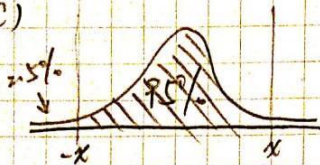


[1]

$$(a) f_Z(z) = \frac{1}{\sqrt{2\pi}} e^{-z^2/2}$$

$$(b) P(-1 < X < 1) = \frac{1}{\sqrt{2\pi}} \int_{-1}^1 e^{-\frac{x^2}{2}} dx = 0.68269.$$

(c)



$$97.5\% = 0.975 \Rightarrow z = 1.96.$$

$$A = 1.96.$$

$$(d) f_Q(q) = \begin{cases} \frac{1}{z^{\frac{1}{2}} \Gamma(1/2)} e^{-\frac{1}{z}} e^{-\frac{q^2}{z}}, & q > 0 \\ 0, & \text{其他} \end{cases}$$

$$(e) E[Q] = 1.$$

$$(f) \text{std}[Q] = \sqrt{2}.$$

$$(g) P(Q \leq 1) = \int_0^1 \frac{1}{\sqrt{2\pi}} \cdot x^{-\frac{1}{2}} \cdot e^{-\frac{x}{2}} dx$$

[2]

$$(a) f_T(t) = \begin{cases} e^{-t}, & t > 0 \\ 0, & \text{其他} \end{cases}$$

$$\alpha = 3$$

$$\beta = 1.$$

$$(b) E(T) = 1.$$

$$(c) \text{std}[T] = 1.$$

$$(d) P(T > 1) = \int_1^{\infty} e^{-t} dt = (-e^{-\infty} + e^{-1}) = e^{-1}.$$

$$(e) f_{T_3}(t) = \begin{cases} \frac{1}{\Gamma(3)} t^2 \cdot e^{-t}, & t > 0 \\ 0, & \text{其他} \end{cases}$$

$$(f) E[T_3] = \alpha\beta = 3.$$

$$(g) \text{std}[T_3] = \sqrt{\alpha\beta^2} = \sqrt{3}.$$

$$(h) P(T_3 > 3) = \int_3^{\infty} \frac{1}{\Gamma(3)} t^2 \cdot e^{-t} dt = 0.423 \neq$$

$$(i) P(T_3 > 1) = 0.0296.$$

st. gamma. sf (x=1, a=3, scale=1).

不接受.