Real-time Forecast Combinations for the Oil Price*

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Summary: Baumeister and Kilian (2015) combine forecasts from six empirical models to predict real oil prices. In this paper, we broadly reproduce their main economic findings, employing their preferred measures of the real oil price and other real-time variables. Mindful of the importance of Brent crude oil as a global price benchmark, we extend consideration to the North Sea based measure and update the evaluation sample to 2017:12. We model the oil price futures curve using a factor-based Nelson-Siegel specification estimated in real time to fill in missing values for oil price futures in the raw data. We find that the combined forecasts for Brent are as effective as for other oil price measures. The extended sample using the oil price measures adopted by Baumeister and Kilian (2015) yields similar results to those reported in their paper. And the futures-based model improves forecast accuracy at longer horizons. The real-time data set is available for download from https://www.niesr.ac.uk/real-time-forecast-combinations-oil-price.

Keywords: Real oil price forecasting, Brent crude oil, Forecast combination

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Appendix to Garratt, Vahey and Zhang (2018)

(I) Shorter evaluation sample, 1992:01–2012:09

Our results from the narrow replication, using the evaluation sample examined by Baumeister and Kilian (2015) are shown in Tables A-1a and A-1b. These results use the same WTI and RAC measures considered by those authors. The results confirm the main findings of their paper. Equal weight point combinations have lower MSPE ratios and higher success ratios than inverse MSPE weights for most horizons. The corresponding recursive MSPE and success ratios for the Brent measure, with the same 1992:01 to 2012:09 evaluation sample are displayed in Table A-1c.

Table A-1a. Forecast Accuracy for RAC, Evaluation 1992:01-2012:09

<u> </u>		Real U.S. re	efiners' acquisition cost	for oil imports	
			Rolling	weights based on winde	ows of length
МН	Equal weight	Recursive weights	36	24	12
		Reci	ırsive MSPE ratios		
1	0.928 ** (0.028)	0.933 **(0.039)	0.935 **(0.045)	0.928 **(0.033)	0.925 **(0.030)
3	0.922 **(0.008)	0.925 **(0.009)	0.925 **(0.009)	0.920 **(0.005)	0.925 **(0.005)
6	0.985 (0.172)	0.989 (0.241)	0.990 (0.254)	0.991(0.282)	0.990 (0.251)
9	0.980 (0.111)	0.985 (0.182)	0.983 (0.156)	0.986 (0.212)	0.988 (0.257)
12	0.941 **(0.001)	0.946 **(0.003)	0.949 **(0.006)	0.947 **(0.004)	0.942 **(0.002)
15	0.932 **(0.000)	0.942 **(0.002)	0.955 **(0.022)	0.954 **(0.018)	0.970 *(0.095)
18	0.974 *(0.073)	0.994 (0.380)	1.023(0.854)	1.030(0.908)	1.055(0.983)
21	1.006(0.636)	1.028(0.947)	1.054(0.995)	1.062(0.996)	1.099(1.000)
24	0.987 (0.224)	0.997 (0.427)	1.000(0.499)	1.005(0.592)	1.046(0.962)
			Success ratios		
1	0.562 **(0.050)	0.546 (0.119)	0.546 (0.119)	0.542 (0.153)	0.546 (0.129)
3	$0.575^{**}(0.034)$	0.583 **(0.017)	$0.579^{**}(0.026)$	0.591 **(0.010)	0.579 **(0.026)
6	0.545 (0.201)	0.520 (0.487)	0.520 (0.487)	0.516 (0.531)	0.512 (0.558)
9	0.539 (0.171)	0.548 * (0.085)	$0.560^*(0.051)$	0.539 (0.146)	0.544 (0.113)
12	0.639 **(0.000)	0.634 **(0.000)	0.643 **(0.000)	0.630 **(0.000)	0.664 **(0.000)
15	0.617 ** (0.000)	0.574 **(0.007)	0.557 **(0.038)	0.553 **(0.047)	0.562 **(0.048)
18	0.573 **(0.001)	0.543 **(0.010)	0.522 (0.100)	0.491(0.363)	0.500(0.290)
21	0.563 ** (0.006)	$0.515^*(0.052)$	$0.546^{**}(0.027)$	0.533 (0.116)	0.498(0.502)
24	0.553 ** (0.048)	0.518 (0.105)	0.549 *(0.079)	0.544 (0.156)	0.531 (0.264)

NOTES: MH represents monthly forecast horizons. Boldface indicates improvements relative to the no-change forecast. As a rough guide, p-values of a Harvey, Leybourne, and Newbold (1997) small-sample adjustment of the Diebold and Mariano (1995) test are reported in brackets after recursive MSPE ratios. We also report p-values for the Pesaran and Timmermann (2009) test for the null hypothesis of no directional accuracy in brackets after success ratios. * denotes significance at the 10% level and ** at the 5% level.

