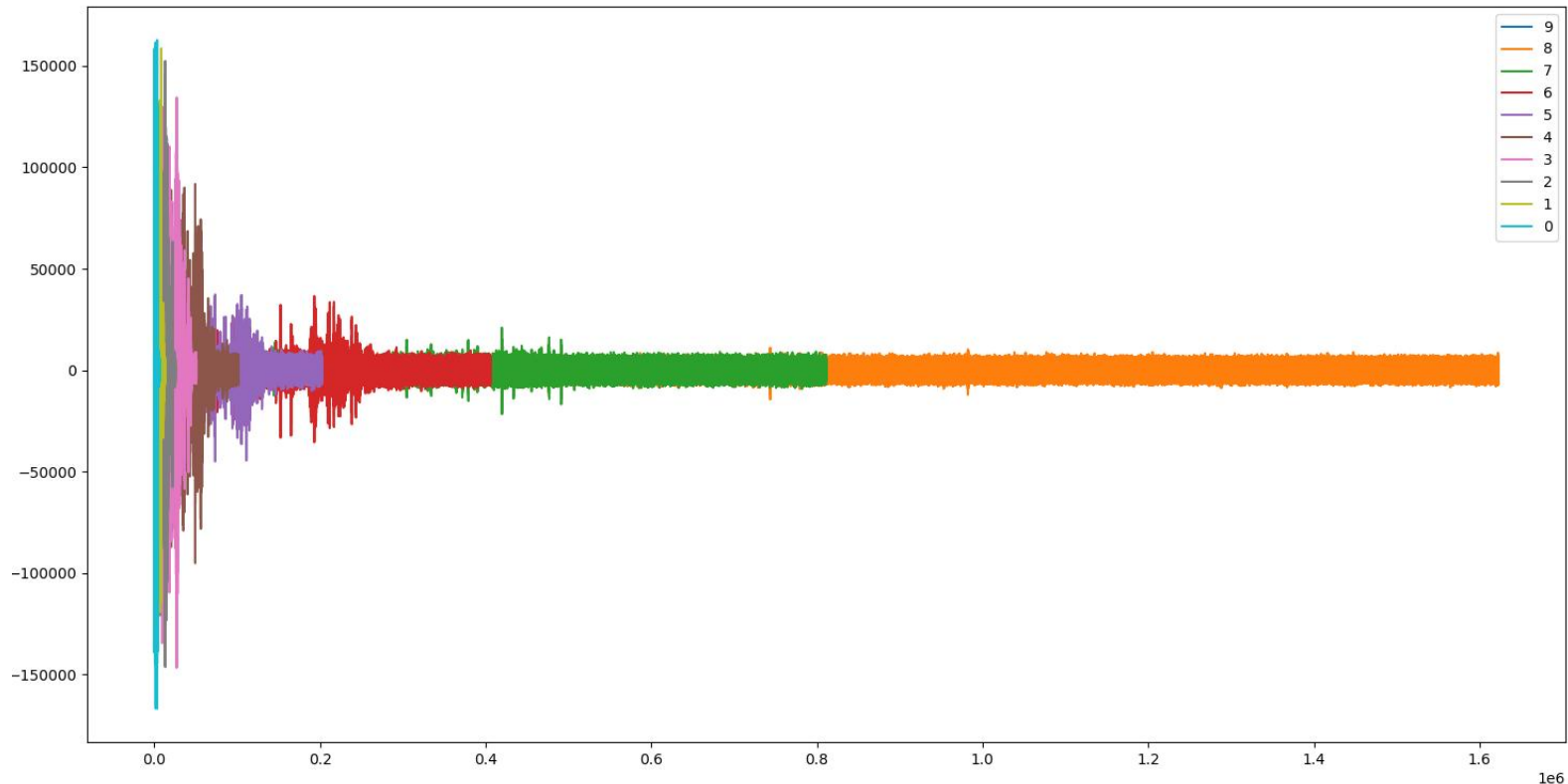




# Discrete Wavelet Transform for Filtering

- By running the following code, DWT is performed

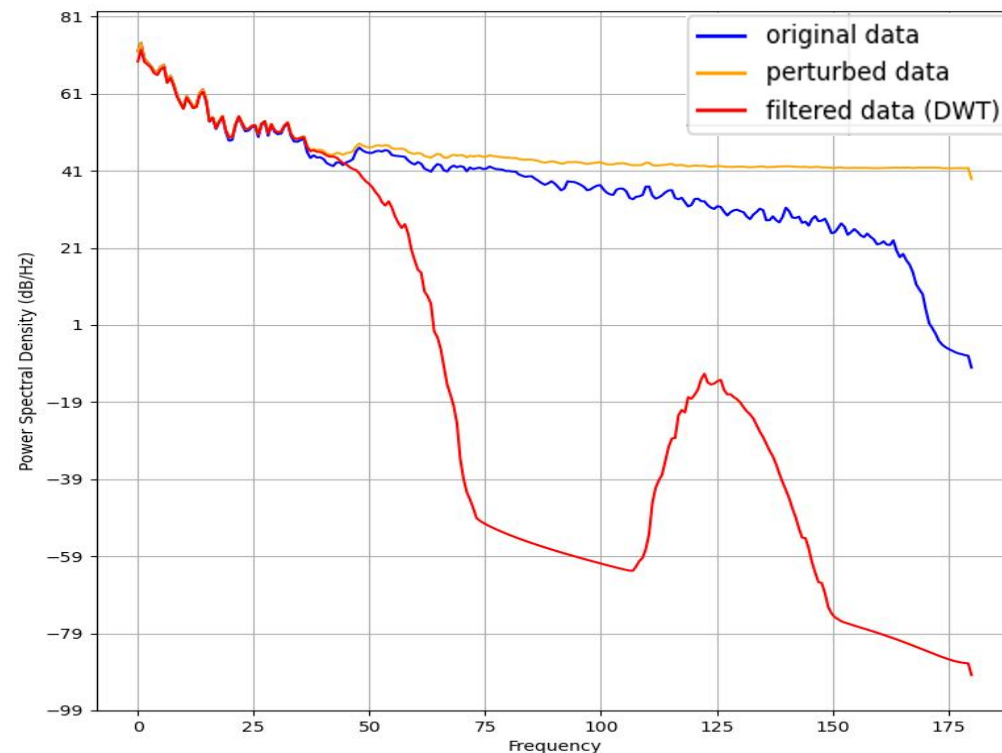
```
DWTcoeffs = pywt .wavedec (data,wavelet_type,mode=mode  
_used, level=9, axis=-1)
```



# Discrete Wavelet Transform for Filtering

- To perform thresholding

```
for i in range(4):  
    DWTcoeffs [-i] = np.zeros_like (DWTcoeffs [-i])
```
- This sets the last 4 coefficient to zero



# Discrete Wavelet Transform for Filtering

```
pywt.waverec(coeffs, wavelet, mode='symmetric', axis=-1)
```

Multilevel 1D Inverse Discrete Wavelet Transform.

**Parameters:** **coeffs** : *array\_like*

Coefficients list [cAn, cDn, cDn-1, ..., cD2, cD1]

**wavelet** : *Wavelet object or name string*

Wavelet to use

**mode** : *str, optional*

Signal extension mode, see [Modes](#).

**axis**: *int, optional*

Axis over which to compute the inverse DWT. If not given, the last axis is used.

