

CS 354 - Machine Organization & Programming

Tuesday, October 22, 2019

Project p3 (6%): DUE at 10 pm on Monday, October 28th

Last Time

- Memory Hierarchy
- Locality
- Bad Locality
- Rethinking Addressing
- Caching Basic Idea

Today

- Caching Basic Idea (from last time)
- Designing a Cache - Blocks
- Designing a Cache - Sets and Tags
- Basic Cache Lines
- Basic Cache Operation
- Basic Cache Practice
- Direct Mapped Cache
- Set Associative Cache

Next Time

- Cache Performance and Coding Considerations

Read: B&O 6.4.5 - 6.4.7, 6.5 - 6.7

Designing a Cache - Blocks

- * The bits of an address are used to look up if a block is in a cache.

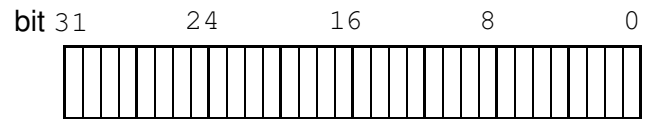
How many bytes in an address space?

$$M = 2^m$$

$$m = \log_2 M$$

Let M be number of bytes in AS. ^{2A-32} 4GB.

32-bit Address Breakdown



Thus m is number of bits in Addr 32 bits.

How big is a block?

$$B = 2^b$$

$$b = \log_2 B$$

Let B be, number of byte 32 bytes. set by CPU Architecture.
per block

b bits: bits in addr that identify which byte in block to access.

- What is the problem with using the most significant bits (left side) for the b bits?

- * Cache blocks must be big enough to capture (nearby) spatial locality.
but small enough to minimize mem latency.

How many 32-byte blocks of memory in a 32-bit address space?

$$2^{(m-b)} = 2^{(32-5)} = 2^{27} = 128M \text{ Blocks.}$$

- * The remaining bits of an address are the blocks number but they're divided into 2 more parts used to access A. cache.

Designing a Cache - Sets & Tags

* A cache must be searched if an unrestrictive PP is used.

→ Problem? slow, worst case $O(N)$ where N is number of locations.

Improvement? limited locs where block can be stored to a specific set.

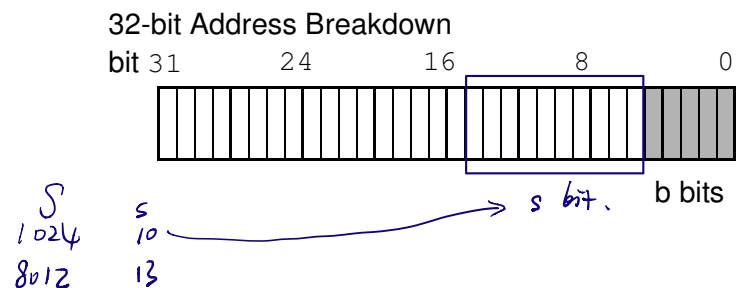
set: loc in cache where block is uniquely mapped.

How many sets in the cache?

$$S = 2^s$$

$$s = \log_2 S$$

Let S be number of sets in caches.



s bits: identify which set in cache to look in.

➤ What is the problem with using the most significant bits (left side) for the s bits?

→ How many blocks map to each set for a 32-bit AS and a cache with 1024 sets? 8192 sets?

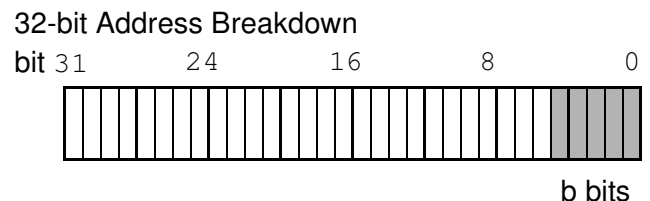
$$1024 \quad 2^{(m-s-b)} = 2^{(32-10-5)} = 2^{17} = 128 \text{ K blocks}$$

$$8192 \quad 16 \text{ K blocks}$$

* Different blocks of memory that map to same set might result in collisions/conflicts.