Table A-1b. Forecast Accuracy for WTI, Evaluation 1992:01-2012:09

			Real WTI price		
			Rolling	weights based on winde	ows of length
МН	Equal weight	Recursive weights	36	24	12
		Recu	ursive MSPE ratios		
1	0.904 **(0.007)	0.908 **(0.008)	0.909 **(0.009)	0.909 **(0.011)	0.906 **(0.011)
3	0.923 **(0.010)	0.926 **(0.010)	0.927 **(0.012)	0.927 **(0.010)	0.931 **(0.011)
6	0.988(0.242)	0.992 (0.314)	0.993 (0.323)	0.994(0.363)	0.998(0.442)
9	0.982 (0.146)	0.988(0.236)	0.983 (0.170)	0.987 (0.228)	0.990(0.296)
12	0.948**(0.004)	0.955 **(0.011)	0.954 **(0.013)	0.950 **(0.007)	0.943**(0.003)
15	0.942 **(0.002)	0.956 **(0.015)	0.966 *(0.070)	0.966*(0.064)	0.945**(0.009)
18	0.973 *(0.070)	0.998(0.465)	1.026(0.883)	1.043(0.963)	1.069(0.989)
21	1.004(0.599)	1.033(0.966)	1.056(0.993)	1.067(0.995)	1.082(0.998)
24	0.979 (0.146)	1.000(0.505)	1.001(0.526)	1.009(0.648)	1.054(0.969)
			Success ratios		
1	0.542 (0.201)	0.546 (0.187)	0.538 (0.267)	0.550 (0.165)	0.554 (0.131)
3	0.551 (0.158)	0.543 (0.220)	0.543 (0.220)	0.547 (0.198)	0.530 (0.407)
6	0.525 (0.425)	0.516 (0.549)	0.512 (0.593)	0.500(0.699)	0.488(0.827)
9	$0.552^*(0.082)$	$0.552^*(0.075)$	0.564 **(0.039)	$0.560^*(0.054)$	0.535 (0.169)
12	0.584 ** (0.005)	0.563 **(0.034)	0.580 **(0.012)	$0.592^{**}(0.004)$	0.592 **(0.003)
15	0.587**(0.004)	0.570 **(0.016)	0.557 **(0.049)	0.566 **(0.035)	0.566 **(0.016)
18	0.582 **(0.001)	0.556 **(0.004)	0.530 *(0.073)	0.522 (0.133)	0.522 (0.133)
21	0.581 **(0.003)	0.511 *(0.062)	0.533 *(0.051)	0.528 (0.177)	0.511 (0.324)
24	0.540 (0.108)	0.482(0.433)	0.531 (0.185)	0.518 (0.430)	0.527 (0.301)

NOTES: MH represents monthly forecast horizons. Boldface indicates improvements relative to the no-change forecast. As a rough guide, p-values of a Harvey et al. (1997) small-sample adjustment of the Diebold and Mariano (1995) test are reported in brackets after recursive MSPE ratios. We also report p-values for the Pesaran and Timmermann (2009) test for the null hypothesis of no directional accuracy in brackets after success ratios. * denotes significance at the 10% level and ** at the 5% level.

Table A-1c. Forecast Accuracy for Brent, Evaluation 1992:01-2012:09

			Real Brent price		
			Rolling	weights based on windo	ows of length
МН	Equal weight	Recursive weights	36	24	12
		Reci	ursive MSPE ratios		
1	0.956 (0.110)	0.935 **(0.019)	0.933 **(0.019)	0.936 **(0.024)	0.948 *(0.086)
3	0.941 **(0.024)	0.940 **(0.017)	0.938 **(0.014)	0.943 **(0.021)	0.945 ** (0.022)
6	0.995 (0.394)	1.001(0.517)	1.005(0.632)	1.005(0.620)	1.008(0.689)
9	0.983 (0.176)	0.990 (0.278)	0.990 (0.280)	0.996 (0.395)	0.996 (0.410)
12	0.952 **(0.003)	0.961 **(0.015)	0.965 **(0.022)	0.966 **(0.022)	0.956 **(0.010)
15	0.947 **(0.001)	0.961 **(0.013)	0.972 *(0.066)	0.979 (0.112)	0.980 (0.117)
18	0.986 (0.203)	1.011(0.737)	1.032(0.963)	1.045(0.995)	1.077(1.000)
21	1.018(0.898)	1.044(0.998)	1.062(1.000)	1.068(1.000)	1.096(1.000)
24	1.014(0.799)	1.030(0.962)	1.039(0.985)	1.046(0.996)	1.101(1.000)
			Success ratios		
1	0.514 (0.199)	0.530 (0.110)	0.530 (0.120)	$0.534^*(0.099)$	0.550 **(0.029)
3	0.538 (0.134)	0.522 (0.263)	0.543 (0.104)	0.538 (0.125)	0.543 (0.104)
6	0.496(0.552)	0.480(0.727)	0.480(0.743)	0.471(0.764)	0.488(0.615)
9	0.506 (0.315)	0.510 (0.261)	0.506 (0.315)	0.490(0.498)	0.498(0.352)
12	$0.567^{**}(0.005)$	0.571 **(0.005)	0.576 **(0.003)	0.563 **(0.006)	0.584 **(0.001)
15	0.583 ** (0.001)	0.596 **(0.000)	0.604 **(0.000)	0.587 **(0.000)	0.609 **(0.000)
18	0.543 ** (0.002)	0.543 **(0.000)	0.500*(0.052)	0.483(0.221)	0.466(0.389)
21	0.528 ** (0.003)	0.502 **(0.006)	$0.507^{**}(0.021)$	0.463(0.427)	0.445(0.621)
24	0.491(0.253)	0.456(0.461)	0.500(0.120)	0.442(0.870)	0.451(0.819)

NOTES: MH represents monthly forecast horizons. Boldface indicates improvements relative to the no-change forecast. As a rough guide, p-values of a Harvey et al. (1997) small-sample adjustment of the Diebold and Mariano (1995) test are reported in brackets after recursive MSPE ratios. We also report p-values for the Pesaran and Timmermann (2009) test for the null hypothesis of no directional accuracy in brackets after success ratios. * denotes significance at the 10% level and ** at the 5% level.

