

Section 2.1

2. Suppose that vehicles taking a particular freeway exit can turn right (R), turn left (L), or go straight (S). Consider

observing the direction for each of three successive vehicles.

- a. List all outcomes in the event A that all three vehicles go in the same direction.
- b. List all outcomes in the event B that all three vehicles take different directions.
- **c.** List all outcomes in the event C that exactly two of the three vehicles turn right.
- d. List all outcomes in the event D that exactly two vehicles go in the same direction.
- e. List outcomes in D', $C \cup D$, and $C \cap D$.



- b) eventB: all three vehicles take different directions
 - B= {RLS, RSL, LSR, LRS, SLR, SRL}
- c) event C: exactly two of three vehicles turn right.

 C= {RRL, RRS, RLR, RSR, LRR, SRRJ /
- d) event 17: exactly two vehicles go in the same direction

LLS. LLR. LSL, LRL. SLL. RLL.

SSL, SSR, SLS, SRS, RSS, LSSJ

e) event D': the three cars go to the same ways or they all go to different directions.

D': {RLS, RSL, LSR, LRS, SLR, SRL, LLL. RRR. SSS}

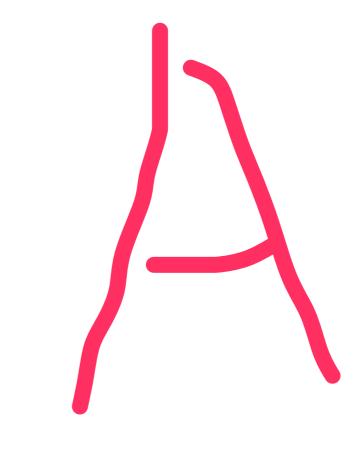
CUD = {RRL, RRS, RLR, RSR. LRR, SRR,

CND= C=

LLS. LLR. LSL, LRL. SLL. RLL.

ERRL. RRS. RLR. RSR. LRR. SRRJ

SSL, SSR, SLS, SRS, RSS, LSS 3 = D



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ir home mortgages is classified as rate (V).

b. Which outcomes are in the event that exactly three of the

selected mortgages are fixed rate?

c. Which outcomes are in the event that all four mortgages are of the same type?

d. Which outcomes are in the event that at most one of the four is a variable-rate mortgage?

e. What is the union of the events in parts (c) and (d), and what is the intersection of these two events?

f. What are the union and intersection of the two events in parts (b) and (c)?

b) event B: exactly three of the saleoted mortgages are fixed rate.

B= IFFFV, FFVF, FVFF, VFFF3

c) event C: all four mortgages are of the same type. C= [FFFF, VVVV]

d). event D: at most one of the four

is a variable—rate movegage

D= IFFFF, VFFF, FFFV, FFVF, FVFFF

as since each has two possibilities. (For V) four mortgages.

So there are 2 = 16 possible outcome.

outcome	He	ome mor	tgage	4	
outcome 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16	FYFFYY	アストーンドラントランドンン	FFFYFY	4 ドドドトトトトトントトトン	

e) event E: the union of C and D. that the mortgage can have all mortgage are variable or that at most one of them is variable rate:

that E= [FFFF, VFFF, FFFV, FFVF, FVFF, VVVV]

the intersection of C and D is the event that all the mortgages are fixed-rate

CND= EFFFF

f) the union of event B and C: all four mortgages are of the same type or exactly three are fixed

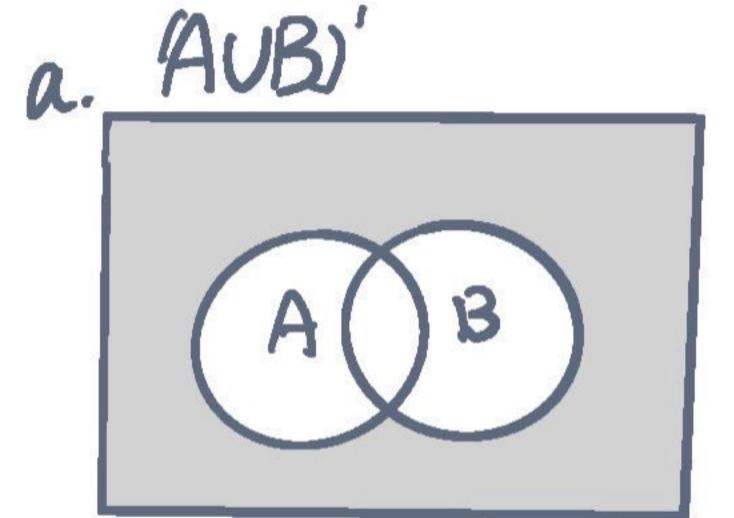
BUCE [FFFV. FFVF. FVFF. VFFF (FFFF, VVVV)

