

Homework 02: 22 CS7 蒋云翔

Section 1.4

Exercises 24.

a. ① let $A(x)$ be a function denoting "x has a cellular ~~out~~ phone"

① $\forall x A(x)$

② let $B(x)$ be a function denoting "x is in your class"

$\exists x (\neg \forall x (B(x) \rightarrow A(x)))$

b. let $A(x)$ be a function denoting "x has seen a foreign movie"

$B(x)$ "x is in your class"

① $\exists x A(x)$

② $\exists x (A(x) \wedge B(x))$

c. let $A(x)$ be a function denoting "x cannot swim"

$B(x)$ "x is in your class"

① $\exists x A(x)$

② $\exists x (A(x) \wedge B(x))$

d. let $A(x)$ be a function denoting "x can solve quadratic equations"

$B(x)$ "x is in your class"

① $\forall x A(x)$

② $\forall x (A(x) \rightarrow B(x))$

Section 1.5

Exercises: 6:

a. Student Randy Goldberg ~~have~~ has CS 252 class.

b. There are some students have Math 695 class.

c. Student Carol Sitea has ^{at least} a class.

d. There is a student has both Math 222 class and CS255 class.

Ex 20. $A(x, y)$

a. let ~~$A(x)$~~ be a function denoting " $x \cdot y > 0$ " $B(x, y)$ denotes " $x > 0, y > 0$ "

$$\forall x (\neg B(x) \rightarrow A(x)) \quad \forall x \forall y (B(x, y) \rightarrow A(x))$$

b. let $A(x, y)$ denotes " $\frac{x+y}{2} > 0$ " $B(x, y)$ denotes " $x > 0, y > 0$ "

$$\forall x \forall y (B(x, y) \rightarrow A(x))$$

c. let $A(x, y)$ denotes " $x - y > 0$ " $B(x, y)$ denotes " $x < 0, y < 0$ "

$$\exists x \exists y (B(x, y) \wedge A(x))$$

d. let $A(x, y)$ denotes " $|x+y| \leq |x| + |y|$ "

$$\forall x \forall y A(x, y)$$

Ex 24.

a. There exists ~~an~~ x for any y that $x + y = y$

b. for any x, y , if $x > 0$ and $y < 0$, then $x - y > 0$

c. ~~There exists x, y , such that~~

c. there exists x and y that satisfy $x \leq 0$ and $y \leq 0$ and $x - y > 0$

d. for any x, y that $x \neq 0$ and $y \neq 0$ if and only if $xy \neq 0$