(II) Longer evaluation sample, 1992:01-2017:12, for RAC and WTI measures

We also present the forecast accuracy of RAC and WTI for the extended 1992:01 to 2017:12 evaluation sample in Tables A-2a and A-2b, respectively.

Table A-2a. Forecast Accuracy for RAC, Evaluation 1992:01 to 2017:12

		Real U.S. re	efiners' acquisition cost	for oil imports	
	-		Rolling	weights based on windo	ows of length
МН	Equal weight	Recursive weights	36	24	12
		Reco	ursive MSPE ratios		
1	0.931 **(0.015)	0.935 **(0.022)	0.939 **(0.029)	0.932 **(0.020)	0.928 **(0.016)
3	0.923 **(0.002)	0.925 **(0.002)	0.930**(0.004)	0.922 **(0.001)	0.921 **(0.001)
6	0.977 ** (0.048)	0.983 *(0.099)	0.984(0.100)	0.979 *(0.058)	0.971 **(0.025)
9	0.971 **(0.015)	0.978 *(0.058)	0.974 **(0.030)	0.972 **(0.029)	0.969**(0.026)
12	0.936 **(0.000)	0.945 **(0.000)	0.941**(0.000)	0.930 **(0.000)	0.921 **(0.000)
15	0.932 **(0.000)	0.944 **(0.000)	0.944 **(0.001)	0.935 **(0.000)	0.927 **(0.000)
18	0.944**(0.000)	0.963 **(0.009)	0.974 *(0.078)	0.972 *(0.079)	0.951 **(0.042)
21	0.972 **(0.022)	0.998 (0.429)	0.998(0.456)	1.001(0.528)	0.994 (0.419)
24	0.970 **(0.024)	1.012(0.798)	0.989 (0.248)	0.991 (0.293)	1.006(0.586)
			Success ratios		
1	0.558 ** (0.042)	$0.545^*(0.095)$	0.564 **(0.024)	$0.554^*(0.053)$	0.561 **(0.033)
3	0.597 **(0.002)	0.594 **(0.002)	0.600 **(0.001)	0.606 **(0.000)	0.606 **(0.000)
6	0.573 **(0.021)	0.547 (0.150)	0.550 (0.111)	0.554 *(0.081)	0.554 *(0.077)
9	0.549 *(0.068)	0.556 **(0.038)	0.582 **(0.003)	0.569 **(0.012)	0.569 **(0.011)
12	0.645 ** (0.000)	0.631 **(0.000)	0.654 **(0.000)	0.645 **(0.000)	0.681 **(0.000)
15	0.614 **(0.000)	0.581 **(0.004)	0.570 **(0.012)	0.584 **(0.003)	0.581 **(0.004)
18	0.586 **(0.001)	0.556 **(0.016)	0.536 *(0.092)	0.508 (0.348)	0.515 (0.258)
21	0.565 **(0.012)	0.517 (0.217)	0.545 *(0.064)	0.551 **(0.039)	0.507 (0.429)
24	0.561 **(0.026)	0.505 (0.432)	0.547 *(0.081)	0.547 *(0.084)	0.529 (0.181)

NOTES: MH represents monthly forecast horizons. Boldface indicates improvements relative to the no-change forecast. As a rough guide, p-values of a Harvey et al. (1997) small-sample adjustment of the Diebold and Mariano (1995) test are reported in brackets after recursive MSPE ratios. We also report p-values for the Pesaran and Timmermann (2009) test for the null hypothesis of no directional accuracy in brackets after success ratios. * denotes significance at the 10% level and ** at the 5% level.

Table A-2b. Forecast Accuracy for WTI, Evaluation 1992:01 to 2017:12

			Real WTI price		
			Rolling	weights based on windo	ows of length
МН	Equal weight	Recursive weights	36	24	12
		Reci	ursive MSPE ratios		
1	0.907 **(0.002)	0.910 **(0.002)	0.912 **(0.003)	0.912 **(0.004)	0.909 **(0.004)
3	0.923 **(0.002)	0.925 **(0.002)	0.929**(0.004)	0.927 **(0.003)	0.927 **(0.002)
6	0.979 *(0.079)	0.984 (0.138)	0.984 (0.131)	0.984 (0.119)	0.988 (0.208)
9	0.973 **(0.027)	0.980 *(0.082)	0.974 **(0.039)	0.974 **(0.043)	0.979 *(0.092)
12	0.942 **(0.000)	0.950 **(0.001)	0.942 **(0.000)	0.931 **(0.000)	0.935 **(0.000)
15	0.937 **(0.000)	0.949 **(0.001)	0.944**(0.001)	0.934 **(0.000)	0.917**(0.000)
18	0.944 **(0.000)	0.963 **(0.011)	$0.970^*(0.056)$	$0.972^*(0.092)$	0.982 (0.248)
21	0.970 **(0.023)	0.994 (0.340)	0.991 (0.313)	0.991 (0.340)	0.987 (0.309)
24	0.956 **(0.005)	0.995 (0.361)	0.967 **(0.035)	0.964 **(0.034)	0.990 (0.377)
			Success ratios		
1	$0.558^*(0.059)$	$0.561^*(0.052)$	0.545 (0.155)	0.551 (0.109)	0.574 **(0.019)
3	$0.577^{**}(0.012)$	$0.565^{**}(0.037)$	$0.571^{**}(0.021)$	$0.571^{**}(0.022)$	0.565 **(0.044)
6	0.544 (0.169)	0.541 (0.213)	0.541 (0.205)	0.534 (0.235)	0.521 (0.436)
9	$0.572^{**}(0.011)$	$0.572^{**}(0.011)$	$0.582^{**}(0.005)$	$0.572^{**}(0.013)$	0.559 **(0.030)
12	0.618 ** (0.000)	0.601 **(0.000)	0.608 **(0.000)	0.621 **(0.000)	0.598 ** (0.001)
15	0.614 ** (0.000)	0.594 **(0.001)	0.594 **(0.001)	0.607 **(0.000)	0.597 **(0.001)
18	0.593 **(0.000)	0.583 **(0.001)	0.573 **(0.004)	0.559 **(0.019)	0.563 **(0.012)
21	0.599 **(0.000)	$0.534^{*}(0.066)$	$0.555^{**}(0.022)$	0.558 **(0.029)	0.551 **(0.048)
24	0.554 **(0.042)	0.488(0.642)	0.547 *(0.071)	0.529 (0.195)	0.536 (0.118)