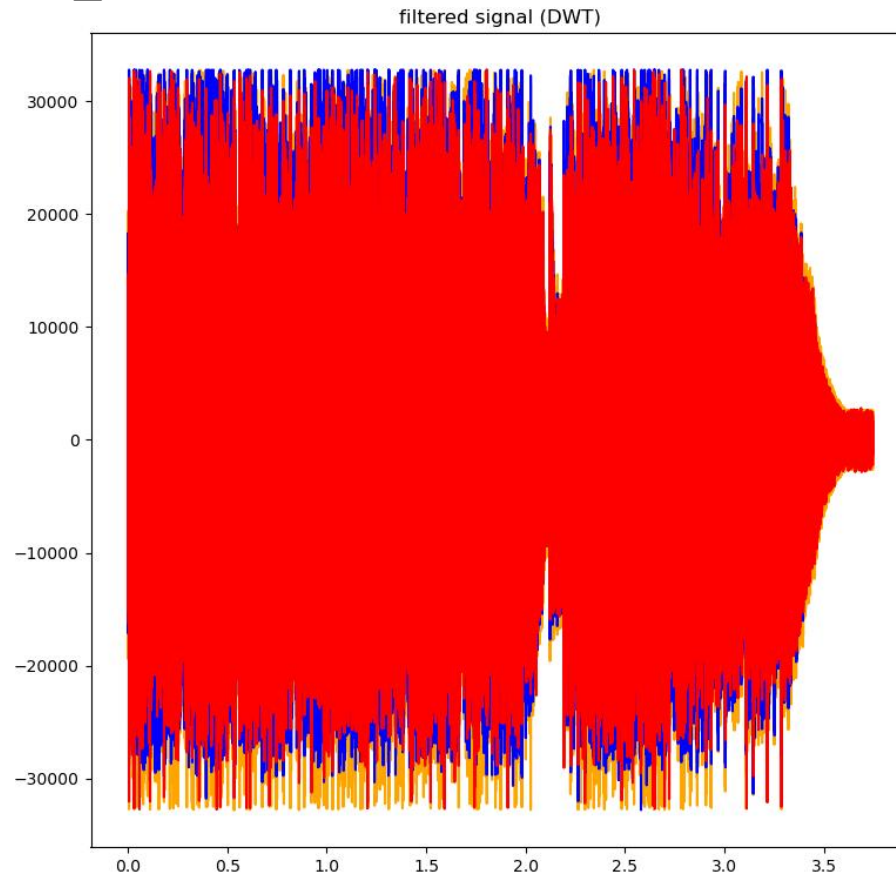
Same as the `pywt.waverec`



# Discrete Wavelet Transform for Filtering

- To perform the I -DWT:

```
filtered_data_dwt=pywt .waverec (DWTcoeffs,wavelet_type,  
mode=mode_used,axis=-1)
```

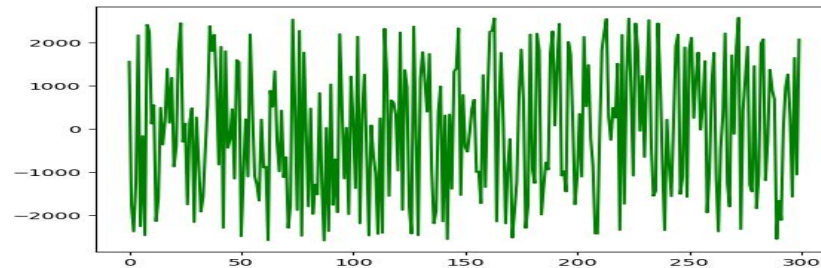


# Discrete Wavelet Transform for Filtering

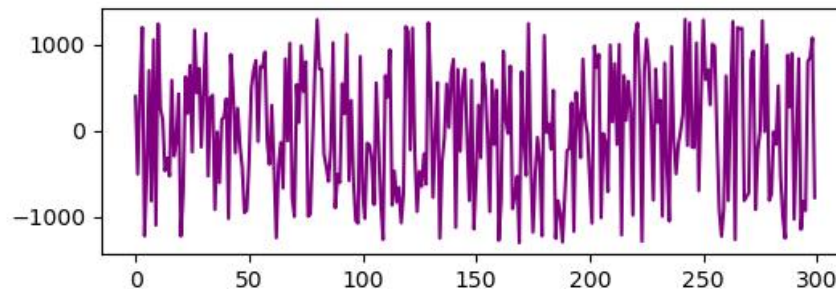
- To calculate the separated noise:

