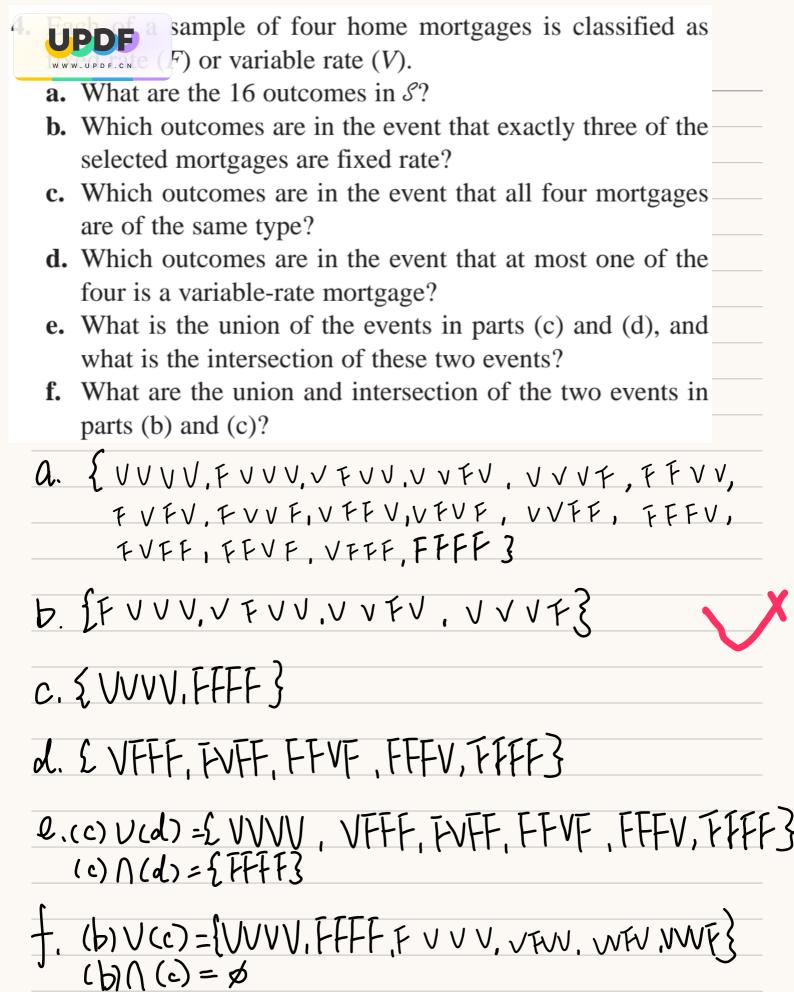




- **2.** Suppose that vehicles taking a particular freeway exit can turn right (R), turn left (L), or go straight (S). Consider observing the direction for each of three successive vehicles.
  - **a.** List all outcomes in the event *A* that all three vehicles go in the same direction.
  - **b.** List all outcomes in the event *B* that all three vehicles take different directions.
  - **c.** List all outcomes in the event *C* that exactly two of the three vehicles turn right.
  - **d.** List all outcomes in the event *D* that exactly two vehicles go in the same direction.
  - **e.** List outcomes in D',  $C \cup D$ , and  $C \cap D$ .
  - a. A= {R,R,R, L,L,L, S,SS3
  - D. B={R,L,S, R,S,L, L,R,S, L,S,R, S,R,L, S,L,R}
- C. C={R.R.L, R.R.S, R,L.R, R,S,R, L,R,R,S,R,R}
- d. D={R.R.L, R.R.S, R.L.R, R.S.R, L.R.R, S.R.R, L.L.R, L.L.S, L.R.L, L.S.L, R.L.L, S.L.L, S.S.R, S.S.L, S.R.S, S.Z.S, R.S.S, L.S.S.
- e. D'={R,R,R, L,L,L, S,S,S, R,L,S, R,S,L, L,R,S, L,S,R, S,R,L, S,L,R}
- CUD = D = {R,R,L, R,R,S, R,L,R, R,S,R, L,R,R, S,R,R, L,L,R, L,L,S, L,R,L, L,S,L, R,L,L,S,L,L, S,S,R, S,S,L, S,R,S, S,L,S, R,SS, L,SS3
- CND=C={R.R.L, R.R.S, R,L.R, R,S.R, L,R,R,S,R,R}