NOTES: MH represents monthly forecast horizons. Boldface indicates improvements relative to the no-change forecast. As a rough guide, p-values of a Harvey et al. (1997) small-sample adjustment of the Diebold and Mariano (1995) test are reported in brackets after recursive MSPE ratios. We also report p-values for the Pesaran and Timmermann (2009) test for the null hypothesis of no directional accuracy in brackets after success ratios. * denotes significance at the 10% level and ** at the 5% level.

(III) The inclusion of futures-based forecasts

Analysing the effect of including the futures-based forecasts, in Table A-3a and A-3b we compare the the forecast accuracy of equal weight combinations with and without futures-based forecasts for the 1992:01-2012:09 and 1992:01-2017:12 sample periods at horizons 18 to 24 months for RAC and WTI. As with Brent in the main text, the inclusion of futures-based forecasts at these horizons reduces MSPE ratios and raises the success ratios. Table A-4 additionally presents the effect of including the futures-based forecasts for the Brent measure in the 1992:01-2012:09 evaluation sample.

Table A-3a: Forecast Accuracy for RAC, Equal Weight Combinations, Excluding and Including Futures-based Forecasts (FUTURES)

		Rea	al RAC price	
	199	92:01-2012:09	199	2:01-2017:12
MH	Excluding FUTURES	Including FUTURES	Excluding FUTURES	Including FUTURES
		Recursive M	SPE ratios	
18	1.013(0.706)	$0.974^*(0.073)$	1.000(0.502)	0.944 **(0.000)
19	1.029(0.887)	0.989 (0.269)	1.009(0.727)	0.952 **(0.001)
20	1.044(0.967)	1.004(0.586)	1.026(0.956)	0.964 **(0.008)
21	1.044(0.966)	1.006(0.636)	1.036(0.992)	0.972 **(0.022)
22	1.036(0.923)	1.000(0.505)	1.036(0.990)	0.971 **(0.020)
23	1.022(0.805)	0.991 (0.293)	1.034(0.979)	0.968 ** (0.015)
24	1.014(0.704)	0.987 (0.224)	1.035(0.979)	0.970 **(0.024)
		Success	ratios	
18	0.522 (0.665)	$0.573^{**}(0.001)$	0.508 (0.567)	0.586 **(0.001)
19	0.524 (0.546)	0.580 **(0.000)	0.537 (0.155)	0.595 **(0.000)
20	0.557 (0.198)	0.609 **(0.000)	0.546 (0.136)	0.614 **(0.000)
21	0.502 (0.894)	0.563 **(0.006)	0.479(0.937)	0.565 ** (0.012)
22	0.518 (0.836)	0.566 **(0.009)	0.485(0.902)	0.560 **(0.021)
23	0.546 (0.577)	$0.555^{**}(0.026)$	0.507 (0.714)	$0.552^{**}(0.044)$
24	0.540 (0.693)	0.553 **(0.048)	0.509 (0.737)	0.561 **(0.026)

NOTES: MH represents monthly forecast horizons. Boldface indicates improvements relative to the no-change forecast. As a rough guide, p-values of a Harvey et al. (1997) small-sample adjustment of the Diebold and Mariano (1995) test are reported in brackets after recursive MSPE ratios. We also report p-values for the Pesaran and Timmermann (2009) test for the null hypothesis of no directional accuracy in brackets after success ratios. * denotes significance at the 10% level and ** at the 5% level.

Table A-3b: Forecast Accuracy for WTI, Equal Weight Combinations, Excluding and Including Futures-based Forecasts (FUTURES)