$$\text{separated noise} = \text{data} - \text{filtered\_data\_dwt}$$

Separated noise



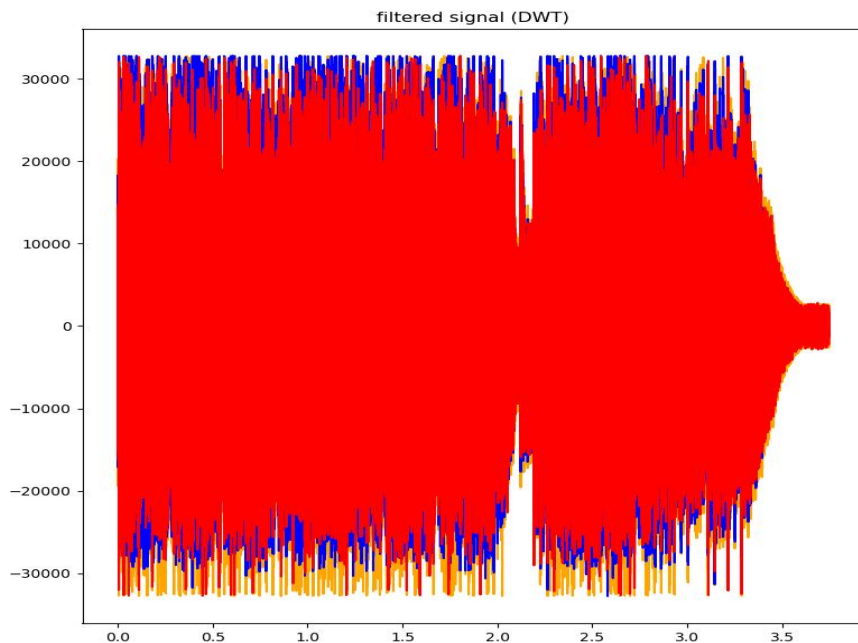
Original noise



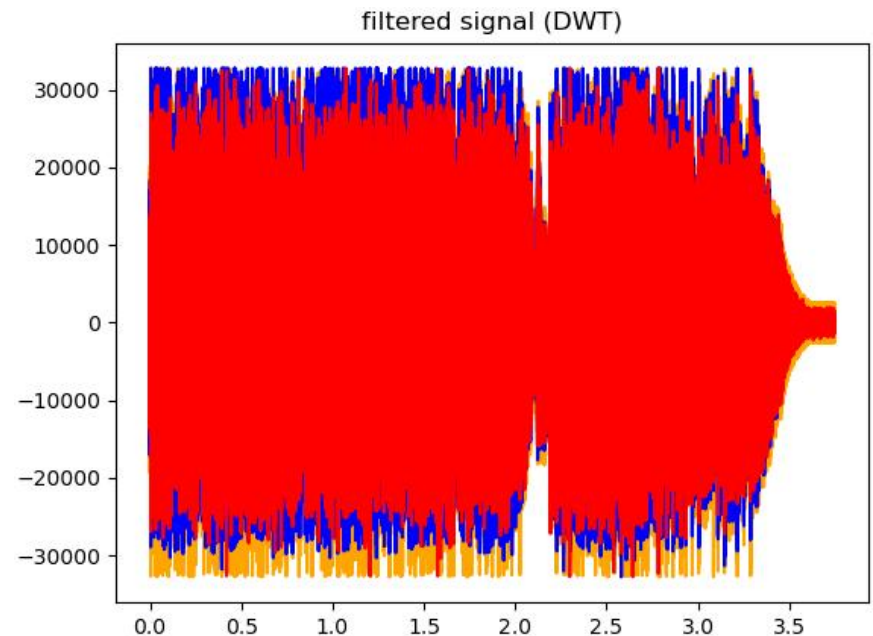
# Discrete Wavelet Transform for Filtering

- Hyperparameters adjustable:
  - (1) wavelet type
  - (2) mode used
  - (3) hard thresholding configuration
  - (4) soft thresholding configuration

Mode='zero'



Mode='symmetric'



# Least Mean Square Adaptive Filter

# Least Mean Square Adaptive Filter

- To perform LMS-filtering:
  - Install the package by “pip install padasip”
  - Before using, make sure to import the package  
`import padasip as pa`
  - The Padasip library is designed to simplify adaptive signal processing tasks within python (filtering, prediction, reconstruction, classification)
  - Documentations available at [Padasip — Padasip 1.2.1 documentation \(matousc89.github.io\)](https://matousc89.github.io/padasip/)

