

Section I: Proof

1. Show that if n is an integer and n^3+5 is odd, then n is even using
 - a) a proof by contraposition.
 - b) a proof by contradiction.
2. Proof that $f(x) = 6x^2 + 5x + 4$ is $O(x^2)$.

Section II: Drawing/Calculation

1. Draw the Venn diagrams for the combination of the sets $A, B, C : \overline{A} \cup (\overline{B} \cap \overline{C})$
2. Solve the linear congruence $2x \equiv 5 \pmod{9}$.

Section III: True/False

1. $(A8E)_{16} = (101010001101)_2$.
2. $(\neg p \wedge (p \vee q)) \rightarrow q$ is a tautology.

Section IV: Completion

1. An algorithm is called _____ if it solves a problem by reducing it to an instance of the same problem with smaller input
2. Among 256 people there are at least _____ who were born in the same month.

Section V: Choices

1. Which is not one of the properties that algorithms generally share?
A. Definiteness B. Finiteness C. Generality D. Comparability
2. Let $S = \{1\}$. Which of the following is not a subset of $P(S)$ (the power set of S).
A. $\{\emptyset\}$. B. $\{1\}$. C. $\{\{1\}\}$. D. $\{\emptyset, \{1\}\}$.