		Rea	al WTI price	
	199	92:01-2012:09	199	2:01-2017:12
MH	Excluding FUTURES	Including FUTURES	Excluding FUTURES	Including FUTURES
		Recursive M	SPE ratios	
18	1.011(0.678)	$0.973^*(0.070)$	0.999 (0.476)	0.944 **(0.000)
19	1.022(0.820)	0.985 (0.206)	1.008(0.693)	0.952 **(0.001)
20	1.035(0.922)	0.998 (0.466)	1.021(0.906)	0.963 **(0.007)
21	1.040(0.942)	1.004(0.599)	1.032(0.973)	0.970 **(0.023)
22	1.027(0.846)	0.995 (0.398)	1.028(0.947)	0.966 **(0.013)
23	1.012(0.667)	0.985 (0.210)	1.022(0.882)	0.960 **(0.007)
24	1.002(0.534)	0.979 (0.146)	1.017(0.808)	0.956 **(0.005)
		Success	ratios	
18	0.526 (0.542)	0.582 **(0.001)	0.522 (0.443)	0.593 **(0.000)
19	0.528 (0.387)	0.593 **(0.000)	0.534 (0.216)	0.609 **(0.000)
20	0.535 (0.411)	0.587 **(0.000)	0.539 (0.226)	0.590 **(0.000)
21	0.498(0.910)	0.581 **(0.003)	0.503 (0.818)	0.599 **(0.000)
22	0.526 (0.753)	0.570 **(0.007)	0.509 (0.768)	$0.584^{**}(0.002)$
23	0.529 (0.687)	$0.551^{**}(0.048)$	0.514 (0.651)	0.569 **(0.012)
24	0.531 (0.720)	0.540 (0.108)	0.505 (0.735)	0.554 **(0.042)

NOTES: MH represents monthly forecast horizons. Boldface indicates improvements relative to the no-change forecast. As a rough guide, p-values of a Harvey et al. (1997) small-sample adjustment of the Diebold and Mariano (1995) test are reported in brackets after recursive MSPE ratios. We also report p-values for the Pesaran and Timmermann (2009) test for the null hypothesis of no directional accuracy in brackets after success ratios. * denotes significance at the 10% level and ** at the 5% level.

Table A-4: Forecast Accuracy for Brent, Equal Weight Combinations, Excluding and Including Futures-based Forecasts (FUTURES)

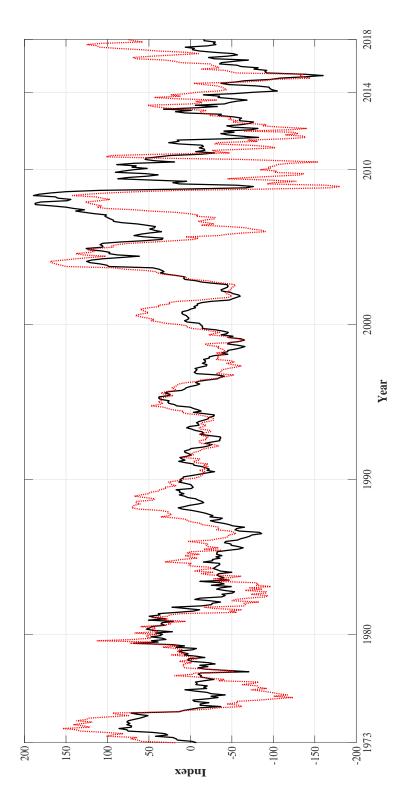
		Real	Brent price	
		1992	2:01-2012:09	
	Recurs	ive MSPE ratios	Suc	cess ratios
МН	Excluding FUTURES	Including FUTURES	Excluding FUTURES	Including FUTURES
9	0.998(0.468)	0.983(0.176)	0.490(0.644)	0.506 (0.315)
10	0.992 (0.365)	$0.975^*(0.071)$	0.504 (0.491)	0.537 **(0.050)
11	0.979 (0.188)	0.961 **(0.012)	0.540 (0.148)	0.573 **(0.004)
12	0.974 (0.131)	0.952 **(0.003)	$0.546^*(0.087)$	0.567 **(0.005)
13	0.974 (0.130)	0.949 **(0.001)	0.515 (0.384)	0.578 **(0.003)
14	0.972 (0.120)	0.945 **(0.001)	0.538 (0.169)	0.568 **(0.005)
15	0.976 (0.154)	0.947 **(0.001)	$0.549^*(0.075)$	0.583 **(0.001)
16	0.989 (0.323)	0.957 **(0.006)	0.534 (0.142)	0.577 **(0.001)
17	1.008(0.631)	0.973 **(0.047)	0.511 (0.280)	0.536 **(0.009)
18	1.023(0.837)	0.986 (0.203)	$0.530^*(0.067)$	0.543 **(0.002)
19	1.036(0.941)	1.001(0.513)	$0.515^*(0.093)$	0.524 **(0.004)
20	1.048(0.983)	1.012(0.787)	$0.526^*(0.099)$	0.522 **(0.005)
21	1.054(0.991)	1.018(0.898)	0.524 (0.203)	0.528 **(0.003)
22	1.051(0.984)	1.018(0.884)	0.504 (0.477)	0.531 **(0.007)
23	1.043(0.958)	1.013(0.787)	0.511 (0.386)	0.515 *(0.051)
24	1.041(0.945)	1.014(0.799)	0.491(0.672)	0.491(0.253)

NOTES: MH represents monthly forecast horizons. Boldface indicates improvements relative to the no-change forecast. As a rough guide, p-values of a Harvey et al. (1997) small-sample adjustment of the Diebold and Mariano (1995) test are reported in brackets after recursive MSPE ratios. We also report p-values for the Pesaran and Timmermann (2009) test for the null hypothesis of no directional accuracy in brackets after success ratios. * denotes significance at the 10% level and ** at the 5% level

(IV) Activity Indexes

Hamilton (2018) proposes a 24-month cumulative activity growth rate based on real shipping rates. This series and the rea are plotted in Figure A-1, see the online dataset documentation for more details.

If we use Hamilton's 24-month cumulative activity growth rate in the VAR, the forecast performance is fairly similar, and the influence on the forecast produced using the equal-weight combination is negligible. The results are presented in Tables A-5, A-6, and A-7 for the three real oil prices measures.