Since different blocks map to the same set how do we identify which block is in a set?

use remaining bits of address as a unique tag.



t bits: bits of an address that identify which block from address space.

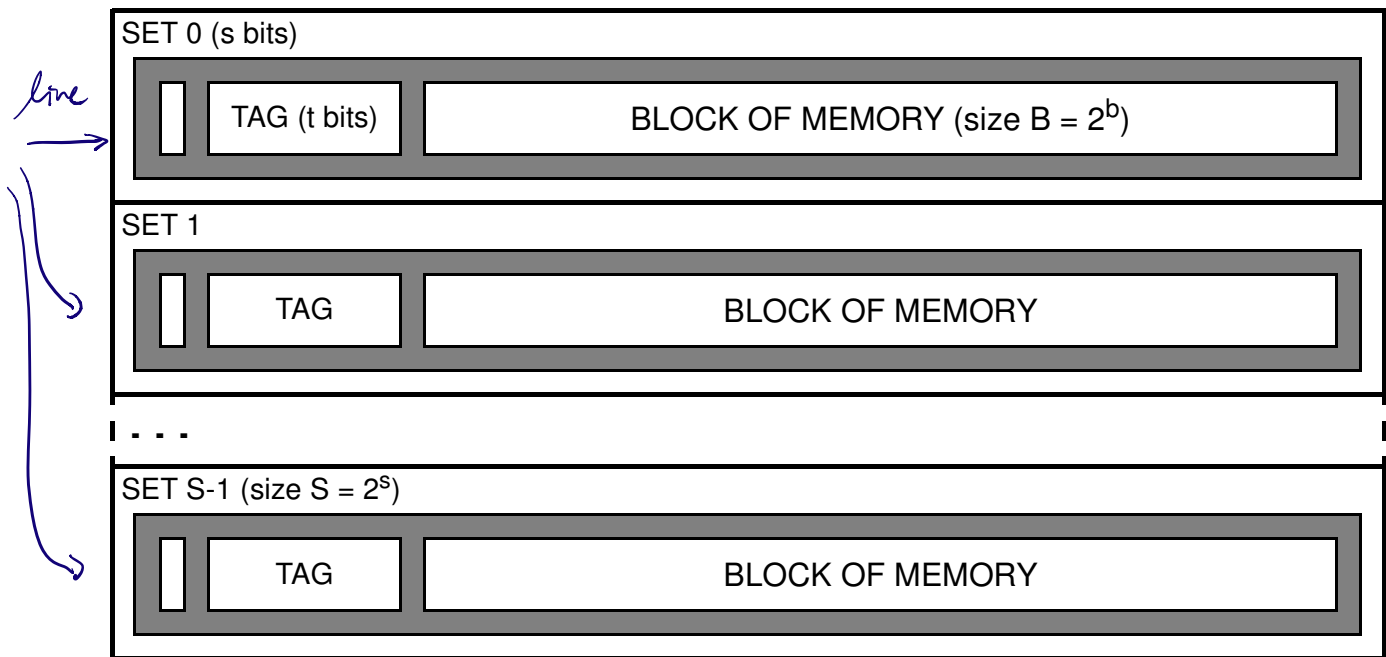
Basic Cache Lines

What? A line is

- ♦ one location in cache.
- ♦ composed of storage for one block and info needed for cache function.

* In our basic cache each set has only 1 line.

Basic Cache Diagram



→ How do you know if a line in the cache is used or not?

use a valid bit.

