

Fundamental Algorithms Problem Set 5

Q1.

a) Merge-Sort on n^2 items

$$\Theta(n \lg n) \Rightarrow n^2 \lg n^2 \Rightarrow 2 \cdot n^2 \lg n \Rightarrow \boxed{\Theta(n^2 \lg n)}$$

b) $n = 2^m$ ANNA takes $\Theta(m^2 2^m)$,

$$\downarrow$$

$$m = \log_2 n$$

$$m^2 2^m$$

$$= (\log_2 n)^2 2^{\log_2 n}$$

$$= (\log_2 n)^2 n \Rightarrow \boxed{\Theta(n \lg^2 n)}$$

c) $n = 2^m$ BOB takes $\Theta(5^m)$

$$m = \log_2 n$$

$$5^m$$

$$= 5^{\log_2 n}$$

$$\Rightarrow \boxed{\Theta(5^{\log_2 n}) \text{ or } \Theta(n^{\lg 5})}$$

d) COUNTING SORT sort n^2 items with each item in range $0 - n^3 - 1$

According to Complexity time of Counting Sort:

$$O(\max(N, K)) \quad K \text{ is } (n^3 - 1) \text{ here } N \text{ is } n^2$$

$$\therefore O(n^3 - 1) \Rightarrow O(n^3)$$

e) RADIX-SORT take to sort n^2 items with each item in range $0 - n^3 - 1$ and base n is used. \therefore base n

$$\text{Item range is } 0 - n^3 - 1$$

$$\therefore D = \log_n(n^3 - 1)$$

$$\therefore \max(N, K) = n^2$$

$$\therefore O(\log_n(n^3 - 1) \cdot n^2) \Rightarrow O(n^2)$$

Q2. Hashing with chaining.

A	B	C	D	E	F	G	H	I	J
1	2	3	4	5	6	7	8	9	10
K	L	M	N	O	P	Q	R	S	T
11	12	13	14	15	16	17	18	19	20
U	V	W	X	Y	Z				
21	22	23	24	25	26				

$$h(\text{COBB}) = (3 + (5 + 2 + 2)) \bmod 7 = 1$$

$$h(\text{RUTH}) = (18 + 21 + 20 + 8) \bmod 7 = 4$$

$$h(\text{ROSE}) = (18 + 15 + 19 + 5) \bmod 7 = 1$$

$$h(\text{BUZ}) = (2 + 21 + 26) \bmod 7 = 0$$

$$h(\text{DOC}) = (4 + 15 + 3) \bmod 7 = 1$$

Insert(COBB): 1 → COBB

Insert(RUTH): 4 → RUTH

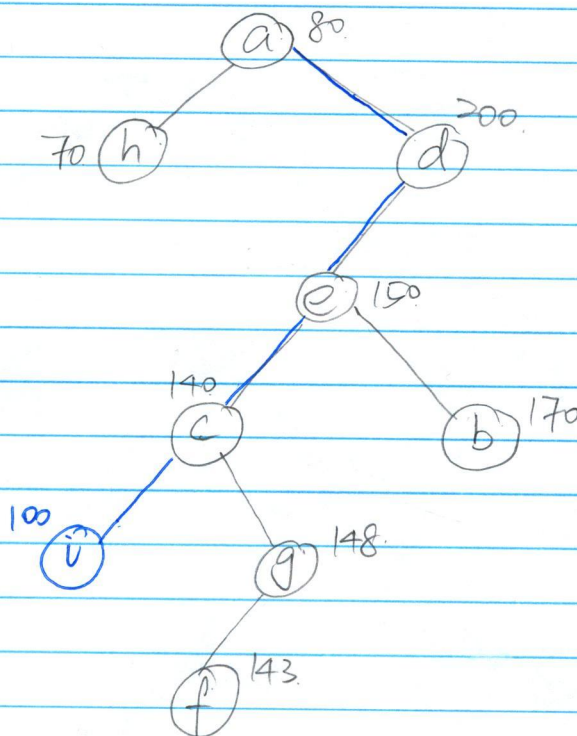
Insert(ROSE): 1 → ROSE → COBB

Search(BUZ): 0
go through: place 0

Insert(DOC): 1 → DOC → ROSE → COBB

continued at
next page

Q3. BST T with vertices a, b, c, d, e, f, g, h ROOT [T] = a



Insert [i] where $\text{key}[i] = 100$

Path $\rightarrow a$. right $\rightarrow d$. left $\rightarrow e$. left $\rightarrow c$. left

$100 > 80$

$100 < 200$

$100 < 150$

$100 < 140$

Q3 continued

Delete COBB: 1

0

1 \rightarrow [DOC] \rightarrow [ROSE]

2

3

4 \rightarrow [PUTH]

5

6