

JAWABAN TUGAS KEL 4806

Tabel Awal

| cj | Basis | K | 2 | 1 | 3 | 0 | 0 | 0 |
|----|-------|----|----|----|----|----|----|----|
| | | | x1 | x2 | x3 | s1 | s2 | s3 |
| 0 | s1 | 59 | 1 | 1 | 1 | 1 | 0 | 0 |
| 0 | s2 | 75 | 2 | 0 | 3 | 0 | 1 | 0 |
| 0 | s3 | 54 | 0 | 1 | 6 | 0 | 0 | 1 |
| | zj | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| | cj-zj | | 2 | 1 | 3 | 0 | 0 | 0 |

Nilai baris cj-zj terbesar di kolom x3. Kolom pivot kolom x3

<----- Model PL

Maks $Z=2x_1+x_2+3x_3$

Batasan

$$x_1+x_2+x_3 \leq 59$$

$$2x_1+3x_3 \leq 75$$

$$x_2+6x_3 \leq 54$$

$$x_1 \geq 0, x_2 \geq 0, x_3 \geq 0$$

Bentuk standar

Maks $Z=2x_1+x_2+3x_3+0s_1+0s_2+0s_3$

Batasan

$$x_1+x_2+x_3+s_1=59$$

$$2x_1+3x_3+s_2=75$$

$$x_2+6x_3+s_3=54$$

$$x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, s_1 \geq 0, s_2 \geq 0, s_3 \geq 0$$

Tabel I

| cj | Basis | K | 2 | 1 | 3 | 0 | 0 | 0 |
|----|-------|----|----|----|----|----|----|----|
| | | | x1 | x2 | x3 | s1 | s2 | s3 |
| 0 | s1 | 59 | 1 | 1 | 1 | 1 | 0 | 0 |
| 0 | s2 | 75 | 2 | 0 | 3 | 0 | 1 | 0 |
| 0 | s3 | 54 | 0 | 1 | 6 | 0 | 0 | 1 |
| | zj | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| | cj-zj | | 2 | 1 | 3 | 0 | 0 | 0 |

Menentukan baris pivot dan nilai pivot

Baris pivot s3

Nilai pivot = 6

Nilai kolom [3 x3] menggantikan baris [0 s3]

Tabel II

| cj | Basis | K | 2 | 1 | 3 | 0 | 0 | 0 |
|----|-------|----|----|------|----|----|----|------|
| | | | x1 | x2 | x3 | s1 | s2 | s3 |
| 0 | s1 | 50 | 1 | 5/6 | 0 | 1 | 0 | -1/6 |
| 0 | s2 | 48 | 2 | -1/2 | 0 | 0 | 1 | -1/2 |
| 3 | x3 | 9 | 0 | 1/6 | 1 | 0 | 0 | 1/6 |
| | zj | 27 | 0 | 1/2 | 3 | 0 | 0 | 1/2 |
| | cj-zj | | 2 | 1/2 | 0 | 0 | 0 | -1/2 |

Tabel II belum optimal. Kolom pivot berikutnya kolom x1

Nilai **positif terkecil** ada di baris s2, yaitu 24, sehingga terpilih sbg baris pivot. Dengan elemen pivot = 1

Nilai kolom [2 x1] menggantikan nilai baris [0 s2]

<----- Berdasarkan nilai pivot, maka baris s1, s2 dan x3 menjadi sbb:

Baris x3 (dibagi elemen pivot)

| | | | | | | |
|---|---|-----|---|---|---|-----|
| 9 | 0 | 1/6 | 1 | 0 | 0 | 1/6 |
|---|---|-----|---|---|---|-----|

Baris s1

| | | | | | | |
|--------|---|-----|---|---|---|------|
| 59 | 1 | 1 | 1 | 1 | 0 | 0 |
| (1)x 9 | 0 | 1/6 | 1 | 0 | 0 | 1/6 |
| 50 | 1 | 5/6 | 0 | 1 | 0 | -1/6 |