---Kilian (2009) rea ----- Hamilton (2018) 24-month cumulative growth rate

Figure A-1: Kilian (2009) rea and Hamilton (2018) 24-month cumulative activity growth rate

Table A-5: Forecast Accuracy for RAC, VAR & Equal Weight Combination, using Kilian (2009) rea and Hamilton (2018) 24-month cumulative activity growth rate

		Transaction 1994:01 to 4014:09						
		VAR	Equal Weig	Equal Weight Combination		VAR	Equal Weig	Equal Weight Combination
MH	Kilian	Hamilton	- Kilian	Hamilton	- Kilian	Hamilton	Kilian	Hamilton
				Recursive MSPE ratios	E ratios			
1	0.990 (0.465)	1.011(0.529)	$0.928^{**}(0.028)$	$0.921^{**}(0.031)$	0.988 (0.452)	1.007(0.523)	$0.931^{**}(0.015)$	$0.925^{**}(0.019)$
33	1.051(0.678)	1.081(0.689)	$0.922^{**}(0.008)$	$0.911^{**}(0.011)$	1.014(0.558)	1.049(0.641)	$0.923^{**}(0.002)$	$0.916^{**}(0.004)$
9	1.186(0.988)	1.183(0.983)	0.985 (0.172)	0.982 (0.145)	1.105(0.926)	1.112(0.934)	$0.977^{**}(0.048)$	$0.978^{*}(0.059)$
6	1.232(1.000)	1.271(1.000)	0.980 (0.111)	0.986 (0.176)	1.119(0.986)	1.158(0.998)	$0.971^{**}(0.015)$	$0.978^{**}(0.036)$
12	1.231(1.000)	1.282(1.000)	$0.941^{**}(0.001)$	$0.947^{**}(0.002)$	1.089(0.953)	1.143(0.996)	$0.936^{**}(0.000)$	$0.944^{**}(0.000)$
15	1.257(1.000)	1.283(1.000)	$0.932^{**}(0.000)$	$0.935^{**}(0.000)$	1.074(0.894)	1.108(0.969)	$0.932^{**}(0.000)$	$0.938^{**}(0.000)$
18	1.322(1.000)	1.327(1.000)	$0.974^*(0.073)$	$0.974^*(0.072)$	1.062(0.829)	1.084(0.914)	$0.944^{**}(0.000)$	$0.949^{**}(0.000)$
21	1.369(1.000)	1.383(1.000)	1.006(0.636)	1.009(0.706)	1.044(0.735)	1.078(0.870)	$0.972^{**}(0.022)$	$0.978^{*}(0.056)$
24	1.385(1.000)	1.385(1.000)	0.987 (0.224)	0.987 (0.225)	1.034(0.675)	1.059(0.801)	$0.970^{**}(0.024)$	$0.975^{**}(0.042)$
				Success ratios	tios			
	$0.546^{*}(0.083)$	$\mathbf{0.558^{**}} (0.041)$	$0.562^{**}(0.050)$	$0.566^{**}(0.038)$	$\mathbf{0.558^{**}}(0.022)$	$0.564^{**}(0.014)$	$0.558^{**}(0.042)$	$0.567^{**}(0.019)$
3	0.526 (0.214)	0.522 (0.248)	$0.575^{**}(0.034)$	$0.583^{**}(0.019)$	0.532 (0.113)	0.526 (0.169)	$0.597^{**}(0.002)$	$0.606^{**}(0.000)$
9	0.475(0.743)	0.426(0.993)	0.545 (0.201)	$0.566^*(0.091)$	0.495(0.500)	0.469(0.868)	$0.573^{**}(0.021)$	$\mathbf{0.590^{**}}(0.005)$
6	0.444(0.949)	0.427(0.994)	0.539 (0.171)	0.523 (0.419)	0.480(0.700)	0.464(0.896)	$0.549^{*}(0.068)$	0.543 (0.117)
12	0.521 (0.167)	0.475(0.857)	$0.639^{**}(0.000)$	$0.634^{**}(0.000)$	$0.578^{**}(0.001)$	$0.538^*(0.070)$	$0.645^{**}(0.000)$	$0.638^{**}(0.000)$
15	0.515 (0.261)	0.455(0.968)	$0.617^{**}(0.000)$	$0.591^{**}(0.007)$	$0.560^{**}(0.006)$	0.510 (0.332)	$0.614^{**}(0.000)$	$0.594^{**}(0.001)$
18	0.513 (0.315)	0.470(0.919)	$0.573^{**}(0.001)$	$0.565^{**}(0.009)$	$0.569^{**}(0.004)$	$0.539^{*}(0.075)$	$0.586^{**}(0.001)$	$0.569^{**}(0.007)$
21	0.502 (0.533)	0.476(0.926)	$0.563^{**}(0.006)$	$0.546^{*}(0.058)$	$0.565^{**}(0.005)$	$0.551^{**}(0.028)$	$0.565^{**}(0.012)$	$0.551^{**}(0.047)$
24	0.500(0.649)	0.491(0.835)	$0.553^{**}(0.048)$	0.544 (0.123)	$0.561^{**}(0.011)$	$0.547^{**}(0.042)$	$0.561^{**}(0.026)$	$0.554^*(0.051)$

small-sample adjustment of the Diebold and Mariano (1995) test are reported in brackets after recursive MSPE ratios. We also report p-values for the Pesaran and Timmermann (2009) test for the null hypothesis of no directional accuracy in brackets after success ratios. * denotes significance at the 10% level and ** at the 5% level. NOTES: MH represents monthly forecast horizons. Boldface indicates improvements relative to the no-change forecast. As a rough guide, p-values of a Harvey et al. (1997)

