

$$P(A \cap B' | A') = \frac{(1-0.4) \cdot (1-0.7)}{1-0.4} = \frac{0.6 \cdot 0.3}{0.6} = 0.3$$

$$P(A \cup B) = 0.4 + 0.7 - 0.4 \times 0.7 = 0.82$$

$$c. P(A \cap B' | A \cup B) = \frac{A \cap B'}{A \cup B} = \frac{0.12}{0.82} = 0.146$$

72. A_2 and A_3 are independent.

$$P(A_2) \times P(A_3) = 0.25 \times 0.28 = 0.07$$

$$P(A_2 \cap A_3) = 0.07$$

$$\begin{aligned} 80. P(\text{system works}) &= (P(1 \cup 2) \cup (P(3 \cap 4))) \\ &= (P(1) + P(2) - P(1 \cap 2)) \cup (P(3 \cap 4)) \\ &= 0.99 + 0.81 - 0.99 \times 0.81 \\ &= 0.9981 \end{aligned}$$

$$84. a. 0.7 \times 0.7 \times 0.7 = 0.343$$

$$b. 1 - 0.343 = 0.657$$

$$c. 3 \times 0.7 \times 0.3 \times 0.3 = 0.189$$

$$d. 0.3 \times 0.3 \times 0.3 = 0.027$$

$$0.027 + 0.189 = 0.216$$

$$e. P(\text{all three pass} | \text{at least one pass})$$

$$= \frac{0.343}{1 - 0.027}$$

$$= \frac{0.343}{0.973}$$

$$= 0.353$$

3.1. 4. Possible values of x : 1, 2, 3, 4, 5

Three zip code examples : 22313, 10002, 20241

$$x(22313) = 5 \quad x(10002) = 2 \quad x(20241) = 4$$

5. No. Let S be set of natural number N , define random variable X as

$X = 0$ if the chosen number from N include 1 or 3 or 5;

$X = 1$ otherwise.

X has only two values, however the sample space is infinite.

$$8. Y = 3 : SSS$$

$$Y = 4 : FSSS$$

$$Y = 5 : FFSSS, SFSSS$$

$$Y = 6 : FFFSSS, SSFSSS, SFFSSS, FSSFSS$$

$$Y = 7 : FFFFSSS, SFFFSSS, FSFFSSS, FFSFSSS, SSFFSSS, FSSFSSS, SFSFSSS$$

$$10. a. 4 + 6 = 10$$

$$T = 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10$$

$$b. X = -4, -3, -2, -1, 0, 1, 2, 3, 4, 5, 6$$

$$c. U = 0, 1, 2, 3, 4, 5, 6$$

$$d. Z = 0, 1, 2$$



3.2. 12. a. $0.05 + 0.1 + 0.12 + 0.14 + 0.25 + 0.17 = 0.83$

b. $1 - 0.83 = 0.17$

c. $P(Y \leq 49) = 0.05 + 0.1 + 0.12 + 0.14 + 0.25$
 $= 0.66$

$P(Y \leq 47) = 0.05 + 0.1 + 0.12$
 $= 0.27$

23 a. $P(X=2) = P(2 \leq X < 3) - P(1 \leq X < 2)$
 $= 0.39 - 0.19$
 $= 0.2$

b. $P(X > 3) = 1 - 0.67 = 0.33$

c. $P(2 \leq X \leq 5) = 0.97 - 0.19 = 0.78$

d. $P(2 < X < 5) = P(3 \leq X \leq 4) = 0.92 - 0.39 = 0.53$

25. $P(Y=0) = P(B) = p$

$P(Y=1) = P(G|B) = (1-p)p$

$P(Y=2) = P(GG|B) = (1-p)^2 p$

$P(Y=y) = \begin{cases} (1-p)^y p & y = 0, 1, 2, 3, \dots \\ 0 & \text{otherwise} \end{cases}$

