

Height 185, 170, 168, 179, 182, 188, 186, 180, 183  
 weight 72, 56, 60, 68, 72, 77, 71, 70, 84, 88

Step 1 - Input dataset, clustering variable  
 & maximum no. of cluster ( $K$  is  
 means clustering)

In This datasets, only two variables,  
 height & weight - are considered for  
 clustering

Step 2: Initialize cluster centroid

In this example, value of  $K$  is  
 considered as 2, cluster centroids  
 are initialised with first 2 observations

| cluster | Initial centroid |        |
|---------|------------------|--------|
|         | height           | weight |
| $K_1$   | 185              | 72     |
| $K_2$   | 170              | 56     |

step - 3

Calculate Euclidean Distance

Euclidean is one of the distance measures used on k-means algorithm. Euclidean distance between an observation & initial cluster centroids 1 & 2 is calculated. Based on Euclidean distance, each observation is assigned to one of the cluster - based on minimum distance.

Euclidean distance =

$$\sqrt{(X_H - x_1)^2 + (X_W - w_1)^2}$$

where

$X_H$  = observation value of variable Height

$x_1$  = centroid value of cluster 1 for var. Height

$X_W$  = observation value of variable weight

$w_1$  = centroid value of cluster 1 for variable weight.

First two observations

| Height | Weight |
|--------|--------|
| 185    | 72     |
| 170    | 56     |

Now initial cluster centroids are

| Cluster | Updated Centroid |        |
|---------|------------------|--------|
|         | Height           | Weight |
| K1      | 185              | 72     |
| K2      | 170              | 56     |



Entire Euclidean Distance calculation from each of the cluster is calculated

| Euclidean distance from cluster <u>1</u>      | Euclidean distance from cluster <u>2</u>      | Assignment |
|---|---|------------|
| $(185-185)^2 + (72-72)^2$<br>$= 0 \checkmark$ | $(185-170)^2 + (72-56)^2$<br>$= 21.93$        | 1          |
| $(170-185)^2 + (56-72)^2$<br>$= 21.93$        | $(170-170)^2 + (56-56)^2$<br>$= 0 \checkmark$ | 2          |

we have considered two observations for assignment only because we knew the assignment & there is no change in centroids as these two observations were only considered as initial centroids

Step 4 : move on to next observation & calculate Euclidean distance

| Height | Weight |
|--------|--------|
| 168    | 60     |

| ED from cluster 1                       | ED from cluster 2                      | Assign |
|---|--|--------|
| $(168-185)^2 + (60-72)^2$<br>$= 20.808$ | $(168-170)^2 + (60-56)^2$<br>$= 4.472$ | 2      |



Since distance is min from cluster 2, so the observation is assigned to cluster 2. Now revise cluster centroid - mean value height & weight as cluster centroids. addition is only to cluster 2, so centroid of cluster 2 will be updated

update cluster centroid

| cluster | Updated Height      | Centroid Weight  |
|---------|---------------------|------------------|
| K=1     | 185                 | 72               |
| K=2     | $(170+168)/2 = 169$ | $(56+60)/2 = 58$ |

Step 5 :- Calculate ED for the next observation assign next observation based on minimum ED & update the cluster centroids

Next observation

| Height | weight |
|--------|--------|
| 179    | 68     |

ED calculation & Assign.

ED from C1      ED from C2      Assignment

$$(185-179)^2 + (68-72)^2 = (169-179)^2 + (58-68)^2$$

$$6^2 + 4^2 = 10^2 + 10^2$$

$$36 + 16 = 100 + 100$$

$$52 = 200$$

✓ (7.2 | 103)

(14.14 | 214)  
X

01



update cluster centroid

cluster updated centroid  
at wt

$$K=1 \quad \underline{182} \quad (185+179)/2 \quad (72+68)/2 \quad 70.66$$

$$K=2 \quad 169 \quad 58$$

continue the steps until all observations are assigned

| final | Height | weight | Assignment |
|-------|--------|--------|------------|
|       | 185    | 72     | 1          |
|       | 170    | 56     | 2          |
|       | 168    | 60     | 2          |
|       | 179    | 68     | 1          |
|       | 182    | 72     | 1          |
|       | 188    | 77     | 1          |
|       | 180    | 71     | 1          |
|       | 180    | 70     | 1          |
|       | 123    | 84     | 1          |
|       | 180    | 88     | 1          |
|       | 180    | 67     | 1          |
|       | 177    | 76     | 1          |

clustered centroid

cluster updated centroid

$$K=1 \quad 182.8 \quad 72$$

$$K=2 \quad 169.0 \quad 58.0$$