Table A-6: Forecast Accuracy for WTI, VAR & Equal Weight Combination, using Kilian (2009) rea and Hamilton (2018) 24-month cumulative activity growth rate

		VAR	Equal Weig	Equal Weight Combination	,	VAR	Equal Weig	Equal Weight Combination
$_{ m MH}$	Kilian	Hamilton	Kilian	Hamilton	Kilian	Hamilton	Kilian	Hamilton
				Recursive MSPE ratios	E ratios			
1	1.009(0.533)	1.050(0.630)	$0.904^{**}(0.007)$	$0.898^{**}(0.010)$	1.001(0.506)	1.036(0.612)	$0.907^{**}(0.002)$	$0.903^{**}(0.004)$
3	1.041(0.640)	1.103(0.739)	$\mathbf{0.923^{**}}(0.010)$	$0.916^{**}(0.017)$	1.011(0.547)	1.076(0.717)	$\mathbf{0.923^{**}}(0.002)$	$\mathbf{0.920^{**}}(0.007)$
9	1.141(0.955)	1.172(0.973)	0.988 (0.242)	0.990 (0.301)	1.075(0.846)	1.113(0.930)	$0.979^{*}(0.079)$	0.984 (0.161)
6	1.177(0.999)	1.233(1.000)	0.982 (0.146)	0.991 (0.281)	1.094(0.963)	1.145(0.997)	$0.973^{**}(0.027)$	$0.982^{*}(0.076)$
12	1.176(0.997)	1.245(1.000)	$0.948^{**}(0.004)$	$0.957^{**}(0.011)$	1.075(0.922)	1.143(0.996)	$0.942^{**}(0.000)$	$0.952^{**}(0.001)$
15	1.192(0.995)	1.235(0.999)	$0.942^{**}(0.002)$	$0.948^{**}(0.005)$	1.054(0.813)	1.100(0.957)	$0.937^{**}(0.000)$	$0.944^{**}(0.000)$
18	1.242(0.998)	1.265(0.999)	$0.973^*(0.070)$	$0.977^*(0.094)$	1.041(0.728)	1.076(0.884)	$0.944^{**}(0.000)$	$0.951^{**}(0.001)$
21	1.280(0.998)	1.311(0.999)	1.004(0.599)	1.011(0.729)	1.029(0.653)	1.072(0.846)	$0.970^{**}(0.023)$	$0.979^{*}(0.071)$
24	1.301(0.997)	1.313(0.999)	0.979 (0.146)	0.982 (0.170)	1.026(0.630)	1.062(0.800)	$0.956^{**}(0.005)$	$0.963^{**}(0.012)$
				Success ratios	ios			
1	0.518 (0.329)	0.506 (0.499)	0.542 (0.201)	0.530 (0.348)	0.535 (0.115)	0.522 (0.245)	$0.558^*(0.059)$	$0.558^{*}(0.065)$
3	$0.547^{*}(0.076)$	0.518 (0.291)	0.551 (0.158)	0.530 (0.377)	$0.545^{**}(0.047)$	0.519 (0.234)	$0.577^{**}(0.012)$	$0.558^{*}(0.063)$
9	0.484(0.653)	0.443(0.974)	0.525 (0.425)	0.553 (0.172)	0.498(0.450)	0.472(0.842)	0.544 (0.169)	$0.573^{**}(0.026)$
6	0.477(0.722)	0.452(0.958)	$0.552^*(0.082)$	0.523 (0.402)	0.487(0.607)	0.464(0.896)	$0.572^{**}(0.011)$	$0.553^{*}(0.068)$
12	0.496(0.468)	0.450(0.963)	$0.584^{**}(0.005)$	$0.563^*(0.064)$	$0.532^*(0.065)$	0.492(0.562)	$0.618^{**}(0.000)$	$0.605^{**}(0.000)$
15	0.532 (0.128)	0.481(0.827)	$0.587^{**}(0.004)$	$0.579^{**}(0.017)$	$0.560^{**}(0.006)$	0.510 (0.332)	$0.614^{**}(0.000)$	$0.607^{**}(0.000)$
18	0.526 (0.190)	0.474(0.887)	$0.582^{**}(0.001)$	$0.560^{**}(0.013)$	$0.553^{**}(0.014)$	0.508 (0.336)	$0.593^{**}(0.000)$	$0.569^{**}(0.005)$
21	0.520 (0.317)	0.493(0.812)	$0.581^{**}(0.003)$	$0.568^{**}(0.016)$	$0.555^{**}(0.010)$	$0.541^*(0.053)$	$0.599^{**}(0.000)$	$0.579^{**}(0.006)$
24	0.496(0.685)	0.487 (0.851)	0.540 (0.108)	0.531 (0.266)	$0.561^{**}(0.012)$	$0.547^{**}(0.044)$	$0.554^{**}(0.042)$	$0.547^*(0.083)$

small-sample adjustment of the Diebold and Mariano (1995) test are reported in brackets after recursive MSPE ratios. We also report p-values for the Pesaran and Timmermann (2009) test for the null hypothesis of no directional accuracy in brackets after success ratios. * denotes significance at the 10% level and ** at the 5% level. NOTES: MH represents monthly forecast horizons. Boldface indicates improvements relative to the no-change forecast. As a rough guide, p-values of a Harvey et al. (1997)

