Chapter 6

Section 6.1.

Ex.1

(a) Use mean value:  $\bar{X} = \frac{\Sigma Xi}{n} = \frac{219.8}{27} = 8.14$ 

(b) Use median value:  $\hat{\chi} = 7.7$ (c) Use:  $\hat{\chi} = \frac{5(x_1 - x_2)^2}{n-1} = \frac{5(x_1 - 2x_1 + x_2)^2}{n-1} = \frac{1860.94 - 2 \times 8.14 \times 219.8 + 27 \times 8.14}{1.27 - 1.275}$ 

(d) Use: 4 = 0.148 1.66 (e) Use:  $\sqrt{\frac{4}{x}} = \frac{0.148}{8.14} = 0.204$  = 1.75 = 1.66

EX-(B)

(a)  $1 - \frac{12}{8} = 0.85$ 

(b) It is clear that: P= 0.85 so: the answer is: P2: 0.852: 0.7225

E[X:19](a)  $E[X] = K = \mu_{\overline{X}} = \mu = E[X] = \frac{0 \times 18 + 1 \times 31 + 2 \times 42 + \cdots + 1 \times 1}{150} = 2.11$ (b) As for position distribution  $G_{\overline{X}} = \frac{\sqrt{2.11}}{\sqrt{n}} = 2.119$ (b):  $G_{\overline{X}}^2 = \mu$  so:  $G_{\overline{X}} = \frac{\sqrt{n}}{\sqrt{n}} = \frac{\sqrt{150}}{\sqrt{150}} = 2.119$ 

First calculate  $\mu = E(x) = E(\overline{x}) = \int_{-1}^{1} x f(x) dx = \int_{-1}^{1} x \cdot (0.5(1+ex)) dx$ 

so: 6=3x, E(8)= E(3x)=3E(x)=3x3

= 0 = unhiased estimator

KOKUYO



Section 6.2

B EX: 20

(a.) The example satisfy binomial distribution: so: f(P)= p3(1-P)<sup>7</sup>

Then: (nfip)=3lnp+17ln(1-P)

 $(nf(p)) = \frac{3}{p} - \frac{17}{1-p}$  $(et: \frac{3}{p} - \frac{17}{1-p} = 0) \quad then: p = \frac{3}{20} = \frac{x}{h}$ 

(b) E(p)= E(n) = n Ew)= n. np=p So: p is unbiased

(c) (1-\$15= (0.85) = 0.444

Ex. (21)

(a) We use moment method can derive the ann answer.

(b) E(x) = B. T (1+1/d)

E(X) = V(x)+E(x)2 = B2([(1+/4)-[(1+1/4)])+ B. [(1+1/4)]

Then:  $\frac{\chi^2}{\tilde{\eta} \cdot \tilde{\Sigma}(\chi_i^2)} = \frac{28^2}{825} = 0.95 = \frac{\Gamma(1-2)^2}{\Gamma(1-2)(1-2)} = \frac{\Gamma(1-2)(1-2)}{\Gamma(1-2)(1-2)} \Rightarrow \alpha = 0.5$ 

then: B = 1(1.2)



Ex. 29.

(a) According to the problem: 
$$\hat{\theta} = min(X_i)$$
  

$$f(X_i X_2 ... X_n) = \lambda e^{-\lambda(X_1 - \theta)} \cdot \lambda e^{-\lambda(X_2 - \theta)} \cdot ... \quad \lambda e^{-\lambda(X_n - \theta)}$$

$$= \lambda^n e^{-\lambda(\sum X_i - n\theta)}$$

differentiate 
$$f(X_i X_i \cdots X_n)$$
 w.r.t  $\lambda$ :  $ln f(X_i X_i - X_n) = n ln \lambda - \lambda (\sum X_i - n \theta)$   
 $(ln f(X_i X_i \cdots X_n)) = \frac{1}{\lambda} - \sum X_i + n \theta = 0$   
 $so: \lambda = \frac{n}{\sum X_i - n \theta} = \frac{n}{\sum X_i - n \cdot min(X_i)}$ 

(2) 
$$\hat{\theta} = 0.64$$
  
 $\hat{S} = \frac{10}{\sum_{x_1 = 10 \times 0.64}} = 0.202$ 

Ex.32.

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(a) 
$$P(Y \le y) = P(X_1 \le y, X_2 \le y, ..., X_n \le y)$$

$$= \frac{1}{4} \cdot \frac{1}{4} \cdot ... \frac{1}{4}$$

$$= (\frac{1}{4})^n$$
So:  $f(Y) = \frac{1}{4} \cdot \frac{1}{4} \cdot \frac{1}{4} \cdot \frac{1}{4} = \frac{ny^{n-1}}{6^n}$ 

(b) 
$$E(\hat{\theta}) = \int_{0}^{\theta} \Re \left\{ \gamma(\theta) dy = \frac{n}{n+1} \max(X_i) \mid (\hat{\theta} = \max(X_i)) \right\}$$
  

$$So: E\left(\frac{n+1}{n}\hat{\theta}\right) = \mp \frac{n+1}{n} E\left(\hat{\theta}\right) = \theta \text{ is unbiased.}$$

