

$$4b. P(A|B) = \frac{P(A \cap B)}{P(B)}$$

$$P(B|A) = \frac{P(A \cap B)}{P(A)}$$

$$P(A) > P(B)$$

$$P(A|B) \neq P(B|A)$$

$$5a. a. p = 0.05$$

$$b. p = 0.07 + 0.05 = 0.12$$

$$c. \text{short-sleeved} : 0.56$$

$$\text{long-sleeved} : 0.44$$

$$d. P(me) = 0.49$$

$$P(pr) = 0.25$$

$$e. P(M|S) = \frac{P(M \cap S)}{P(S)}$$

$$= 0.53$$

$$f. P(S|mp) = \frac{P(S \cap mp)}{P(mp)}$$

$$= \frac{0.08}{0.08 + 0.10} = 0.44$$

$$f. P(S|M_p) = \frac{P(S \cap M_p)}{P(M_p)}$$

$$= \frac{0.08}{0.08 + 0.10} = 0.44$$

$$18. P(A \cup B | C) = \frac{P(A \cup B \cap C)}{P(C)}$$

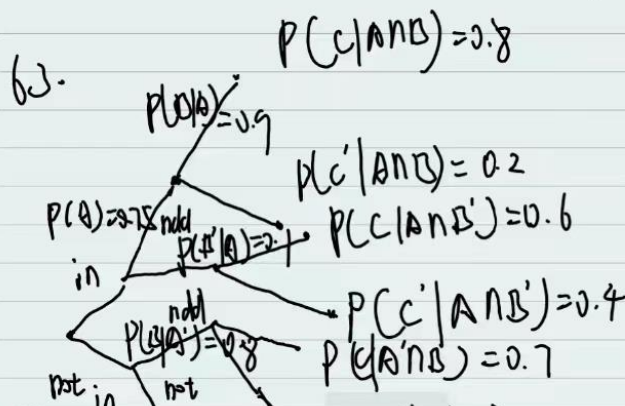
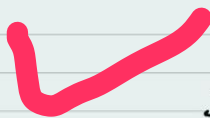
$$= \frac{P((A \cap C) \cup (B \cap C))}{P(C)}$$

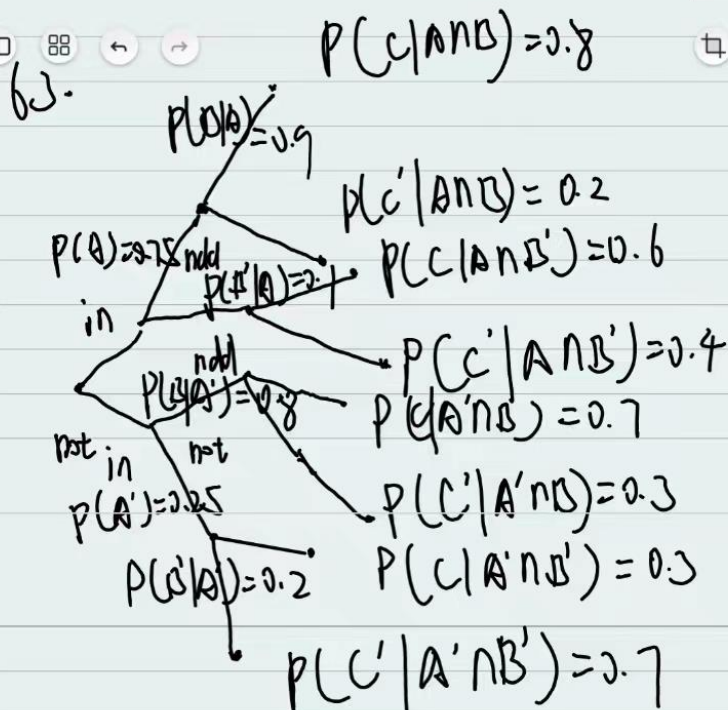
$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$\frac{P((A \cap C) \cup (B \cap C))}{P(C)} = \frac{P(A \cup B \cap C)}{P(C)}$$

$$= \frac{(P(A) + P(B) - P(A \cap B)) \cap C}{P(C)}$$

$$= \frac{P(A \cap C) + P(B \cap C) - P(A \cap B \cap C)}{P(C)}$$





$$\begin{aligned}
 b. P(A \cap B \cap C) &= P(C|A \cap B) \cdot P(A \cap B) \\
 &= P(C|A \cap B) \cdot P(B|A) \cdot P(A) \\
 &= 0.54
 \end{aligned}$$

$$\begin{aligned}
 c. P(B \cap C) &= P(A \cap B \cap C) + P(A' \cap B \cap C) \\
 &= 0.54 + (0.25) \cdot (0.8) \cdot (0.7) \\
 &= 0.68
 \end{aligned}$$

$$d. P(C) = P(A \cap B \cap C) + P(A' \cap B \cap C) + \dots$$

$$= 0.68$$

$$d. P(C) = P(A \cap B \cap C) + P(A' \cap B \cap C) + P(A \cap B' \cap C') + P(A' \cap B' \cap C')$$

$$= 0.54 + 0.45 + 0.14 + 0.045$$

$$= 0.74$$

$$e. P(A|B \cap C) = \frac{P(A \cap B \cap C)}{P(B \cap C)}$$

$$= \frac{0.54}{0.68}$$

$$= 0.7941$$

Assignments for fourth week

Finish the homework:

Section 2.5 71, 72, 80, 84

Section 3.1 4, 5, 8, 10

Section 3.2 12, 23, 25