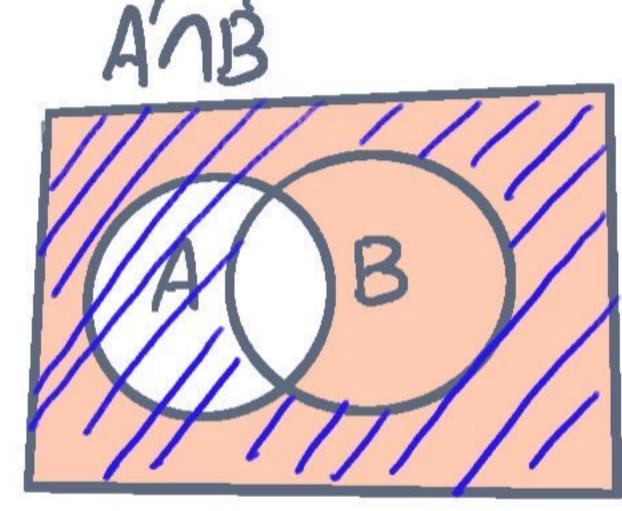
Bnc = & since they have no common outcome

verify the following two relationships 3 (these are called De Morgan's laws):

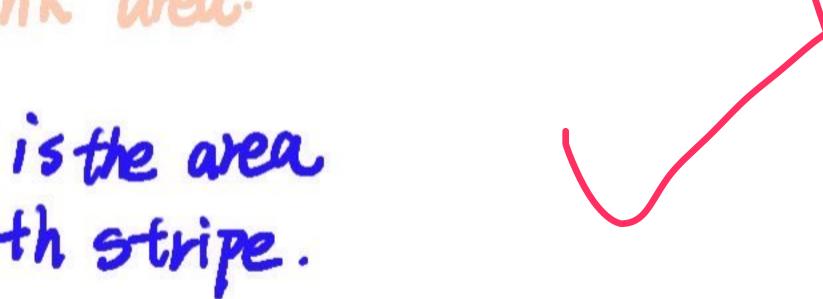
b.
$$(A \cap B)' = A' \cup B'$$

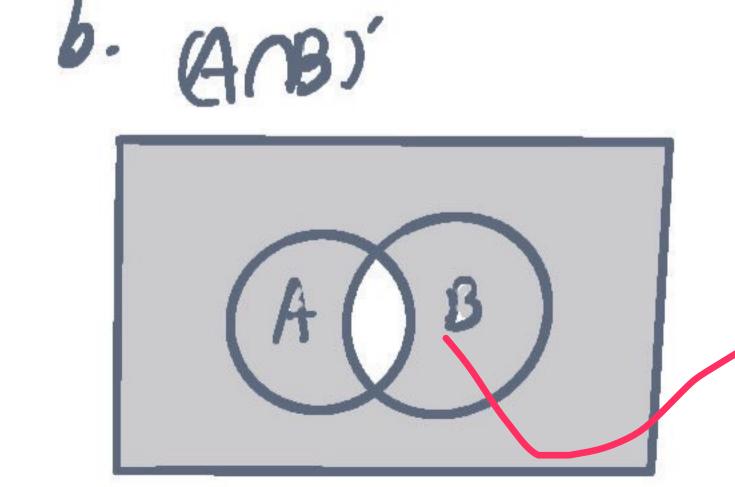
[Hint: In each part, draw a diagram corresponding to the left side and another corresponding to the right side.]

