

Ex. 14.
Homework 14

Section 7.1

Ex 22. $\frac{32}{100}$

Ex 24. a) $\frac{1}{C_{30}^6}$

b) $\frac{1}{C_{36}^6}$

Section 7.2

Ex. 2 As for number "1, 2, 4, 5, 6", the probability is $\frac{1}{7}$
As for number "3", the probability is $\frac{2}{7}$

Ex. 16. We just need to ~~identify~~ identify that $P(\bar{E}\bar{F}) = P(\bar{E}) \cdot P(\bar{F})$

$$\begin{aligned} \text{It's clear that: } P(\bar{E}\bar{F}) &= P(\overline{E \cup F}) \\ &= 1 - P(E \cup F) \\ &= 1 - (P(E) + P(F) - P(E \cap F)) \\ &= 1 - P(E) - P(F) + P(E \cap F) \\ &= 1 - P(E) - P(F) + P(E) \cdot P(F) \\ &= (1 - P(E)) \cdot (1 - P(F)) \\ &= P(\bar{E}) \cdot P(\bar{F}) \end{aligned}$$

Then we prove it completely

* Section 7.3 $P(E|F) = \frac{P(E \cap F)}{P(F)}$

Ex. 2

$$\begin{aligned} P(E|F) &= \frac{P(F|E) \cdot P(E)}{P(F|E) \cdot P(E) + P(F|\bar{E}) \cdot P(\bar{E})} \\ &= \frac{\frac{5}{8} \cdot \frac{2}{3}}{\frac{5}{8} \cdot \frac{2}{3} + \frac{3}{8} \cdot \frac{1}{3}} \\ &= \frac{\frac{10}{12}}{\frac{10}{12} + \frac{1}{8}} \\ &= \frac{10}{12} \end{aligned}$$

$$\begin{aligned} &= \frac{P(F)}{P(F)} \\ &= \frac{\frac{5}{8} \cdot \frac{2}{3}}{\frac{5}{8} \cdot \frac{2}{3}} \\ &= \frac{5}{9} \end{aligned}$$

Ex 6. Suppose \bar{E} be the event that the person tests positive that eat steroid

"D" be the event that player takes steroid

$$P(D|E) = \frac{P(E|D)P(D)}{P(E|D)P(D) + P(E|\bar{D})P(\bar{D})} = \frac{(0.98)(0.05)}{(0.98)(0.05) + (0.12)(0.95)}$$

We know: $P(D) = 0.05$, $P(\bar{D}) = 0.95$

$P(E) = 0.98$ $P(E|D) = 0.98$

$P(E|\bar{D}) = 0.12$