0 = invalid (Empty)

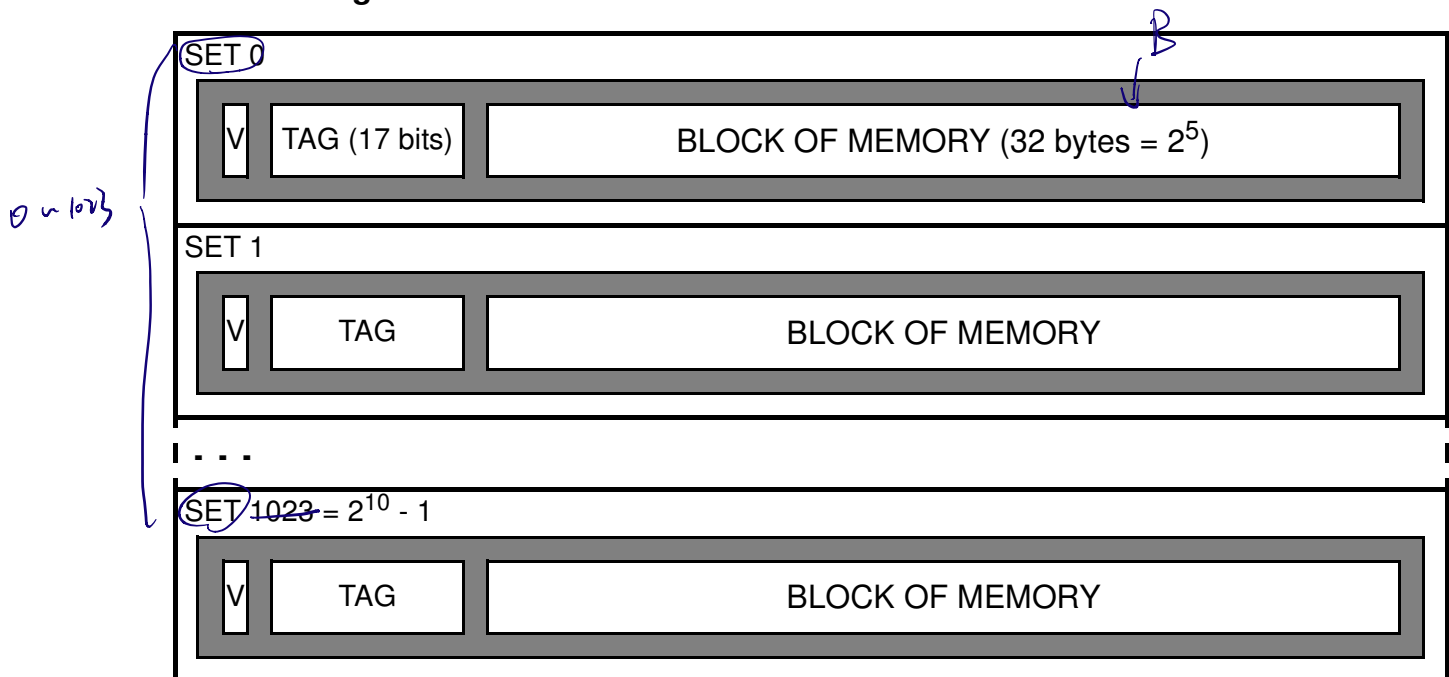
1 = valid (Full)

→ How big is a basic cache given S sets with blocks having B bytes?

$$S \times B$$

Basic Cache Operation

Basic Cache Diagram



→ How big is this basic cache? $S \times B = 32K \text{ Bytes.}$
1K 32

How does a cache process a request for a word at a particular address?

1. Set Selection

extract s bits to identify which set to check.

32-bit Address Breakdown



2. Line Matching

extract t bits and compare with lines' Tag

if no match or valid bit is 0 *Miss!*

Fetch from next lower level.

if match and valid bit is 1 *Hits Faster mem access*

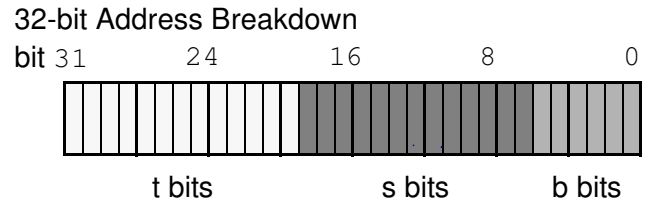
For L1 cache only

3. word extraction.

uses word offsets bits to identify which word in block is accessed.