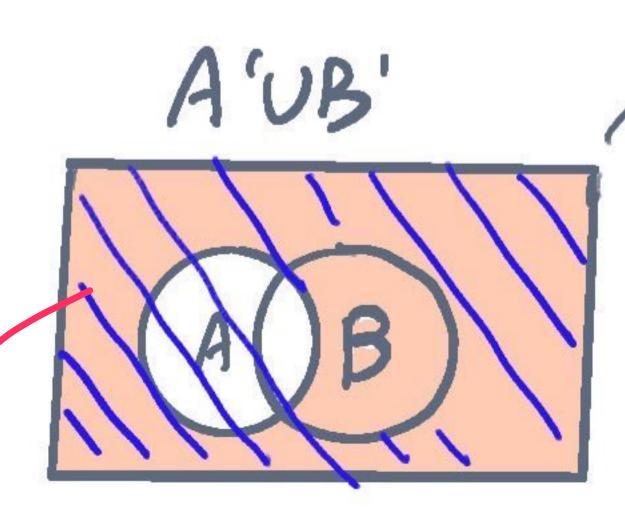




A' is the



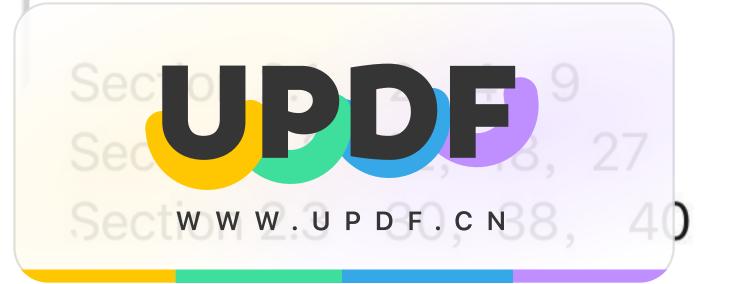




In have either pink or stripes or both.

A' is the

Pink area. Two diagram display
B'is the area the same own. with stripe.



Section2.2.

12. Consider randomly selecting a student at a certain university, and let A denote the event that the selected individual has a Visa credit card and B be the analogous event for a MasterCard. Suppose that P(A) = .5, P(B) = .4, and $P(A \cap B) = .25$.

events: selected individual has a Visa credit card.

events: selected individual has a Master Card.

- **a.** Compute the probability that the selected individual has at least one of the two types of cards (i.e., the probability of the event $A \cup B$).
- **b.** What is the probability that the selected individual has neither type of card?

c. Describe, in terms of A and B, the event that the selected student has a Visa card but not a MasterCard, and then calculate the probability of this event.

calculate the probability of this event.

a) event C: Selected individual has at least one of the two types of courds

P(AVB) = P(A) + P(B) - P(ANB)

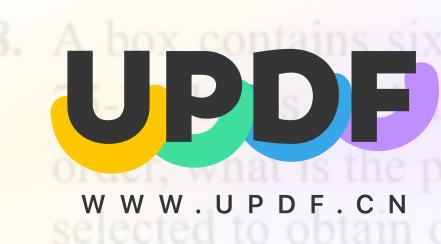
= 0.5 + 0.4 - 0.25

b) even-ti7: selected individual has neither type of card.

 $P(D) = P(A' \cap B') = P(A \cup B) = 1 - P(A \cup B)$ = 1-0.45=0.35

c) eventE: selected student has a Visa courd but not a MasterCard.

P(E) = P(ANB') = P(A)-PGANB)=0.5005

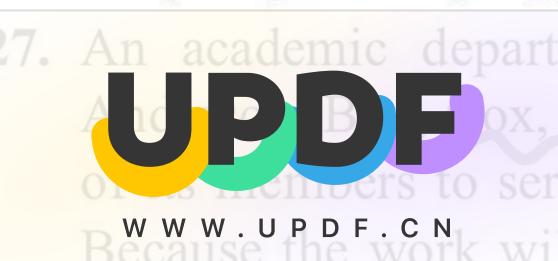


bulbs, five 60-W bulbs, and four e selected one by one in random lity that at least two bulbs must be at is rated 75 W?

event A: At least two bulbs mustbe selected to obtain one that is rated 75W. there are a lot of case if the 75W bulbs can't be selected in the first time.

Event B: 75-W bulb is selected in the first time.





nt with five faculty members amer, and Fisher—must select two on a personnel review committee. be time-consuming, no one is anx-

ious to serve, so it is decided that the representative will be selected by putting the names on identical pieces of paper and then randomly selecting two.

