

Section 5.3

Ex 38

a. T_0	0	1	2	3	4
$P(T_0)$	0.04	0.2	0.37	0.2	0.09

β^+

b. $M_{T_0} = \mu \cdot n = 2.2$

c. $V(T_0) = n V(x)^2 = 2 \times 0.49 = 0.98$

d. now $n=4$,

$E(T_0) = n \mu = 4.4$;

$V(T_0) = n \sigma^2 = 1.96$

e. X is ~~satisfied~~ satisfy normal distribution.

~~$\mu = \frac{E(T_0)}{n}$~~

$p(T_0=8) = p(z = \frac{8-4.4}{1.4}) = p(z=2.57) = 0.9949$

$p(T_0 \geq 7) = p(z \geq \frac{7-4.4}{1.4}) = p(z \geq 1.85) = 1 - \Phi(1.85) = 1 - 0.9678 = 0.0322$

Ex 41

a. X_i	2	3	4	5	6	7	8
$P(X_i)$	0.16	0.24	0.25	0.2	0.1	0.04	0.01
\bar{x}	1.5	2	2.5	3	3.5	4	

b. $M_x = \sum_{i=1}^8 \bar{x} p(\bar{x}) = 2$

$\sigma_x^2 = \sum_{i=1}^8 (\bar{x}^2 p(\bar{x}) - M^2) = 1.78$

$p(\bar{x} \leq 2.5) = p(z \leq \frac{2.5-2}{0.707}) = 0.707$

c. R	0	1	2	3
$P(R)$	0.3	0.4	0.22	0.08

d. ~~Assume that $T_0 = X_1, X_2, X_3, X_4$, $E(T_0) = n \mu$~~

$p(\bar{x} \leq 1.5) = p(1,1,1,1) + p(2,1,1,1) + p(2,2,1,1) + p(3,1,1,1) = (0.4)^4 + 4(0.4)^3(0.3) + 6(0.4)^2(0.2)^2 + 4(0.4)(0.2)^3 = 0.24$

Section 5.4

Ex 46. a. \bar{x} is satisfied normal distribution.

$\sigma_{\bar{x}} = \frac{\sigma_x}{\sqrt{n}} = \frac{0.04}{4} = 0.01$

b. \bar{x} is satisfied normal distribution

$\sigma_{\bar{x}} = \frac{0.04}{8} = 0.005$

c. The second sample. Because with the larger sample, comes with the lower variability

We know $\mu=10$, $\sigma=2$, so $\bar{X} \sim N(10, 4)$, $\sigma_z = \frac{\sigma}{\sqrt{n}} = \frac{2}{\sqrt{5}}$ or $\frac{2}{\sqrt{5}}$

for day one: $p(\bar{X}_1 \leq 11) = p(z \leq \frac{11-10}{2/\sqrt{5}}) = 0.86$

for day two $p(\bar{X}_2 \leq 11) = p(z \leq \frac{11-10}{2/\sqrt{5}}) = 0.88$

for average $p(\bar{X} \leq 11) = 0.86 \times 0.88 = 0.7728$

Ex 55

a. for poisson distribution, $\mu = \sigma = 50$

$$p(35 \leq \bar{X} \leq 50) = p\left(\frac{35-50}{\sqrt{50}} \leq z \leq \frac{50-50}{\sqrt{50}}\right) = p(-2.24 \leq z \leq 0) = 0.5160 - 0.4880 = 0.028$$

$\sigma = \sqrt{50}$

b. the daily mean is 50, so the five day mean is $\mu = 250$, so $\sigma = \sqrt{250}$

$$p(225 \leq \bar{X} \leq 275) = p\left(\frac{225-250}{\sqrt{250}} \leq z \leq \frac{275-250}{\sqrt{250}}\right) = p(-0.5 \leq z \leq 0.5) = 0.719 - 0.469 = 0.25$$

Section 5.5

Ex 58

$$1) E(X) = 27 \times 200 + 125 \times 250 + 512 \times 100 = 87850$$

$$V(X) = 27^2 \times 10^2 + 125^2 \times 10^2 + 512^2 \times 10^2 = 1910016$$

2) the expected value is correct

the ~~variance~~ variance is incorrect, because the ~~covariance~~ covariance also contribute the variance

Ex 70

$$1) E(Y_i) = 0.5, E(W) = \sum_{i=1}^n 0.5(1+i) = 0.5 \times \frac{n(n+1)}{2} = \frac{n(n+1)}{4}$$

$$2) V(Y_i) = E(Y_i^2) - E(Y_i)^2 = 0.25, V(W) = V(Y) \cdot \sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{24}$$

Ex 73

a. given that the sample value is relatively large, so \bar{x} and \bar{y} is normally distributed.

b. \bar{x} and \bar{y} is just special linear combination, so it is also normally distribution

$$c. \mu_{\bar{x}-\bar{y}} = 5, \sigma_{\bar{x}-\bar{y}}^2 = \frac{8^2}{40} + \frac{6^2}{35} = 2.629, \sigma = 1.621, p(-1 \leq \bar{x}-\bar{y} \leq 1) = p(-3.7 \leq z \leq -2.4) = 0.0068$$

d. $p(\bar{x}-\bar{y} \geq 10) = p(z \geq \frac{10-5}{1.621}) = p(z \geq 3.08) = 0.001$, this is too small, so it's doubtful