Basic Cache Practice

You are given the following 32-bit address breakdown used by a cache:



→ How big are the blocks?

$$B = 2^6 = 64$$

→ How many sets? $2^{13} = 8 \text{ K sets}$

→ How big is this basic cache?

$$S \times B = 2^{13} \times 2^6 = 2^{19} = 512 \text{ K bytes}$$

Assume the cache design above is given the following specific address: 0x07515E2B

0	7	5	1	5	E	2	B
0000	0111	0101	0001	0101	1110	0010	1011
s						b	
						word offset	

→ Which set should be checked given the address above?

Convert s bits to decimal

1400

→ Which word in the block does the L1 cache access for the address?

Convert word offset bytes to decimal. 10.

➤ Which byte in the word does the address specify?

→ If a set had the following V bit and tag, does the address produce a hit or miss?

V tag

1.) 1 0x0750 *MISS*

2.) 0 0x0750 *MISS*

3.) 1 0x00EA *HIT*

4.) 0 0x00EA *MISS*

Direct Mapped Cache

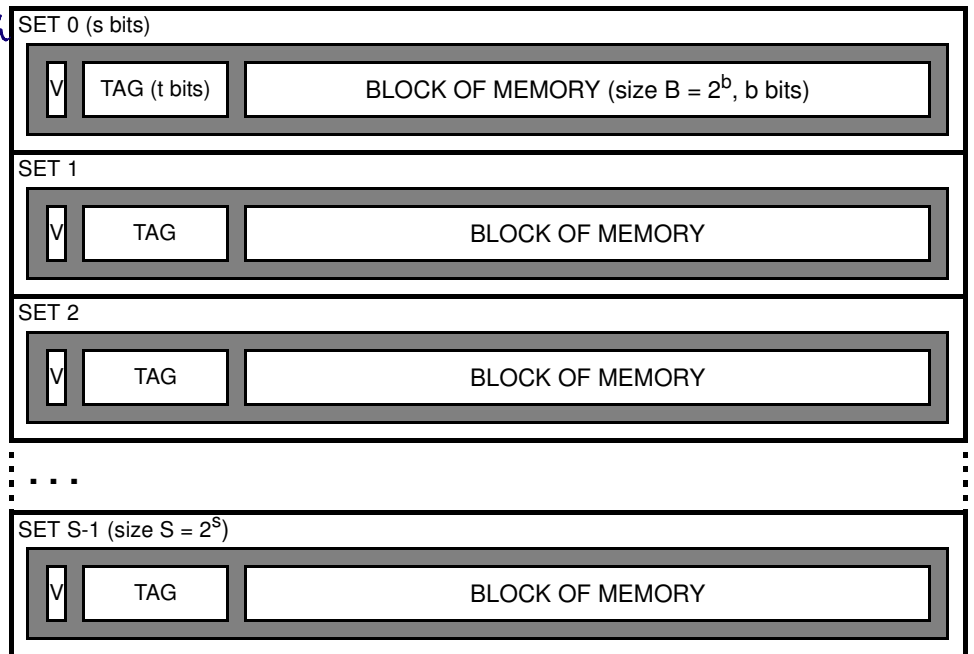
Direct Mapped Cache

is a cache

where each block maps to exactly 1 set. and each set has exactly one line.

+ no need to search

+ simple circuitry to match tag in line with E bits in addr.



→ What happens when two different memory blocks map to the same set?

- conflict misses. and frequent since each set can store only one block.

→ Improvements?