Table A-7: Forecast Accuracy for BRENT, VAR & Equal Weight Combination, using Kilian (2009) rea and Hamilton (2018) 24-month cumulative activity growth rate

		Evaluation 1	1992:01 to 2012:09			Evaluation 1	Evaluation 1992:01 to 2017:12	
		VAR	Equal Weig	Equal Weight Combination		VAR	Equal Weig	Equal Weight Combination
MH	Kilian	Hamilton		Hamilton	Kilian	Hamilton	- Kilian	Hamilton
				Recursive MSPE ratios	E ratios			
П	1.017(0.563)	1.083(0.720)	0.956 (0.110)	0.953 (0.122)	1.017(0.571)	1.077(0.742)	$0.941^{**}(0.030)$	$0.939^{**}(0.039)$
3	1.057(0.697)	1.138(0.802)	$0.941^{**}(0.024)$	$0.934^{**}(0.031)$	1.040(0.665)	1.123(0.823)	$0.935^{**}(0.005)$	$0.932^{**}(0.010)$
9	1.180(0.986)	1.205(0.989)	0.995 (0.394)	0.995 (0.397)	1.111(0.936)	1.144(0.969)	$0.978^{*}(0.093)$	0.981 (0.118)
6	1.219(1.000)	1.261(1.000)	0.983 (0.176)	0.990 (0.255)	1.116(0.986)	1.159(0.999)	$0.961^{**}(0.007)$	$0.968^{**}(0.011)$
12	1.233(1.000)	1.287(1.000)	$0.952^{**}(0.003)$	$0.958^{**}(0.005)$	1.089(0.953)	1.150(0.997)	$0.929^{**}(0.000)$	$0.937^{**}(0.000)$
15	1.264(1.000)	1.297(1.000)	$0.947^{**}(0.001)$	$0.951^{**}(0.001)$	1.074(0.892)	1.118(0.979)	$0.923^{**}(0.000)$	$0.930^{**}(0.000)$
18	1.315(1.000)	1.326(1.000)	0.986 (0.203)	0.988 (0.216)	1.069(0.854)	1.096(0.942)	$0.937^{**}(0.000)$	$0.943^{**}(0.000)$
21	1.346(1.000)	1.362(1.000)	1.018(0.898)	1.022(0.940)	1.049(0.759)	1.084(0.897)	$0.955^{**}(0.002)$	$0.962^{**}(0.004)$
24	1.358(1.000)	1.359(1.000)	1.014(0.799)	1.014(0.822)	1.032(0.672)	1.061(0.817)	$0.950^{**}(0.002)$	$0.955^{**}(0.002)$
				Success ratios	tios			
1	0.502 (0.510)	0.498(0.575)	0.514 (0.199)	$0.526^*(0.094)$	0.513 (0.341)	0.506 (0.446)	$0.526^*(0.069)$	$0.542^{**} (0.017)$
3	0.510 (0.395)	0.498(0.539)	0.538 (0.134)	0.522 (0.263)	0.516 (0.263)	0.510 (0.352)	$0.561^{**}(0.015)$	$0.542^*(0.070)$
9	0.480(0.694)	0.439(0.983)	0.496(0.552)	0.480(0.743)	0.495(0.507)	0.469(0.867)	0.534 (0.112)	0.524 (0.203)
6	0.452(0.915)	0.436(0.989)	0.506 (0.315)	0.481(0.602)	0.477(0.729)	0.467(0.874)	$0.569^{**}(0.003)$	$0.553^{**}(0.015)$
12	0.479(0.680)	0.433(0.989)	$0.567^{**}(0.005)$	$0.580^{**}(0.002)$	$0.538^*(0.061)$	0.505 (0.404)	$0.605^{**}(0.000)$	$0.608^{**}(0.000)$
15	0.506 (0.370)	0.447(0.978)	$0.583^{**}(0.001)$	$0.562^{**}(0.011)$	$0.560^{**}(0.009)$	0.510 (0.344)	$0.621^{**}(0.000)$	$0.611^{**}(0.000)$
18	0.509 (0.361)	0.466(0.945)	$0.543^{**}(0.002)$	$0.552^{**}(0.001)$	$0.576^{**}(0.002)$	$0.539^*(0.073)$	$0.586^{**}(0.000)$	$0.603^{**}(0.000)$
21	0.502 (0.533)	0.485(0.879)	$0.528^{**}(0.003)$	$0.546^{**}(0.000)$	$0.572^{**}(0.003)$	$0.565^{**}(0.009)$	$0.558^{**}(0.004)$	$0.579^{**}(0.000)$
24	0.478(0.849)	0.469(0.945)	0.491(0.253)	0.491(0.253)	$0.554^{**}(0.025)$	$0.540^{*}(0.076)$	$0.540^{*}(0.055)$	$0.547^{**}(0.031)$

small-sample adjustment of the Diebold and Mariano (1995) test are reported in brackets after recursive MSPE ratios. We also report p-values for the Pesaran and Timmermann (2009) test for the null hypothesis of no directional accuracy in brackets after success ratios. * denotes significance at the 10% level and ** at the 5% level. NOTES: MH represents monthly forecast horizons. Boldface indicates improvements relative to the no-change forecast. As a rough guide, p-values of a Harvey et al. (1997)

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