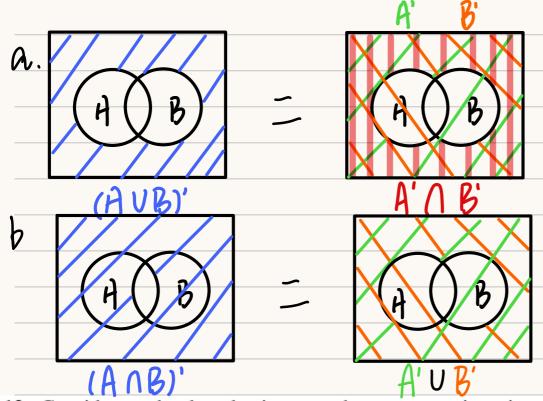


diagrams to verify the following two relationships with A and B (these are called De Morgan's laws):

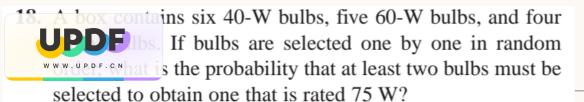
$$\mathbf{a.} \ (A \cup B)' = A' \cap B'$$

**b.** 
$$(A \cap B)' = A' \cup B'$$

[Hint: In each part, draw a diagram corresponding to the left side and another corresponding to the right side.]

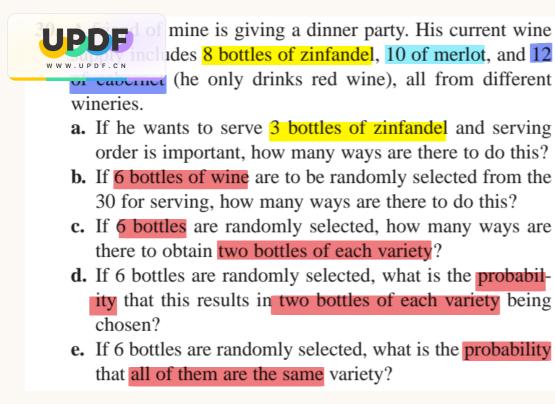


- 12. Consider randomly selecting a student at a certain university, and let A denote the event that the selected individual has a Visa credit card and B be the analogous event for a MasterCard. Suppose that P(A) = .5, P(B) = .4, and  $P(A \cap B) = .25.$ 
  - a. Compute the probability that the selected individual has at least one of the two types of cards (i.e., the probability of the event  $A \cup B$ ).
  - **b.** What is the probability that the selected individual has neither type of card?
  - **c.** Describe, in terms of A and B, the event that the selected student has a Visa card but not a MasterCard, and then calculate the probability of this event.



- Anderson, Box, Cox, Cramer, and Fisher—must select two of its members to serve on a personnel review committee. Because the work will be time-consuming, no one is anxious to serve, so it is decided that the representative will be selected by putting the names on identical pieces of paper and then randomly selecting two.
  - **a.** What is the probability that both Anderson and Box will be selected? [*Hint:* List the equally likely outcomes.]
  - **b.** What is the probability that at least one of the two members whose name begins with *C* is selected?
  - **c.** If the five faculty members have taught for 3, 6, 7, 10, and 14 years, respectively, at the university, what is the probability that the two chosen representatives have a total of at least 15 years' teaching experience there?

c p(at least 15 years' experience) = 
$$\frac{b}{10} = \frac{3}{5} = 0.6$$
  
 $\{3.143, \{6.10\}, \{6.143, \{7.103, \{7.14\}, \{10.14\}\}\}$ 



## a. P3 = 8x7xh =336

e. p (all same variety) = 
$$\frac{C_8 + C_{10} + C_{12}}{C_{20}^6} = \frac{1162}{593775} = 0.00196$$



bulbs, five 60-W bulbs, and six 75-W bulbs. Suppose that three bulbs are randomly selected.

- **a.** What is the probability that exactly two of the selected bulbs are rated 75-W?
- **b.** What is the probability that all three of the selected bulbs have the same rating?
- **c.** What is the probability that one bulb of each type is selected?
- **d.** Suppose now that bulbs are to be selected one by one until a 75-W bulb is found. What is the probability that it is necessary to examine at least six bulbs?

a. 
$$p(two 75-W bulbs) = \frac{C_6^2 \times C_4^2}{C_{15}^2} = \frac{135}{455} = \frac{21}{91} = 0.297$$

b. 7 (all same rating) = 
$$\frac{C_4^3 + C_5^3 + C_6^3}{C_{15}^3} = \frac{34}{455} = 0.0747$$

c. 
$$p$$
 (all otifierent vating) =  $\frac{C_4 \times C_5 \times C_6}{C_{35}^3} = \frac{120}{455} = \frac{24}{91} = 0.264$ 