enable each set to have more than one line to resolve conflict

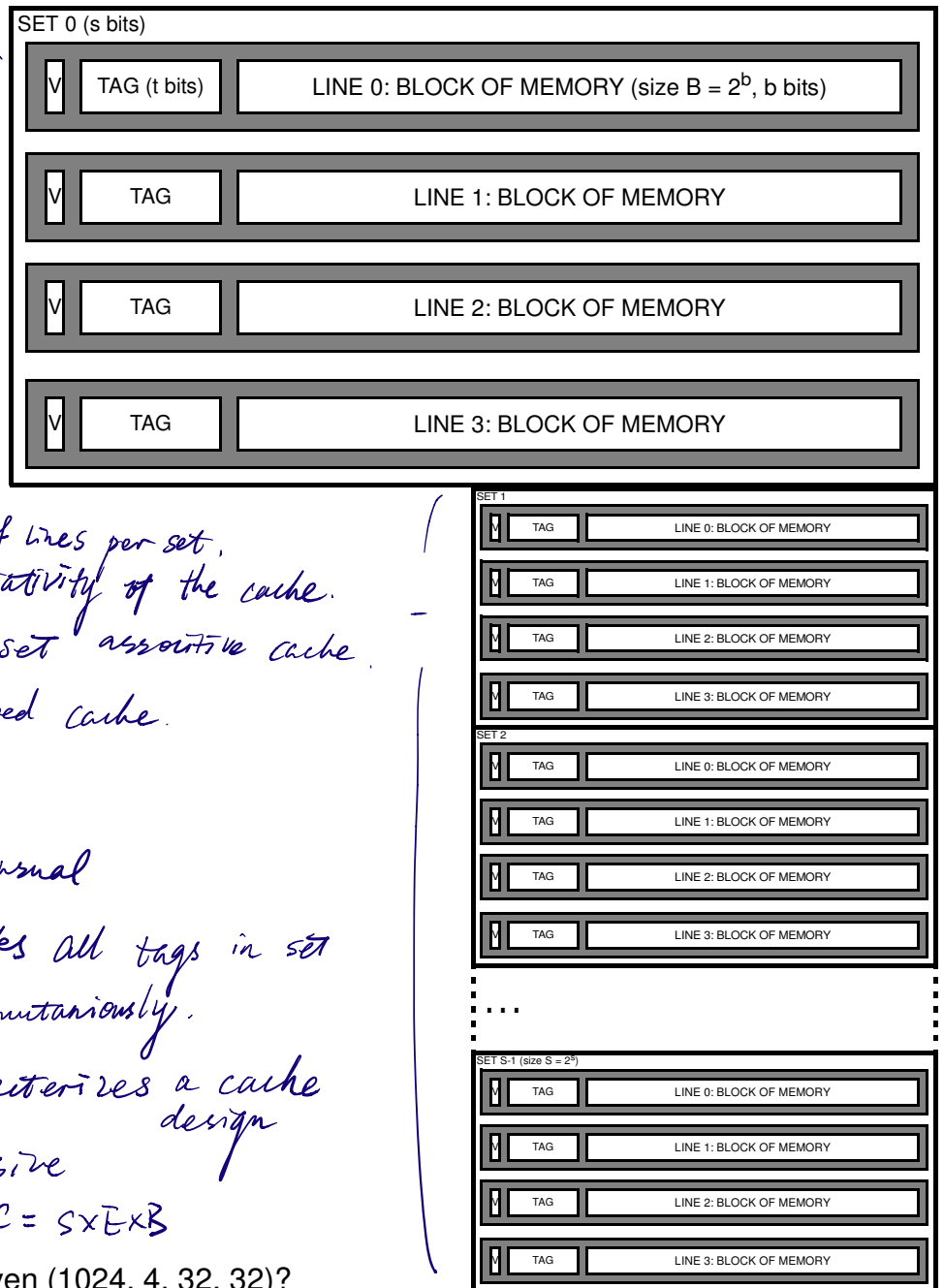
Set Associative Cache

Set Associative Cache

is a cache where each block maps to exactly one set.
and each set has 2 or more lines.

- + Reduces conflict misses.
- Requires complex to match tags with t bits.

set of 4 lines



Let E be the number of lines per set, which is the associativity of the cache.

E = 4 is a four-way set associative cache.

E = 1 is direct mapped cache.

Operation

1. Set Selection As usual
2. Line Matching Checks all tags in set simultaneously.

* $C = (S, E, B, m)$ characterizes a cache design

Let C be the cache size in bytes. $C = S \times E \times B$

→ How big is a cache given (1024, 4, 32, 32)?

$$1024 \times 4 \times 32 = 128 \text{ KB.}$$

1K