Baris s2

| | | | | | | |
|--------|---|------|---|---|---|------|
| 75 | 2 | 0 | 3 | 0 | 1 | 0 |
| (3)x 9 | 0 | 1/6 | 1 | 0 | 0 | 1/6 |
| 48 | 2 | -1/2 | 0 | 0 | 1 | -1/2 |

| | | | | | | | | | | |
|-----------|----|-------|----|----|-------|----|----|------|------|------------------|
| Tabel III | cj | Basis | K | 2 | 1 | 3 | 0 | 0 | 0 | |
| | | | | x1 | x2 | x3 | s1 | s2 | s3 | |
| | 0 | s1 | 26 | 0 | 13/12 | 0 | 1 | -1/2 | 1/12 | $=26/(12/13)=24$ |
| | 2 | x1 | 24 | 1 | -1/4 | 0 | 0 | 1/2 | -1/4 | $=24/(-1/4)=-96$ |
| | 3 | x3 | 9 | 0 | 1/6 | 1 | 0 | 0 | 1/6 | $=9/(1/6)=54$ |
| | | zj | 75 | 2 | 0 | 3 | 0 | 1 | 0 | |
| | | cj-zj | | 0 | 1 | 0 | 0 | -1 | 0 | |

Tabel III belum optimal. Kolom pivot berikutnya kolom x2
 Nilai **positif terkecil** ada di baris s1, yaitu 24, sehingga terpilih sbg baris pivot. Dengan elemen pivot = 13/12
 Nilai kolom [1 x2] menggantikan nilai baris [0 s1]

<----- Berdasarkan nilai pivot, maka baris x1, s1 dan x3 menjadi sbb:

Baris x1 (dibagi elemen pivot)

| | | | | | | | |
|----|---|------|---|---|-----|------|--|
| 24 | 1 | -1/4 | 0 | 0 | 1/2 | -1/4 | |
|----|---|------|---|---|-----|------|--|

Baris s1

| | | | | | | | |
|---------|---|-------|---|---|------|------|---|
| 50 | 1 | 5/6 | 0 | 1 | 0 | -1/6 | |
| (1)x 24 | 1 | -1/4 | 0 | 0 | 1/2 | -1/4 | - |
| 26 | 0 | 13/12 | 0 | 1 | -1/2 | 1/12 | |

Baris x3

| | | | | | | | |
|---------|---|------|---|---|-----|------|---|
| 9 | 0 | 1/6 | 1 | 0 | 0 | 1/6 | |
| (0)x 24 | 1 | -1/4 | 0 | 0 | 1/2 | -1/4 | - |
| 9 | 0 | 1/6 | 1 | 0 | 0 | 1/6 | |

| | | | | | | | | | | |
|----------|----|-------|----|----|----|----|--------|-------|-------|--|
| Tabel IV | cj | Basis | K | 2 | 1 | 3 | 0 | 0 | 0 | |
| | | | | x1 | x2 | x3 | s1 | s2 | s3 | |
| | 1 | x2 | 24 | 0 | 1 | 0 | 12/13 | -6/13 | 1/13 | |
| | 2 | x1 | 30 | 1 | 0 | 0 | 3/13 | 5/13 | -3/13 | |
| | 3 | x3 | 5 | 0 | 0 | 1 | -2/13 | 1/13 | 2/13 | |
| | | zj | 99 | 2 | 1 | 3 | 12/13 | 7/13 | 1/13 | |
| | | cj-zj | | 0 | 0 | 0 | -12/13 | -7/13 | -1/13 | |

Tabel IV sudah optimal
 Solusi

$$\begin{aligned}
 x1 &= 30 \\
 x2 &= 24 \\
 x3 &= 5 \\
 Z \text{ maks} &= 2x1 + x2 + 3x3 \\
 &= 2*(30) + (24) + 3*(5) \\
 &= 60 + 24 + 15 \\
 &= 99
 \end{aligned}$$

<----- Berdasarkan nilai pivot, maka baris x2, x1 dan x3 menjadi sbb:

Baris x2 (dibagi elemen pivot)

| | | | | | | | |
|----|---|---|---|-------|-------|------|--|
| 24 | 0 | 1 | 0 | 12/13 | -6/13 | 1/13 | |
|----|---|---|---|-------|-------|------|--|

Baris x1

| | | | | | | | |
|------------|---|------|---|-------|-------|-------|---|
| 24 | 1 | -1/4 | 0 | 0 | 1/2 | -1/4 | |
| (-1/4)x 24 | 0 | 1 | 0 | 12/13 | -6/13 | 1/13 | - |
| 30 | 1 | 0 | 0 | 3/13 | 5/13 | -3/13 | |

Baris x3

| | | | | | | | |
|-----------|---|-----|---|-------|-------|------|---|
| 9 | 0 | 1/6 | 1 | 0 | 0 | 1/6 | |
| (1/6)x 24 | 0 | 1 | 0 | 12/13 | -6/13 | 1/13 | - |
| 5 | 0 | 0 | 1 | -2/13 | 1/13 | 2/13 | |