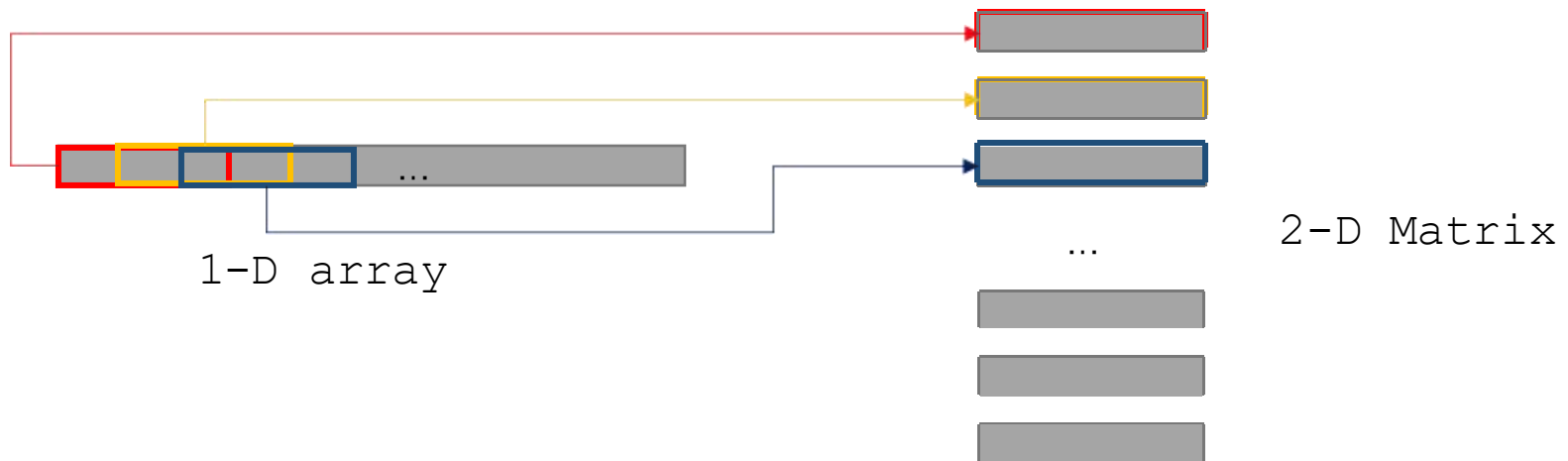


# Least Mean Square Adaptive Filter

- To initialize a LMS-filter:

```
filter = pa.filters .FilterLMS (n=..., mu=... )
```

- n: the size of the filter
- The input data to the LMS -filter need to be adjusted from a 1 - D array into a 2 -D matrix by using a sliding window
- Each row should be of size n.

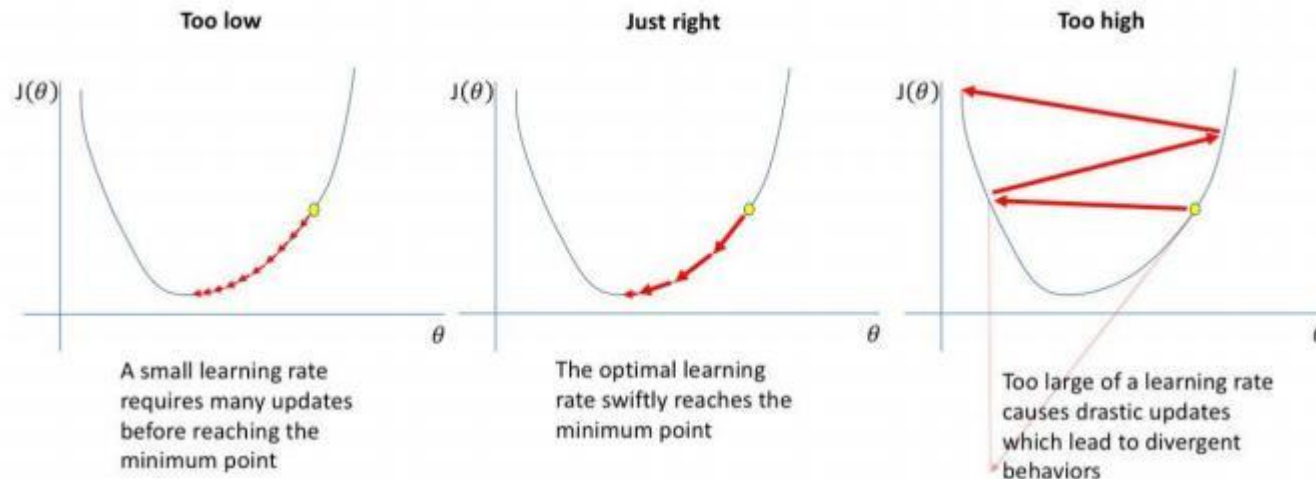


# Least Mean Square Adaptive Filter

- To initialize a LMS-filter:

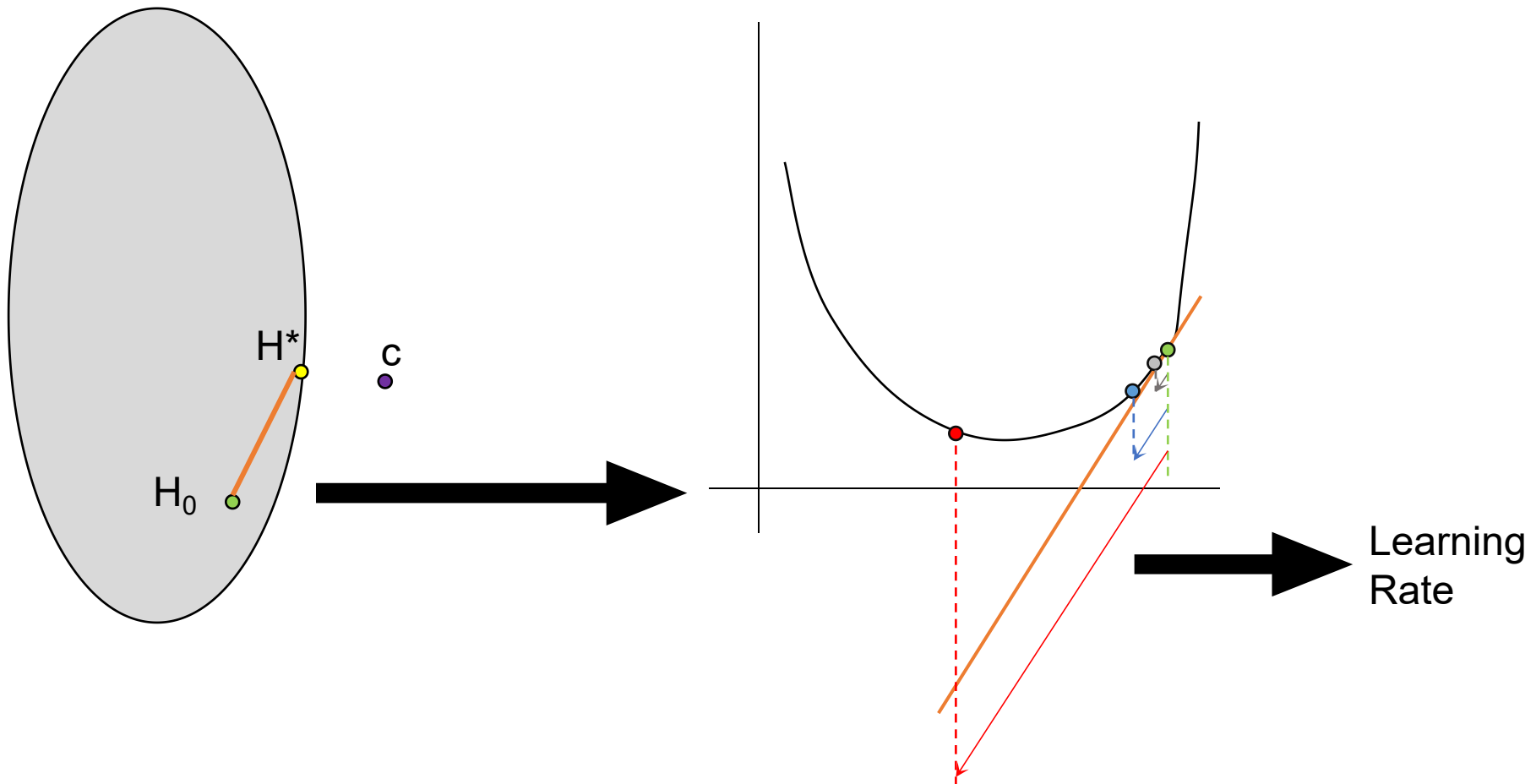
```
filter = pa.filters .FilterLMS (n=..., mu=... )
```

- Mu: The learning rate of the Least Mean Square algorithm
- Mu being too large will cause the filter not to train properly
- Mu being too small will cause training to be slow and not reaching the best value after training



