

2. a.  $A = \{LLL, RRR, SSS\}$

b.  $B = \{LRS, RLS, LSR, RSL, SRL, SLR\}$

c.  $C = \{RRL, RRS, RLR, RSR, LRR, SRR\}$

d.  $D = \{RRL, RRS, RLR, RSR, LRR, SRR, LLR, LLS, LSL, LRL, RLL, SLL, SSL, SSR, SLS, SRS, LSS, RSS\}$

e.  $D' = \{LSR, LRS, RLS, RSL, SRL, SLR, RRR, LLL, SSS\}$

$C \cup D = D = \{RRL, RRS, RLR, RSR, LRR, SRR, LLR, LLS, LSL, LRL, RLL, SLL, SSL, SSR, SLS, SRS, LSS, RSS\}$

$C \cap D = \{RRL, RRS, RLR, RSR, LRR, SRR\} = C$

4. a.  $S = \{FFFF, VVVV, FFFV, FFVF, FVFF, VVVF, VVVF, VFVV, FFFV, FVFF, FVVF, VVFF, VVVF, VFFV, VFFF, FVVV\}$

b.  $\{FFFF, FFVF, FVFF, VFFF\}$

c.  $\{FFFF, VVVV\}$

d.  $\{FFFF, VFFF, FVFF, FFVF, FFFV\}$

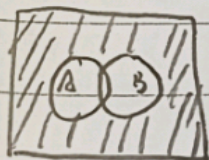
e. Union:  $\{FFFF, VVVV, FVFF, VFFF, FFVF, FFFV\}$

intersection:  $\{FFFF\}$

f. Union:  $\{FFFF, FFVF, FVFF, VFFF, FFFV, VVVV\}$

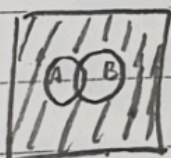
intersection:  $\emptyset$

9. a.



$(A \cup B)'$

=



$A' \cap B'$

b.



$(A \cap B)'$

=



$A' \cup B'$



$$P(A \cup B) = P(A) + P(B) - P(A \cap B) = 0.5 + 0.4 - 0.25 = 0.65$$

b. Let C denotes "the selected individual has neither type of card, so  $P(C) = 1 - P(A \cup B) = 1 - 0.65 = 0.35$ .

c. That is  $A \cap B'$ ,

$$P(A \cap B') = P(A) - P(A \cap B) = 0.5 - 0.25 = 0.25$$

18. Since at least two bulbs must be selected to obtain one that is rated 75W, so it means in the first try we cannot select the 75W bulbs.

Let A denotes "In the first try we select the 75W bulb", we know

$$P(A) = \frac{4}{15}$$

So the probability that at least two attempts to obtain 75W bulb is exactly  $P(A') = 1 - \frac{4}{15} = \frac{11}{15}$ .

27. a. There're 10 outcomes:  $\{Anderson, Box\}$ ,  $\{Anderson, Cox\}$ ,  $\{Anderson, Cramer\}$ ,  $\{Anderson, Fisher\}$ ,  $\{Box, Cox\}$ ,  $\{Box, Cramer\}$ ,  $\{Box, Fisher\}$ ,  $\{Cox, Cramer\}$ ,  $\{Cox, Fisher\}$ ,  $\{Cramer, Fisher\}$ .

So the probability is  $\frac{1}{10}$ .

b.  $\frac{7}{10}$

c. Let A denotes "the two chosen representatives have a total of at least 15 years' teaching experience", so  $P(A) = P(\{Anderson, Fisher\}) + P(\{Box, Cramer\}) + P(\{Box, Fisher\}) + P(\{Cox, Cramer\}) + P(\{Cox, Fisher\}) + P(\{Cramer, Fisher\}) = 0.6$



2.3 30. a.  $1!5!148,3 = 8 \times 7 \times 6 = 336$   
 b.  $1!5! C_{30,6} = \frac{30 \times 29 \times 28 \times 27 \times 26 \times 25}{6 \times 5 \times 4 \times 3 \times 2 \times 1} = 593775$   
 c.  $1!5! C_{8,2} \times C_{10,2} \times C_{12,2} = \frac{8 \times 7}{2} \times \frac{10 \times 9}{2} \times \frac{12 \times 11}{2} = 83160$   
 d.  $p = \frac{83160}{593775} = 0.14$

e.  $p = \frac{C_{8,6} + C_{10,6} + C_{12,6}}{C_{30,6}} = 0.002$

3. a.  $p = \frac{C_{6,2} C_{9,1}}{C_{15,3}} = \frac{135}{455} = 0.2967$

b.  $p = \frac{C_{4,3} + C_{5,3} + C_{6,3}}{C_{15,3}} = \frac{34}{455} = 0.0747$

c.  $p = \frac{C_{4,1} C_{6,1} C_{5,1}}{C_{15,3}} = \frac{120}{455} = 0.2637$

d. In this case, the first 5 tries cannot select a 75W bulb, we denote this as A, so  $P(A) = \frac{C_{9,5}}{C_{15,5}} = \frac{126}{3003} = 0.042$ .

40. a. If they were distinguishable, there're  $12!$  such chain molecules.

If the subscripts are removed from the A's, every 6 sample of  $12!$  chain become one, so there're  $\frac{12!}{6}$  chain molecules.

b.  $p = \frac{A_{4,4}}{\frac{12!}{6 \times 6 \times 6 \times 6}} = \frac{24}{369600} = 0.000065$