- a. What is the probability that both Anderson and Box will be selected? [*Hint*: List the equally likely outcomes.]
- **b.** What is the probability that at least one of the two members whose name begins with C is selected?
- c. If the five faculty members have taught for 3, 6, 7, 10, and 14 years, respectively, at the university, what is the probability that the two chosen representatives have a total of at least 15 years' teaching experience there?

C) event C: the two chosen representative have a total of at least 15 years' teaching experience.

PC)=P(I4,33 [14.13 [14.13] 到明到一格马

a). eventA: both Anderson and Bow will be selected.

since there are $C_{5,2} = 10$ cases. $P(A) = \int_{0}^{2\pi} is \text{ one situation.}$ b) evently: at least one of the two members whose name begins with C is selected.

P(B) = P({A,Co} {A,Co} {B,Co} {B,Cd} IF.C.3 [F.C.]. [Co Red



Section 2.3

- **30.** A friend of mine is giving a dinner party. His current wine supply includes 8 bottles of zinfandel, 10 of merlot, and 12 of cabernet (he only drinks red wine), all from different wineries.
 - **a.** If he wants to serve 3 bottles of zinfandel and serving order is important, how many ways are there to do this?
 - **b.** If 6 bottles of wine are to be randomly selected from the 30 for serving, how many ways are there to do this?
 - **c.** If 6 bottles are randomly selected, how many ways are there to obtain two bottles of each variety?
 - **d.** If 6 bottles are randomly selected, what is the probability that this results in two bottles of each variety being chosen?
 - **e.** If 6 bottles are randomly selected, what is the probability that all of them are the same variety?

b) order is not important.

c) two bottles of each variety.

d) total wine: 8+10+12=30

total case C30,6=593775

that event 17: two bottles of each variety being chosen:

= 0.14

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www.updf.cn pply room contains four 40-W lightbulos, five oo w bulos, and six 75-W bulbs. Suppose that three bulbs are randomly selected.

- **a.** What is the probability that exactly two of the selected bulbs are rated 75-W?
- **b.** What is the probability that all three of the selected bulbs have the same rating?
- **c.** What is the probability that one bulb of each type is selected?
- **d.** Suppose now that bulbs are to be selected one by one until a 75-W bulb is found. What is the probability that it is necessary to examine at least six bulbs?

c) event C: one bulb of each

type is selected

T(C) - C6 - C4 - C5

PCC)= $\frac{C_6 - C_4 - C_5}{C_{15}^{35}} = \frac{120}{2455} = 0.2637$ evento: examine at least six bulbs to selected a 75-w bulb. that happen when the first five bulbs were all of the Low or bow bulbs. (there are totally 9 such bulbs)

$$P(D) = \frac{C_{9.5}}{C_{15.6}} = \frac{126}{3003} = 0.042$$

a) eventA: two of the selected bulbs are rated 75-W. $P(A) = \frac{C_{b12} \cdot C_{9.1}}{C_{15.25}} = \frac{15 \times 9}{455}$ ≈ 0.2967

b) event B: all afthe selected bulbs have the same parting



and three of type *D* are to be linked together to form a chain molecule. One such chain molecule is *ABCDABCDABCD*, and another is *BCDDAAABDBCC*.

a. How many such chain molecules are there? [Hint: If the three A's were distinguishable from one another— A_1 , A_2 , A_3 —and the B's, C's, and D's were also, how many

molecules would there be? How is this number reduced when the subscripts are removed from the A's?]

b. Suppose a chain molecule of the type described is randomly selected. What is the probability that all three molecules of each type end up next to one another (such as in *BBBAAADDDCCC*)?

a) since in different type they are distinguishable.

there are $P_{12}^{12}=12!$ possible chain molecules.

But when A is the same, the sating inside A invain, then when the B.C.D order does not change, there will be 3! way to become one, B.C.D use the same method. (That is, they no longer have any order within themselves then it will have $\frac{12!}{(3!)^4} = 369600$ chain molecules.

b) if we want that all three molecules of each type end up next to one another.

we can consider each type as a whole

then it would have 4! = 24 ways.

the probability that all three molecules of each type end up next to one another.

$$\frac{15}{369600} \approx 0.00006494$$

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