# Least Mean Square Adaptive Filter

- Learning rate and optimization



# Least Mean Square Adaptive Filter

- To initialize a LMS-filter:

```
filter = pa.filters.FilterLMS (n=..., mu=...)
```

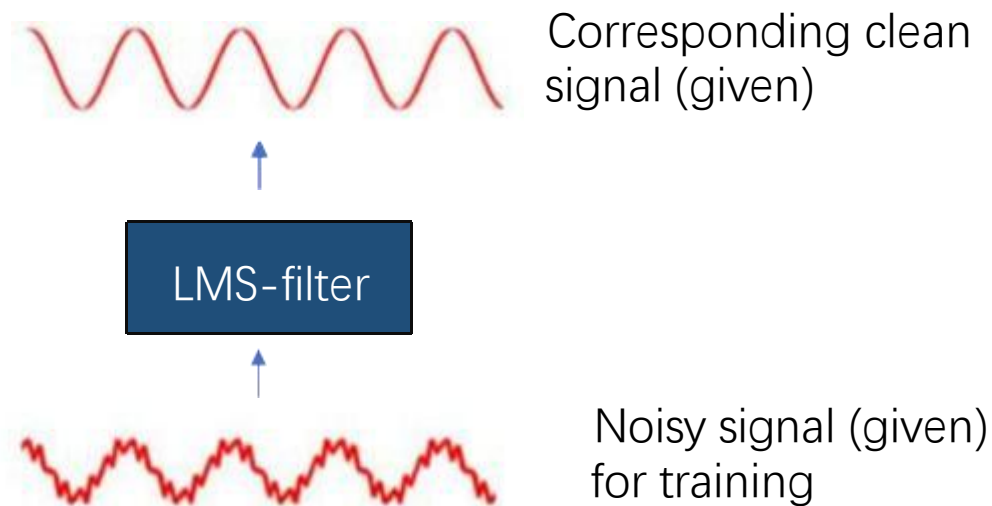
- The output of the above line is an object for the filter
- With this filter object, training and predictions can be performed.

# Least Mean Square Adaptive Filter

- To train the filter object:

```
y, e, w = filter .run (Target_signal, Corresponding_noisy_signal)
```

- With the above line, the filter value is automatically adjusted based on the Noisy\_signal and Corresponding\_clean\_signal.



# Least Mean Square Adaptive Filter

- To train the filter object:

```
y, e, w = filter .run (Target_signal, Corresponding_noisy_signal)
```

- Target\_signal: 1 -D signal
- Corresponding\_noisy\_signal: 2 -D matrix
- y: filtered signal with the trained filter (1 -D signal)

# Least Mean Square Adaptive Filter

- To make a new prediction with the filter object based on new inputs:

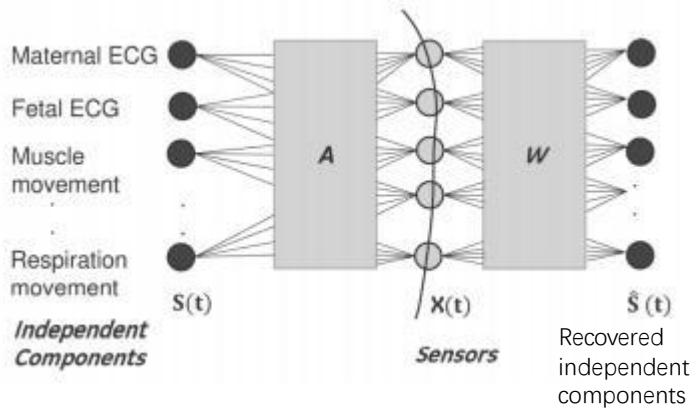
```
y1=[]  
for i in range(len(x)):  
    temp = filter.predict(x[i])  
    y1.append(temp)
```

- The new input needs to be converted into a 2 -D matrix using the sliding window (stride = 1)
- Values in each sliding window need to be fed into “filter.predict()” to gain “temp”, which is a single value.
- The hyperparameters adjustable are:
  - (1) filter size (n)
  - (2) learning rate (mu)

