

$$A = \{RRR, LLL, SSS\};$$

$$B = \{RLS, RSL, LRS, LSR, SRL, SLR\}$$

$$C = \{RRL, RRS, LRR, SRR, RSR, RLR\}$$

$$D = \{RRL, RRS, LRR, SRR, RSR, RLR, LLR, LLS, ALL, SLL, LSL, LRL, SSL, SSR, SRL, SLS, LSS, RSS\}$$

$$D' = \{RRR, LLL, SSS, RLS, RSL, LRS, LSR, SRL, SLR\}$$

$$C \cup D = D$$

$$C \cap D = C$$

$$4. a. S = \{FFFF, FFFV, FFVF, FFVV, FVFF, FVVF, FVVV, FVVF, VFFF, VFFV, VFVF, VFVV, VVFF, VVVV\}$$

$$b. \text{FFFF, FFFV, FFVF, FVFF, VFFF}$$

$$c. \text{FFFF, VVVV}$$

$$d. \text{FFFF, FFFV, FFVF, FVFF, VFFF}$$

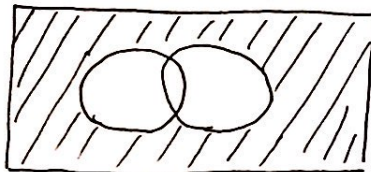
$$e. \text{union: FFFF, VVVV, FFFV, FFVF, FVFF, VFFF}$$

$$\text{intersection: FFFF}$$

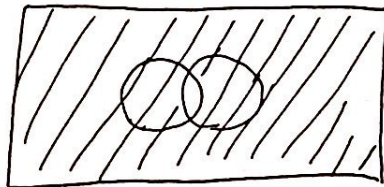
$$f. \text{union: FFFF, VVVV, FFFV, FFVF, VFFF, FVFF}$$

$$\text{intersection: empty set.}$$

9. a.



b.



$$2.2.12. a. P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$= 0.5 + 0.4 - 0.25$$

$$= 0.65$$

$$b. P(A' \cap B') = P[(A \cup B)'] = 1 - P(A \cup B)$$

$$= 1 - 0.65$$

$$= 0.35$$

$$c. P(A \cap B') = P(A) - P(A \cap B)$$

$$= 0.5 - 0.25$$

$$= 0.25$$



$$+ \left(\frac{11}{15} \times \frac{4}{14} \right)$$

$$= \frac{44}{210} + \frac{44}{210}$$

$$= \frac{44}{105}$$

27. a. $P(\{A, B\}) = 10$

b. $P(\{ \text{start with at least one C} \}) = P(\{A, C_{ox}\} + \{A, C_r\} + \{B, C_{ox}\} + \{B, C_r\} + \{C_{ox}, C_r\} + \{C_{ox}, F\} + \{C_r, F\})$
 $= \frac{7}{10}$

c. $P(\{ \text{at least 15 years experience} \}) = P(\{3, 14\} + \{6, 10\} + \{6, 14\} + \{7, 10\} + \{7, 14\} - \{10, 14\})$
 $= \frac{6}{10}$

2.3. 30. a. $P_{3,8} = \frac{8!}{(8-3)!} = 8 \cdot 7 \cdot 6 = 336$

b. $C_{6,30} = \binom{30}{6} = \frac{30!}{6!(30-6)!} = \frac{30!}{6!24!} = 593775$

c. $C_{2,8} = \frac{8!}{2!(8-2)!} = 28$

$C_{2,10} = \frac{10!}{2!(10-2)!} = 45$

$C_{2,12} = \frac{12!}{2!(12-2)!} = 66$

$28 \cdot 45 \cdot 66 = 83160$

d. $\frac{83160}{593775} = 0.14$

e. $P(\{ \text{All vines bottles are same} \}) = P(\{ \text{all are zindandel} \}) + P(\{ \text{all are merlot} \}) + P(\{ \text{all are cabernet} \})$
 $= \binom{8}{6} + \binom{10}{6} + \binom{12}{6}$
 $= 28 + 210 + 924$
 $= 1162$

$\frac{1162}{593775} = 0.002$



38. a. Total number of ways to select three bulbs = $C(15, 3) = 455$

Number of ways to select two 75-w bulbs = $C(6, 2) \times C(9, 1) = 135$

$$\frac{135}{455} = 0.297$$

b. Number of ways to select three bulbs of the same rating :

$$C(4, 3) + C(5, 3) + C(6, 3) = 4 + 10 + 20 = 34$$

$$\frac{34}{455} = 0.0747$$

$$c. C(4, 1) \times C(5, 1) \times C(6, 1) = 4 \times 5 \times 6 = 120$$

$$\frac{120}{455} = 0.264$$

$$d. 1 - \frac{6}{15} - \frac{9}{15} \times \frac{6}{14} - \frac{9 \cdot 8}{15 \cdot 14} \times \frac{6}{13} - \frac{9 \cdot 8 \cdot 7}{15 \cdot 14 \cdot 13} \times \frac{6}{12} - \frac{9 \cdot 8 \cdot 7 \cdot 6}{15 \cdot 14 \cdot 13 \cdot 12} \times \frac{6}{11}$$

$$= 1 - 0.958$$

$$= 0.042$$

40. a. The total number of possible chain molecules is $12! = 479001600$.

$$\frac{12!}{3!3!3!3!} = 369600$$

$$b. P(4, 4) = 4! = 24$$

$$\frac{24}{369600} = 0.00006494$$