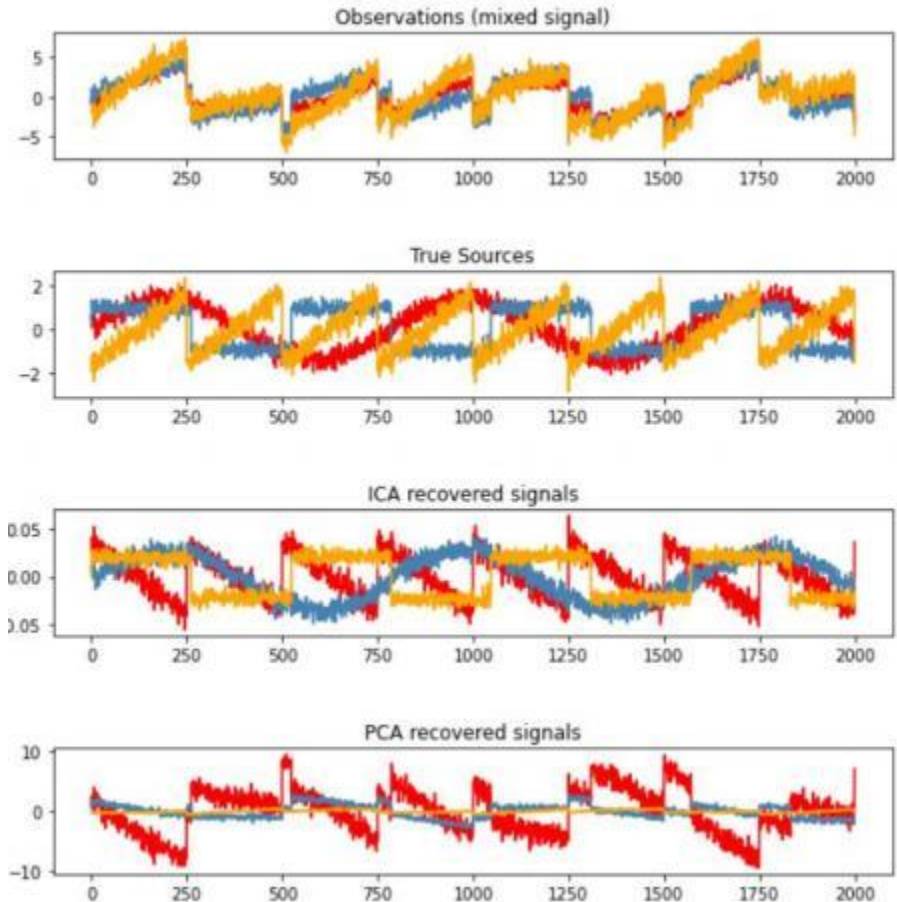
# Independent Component Analysis (ICA)



# Independent Component Analysis (ICA)



ICA can better  
disentangle signal  
than PCA



# Independent Component Analysis (ICA)

- Before using ICA, it need to be imported from sklearn
  - `from sklearn.decomposition import FastICA`
  - Documentations given at [sklearn.decomposition.FastICA — scikit - learn 1.1.1 documentation](#)
- Build a toy dataset:
  - We start with 3 independent signals ( $s_1$ ,  $s_2$ ,  $s_3$ ) and a mixing matrix  $A$
  - We then mix the three signals using the mixing matrix  $A$

# Independent Component Analysis (ICA)

- Steps to perform the mixing (for the toy example):

```
s1 = np.sin(2 * time)    # Signal 1 : sinusoidal signal
s2 = np.sign(np.sin(3 * time)) # Signal 2 : square signal
s3 = signal.sawtooth(2 * np.pi * time) # Signal 3: saw tooth signal

S = np.c_[s1, s2, s3]
S += 0.2 * np.random.normal(size=S.shape) # Add noise

S /= S.std(axis=0) # Standardize data
# Mix data
A = np.array([[1, 1, 1], [0.5, 2, 1.0], [1.5, 1.0, 2.0]]) # Mixing matrix
X = np.dot(S, A.T) # Generate observations
```

# Independent Component Analysis (ICA)

- To perform the disentangling with ICA:

```
ica = FastICA(n_components=3)
```

```
S_ = ica.fit_transform(X)
```

- Parameter:

n\_component: it indicates the amount of signal that we aim to disentangle

- X: the mixed input in the form of a matrix

- Method:

fit\_transform(X): calculate the disentangled result

# Independent Component Analysis (ICA)

