

2. a.  $A = \{LLL, sss, RRR\}$  ✓

b.  $B = \{LRS, LSR, SLR, SRL, RSL, RLS\}$

c.  $C = \{RRS, RRL, RSR, RLR, SRR, LRR\}$

d.  $D = \{RRS, RRL, RSR, RLR, SRR, LRR, LLS, LLR, LSL, LRL, SLL, RLL, SSL, SSR, SRS, SLS, LSS, RSS\}$

e.  $D' = \{LLL, sss, RRR, LRS, LSR, SLR, SRL, RSL, RLS\}$

$C \cup D = \{RRS, RRL, RSR, RLR, SRR, LRR, LLS, LLR, LSL, LRL, SLL, RLL, SSL, SSR, SRS, SLS, LSS, RSS\}$

4. a.  $S = \{FFFF, VVVV, VFFF, FVFF, FFVF, FFFV, FFVV, FVVF, FVVF, VVFF, FVVV, VFVV, VVVF, VVVF, VFVF\}$  ✓

b.  $\{FFFF, FFVF, FVFF, VFFF\}$

c.  $\{FFFF, VVVV\}$

d.  $\{FFFF, FFFV, FFVF, FVFF, VFFF\}$

e.  $\{FFFF, VVVV, FFFV, FFVF, FVFF, VFFF\}$

f.  $\{FFFF\}$

part (b)  $\cup$  part (c) =  $\{FFFF, VVVV, FFFV, FFVF, FVFF, VFFF\}$

part (b)  $\cap$  part (c) =  $\emptyset$

30. a. There are  $A_3^3 = 3 \times 2 \times 1 = 6$  ways to do this

b. There are  $C_{30}^6 = \frac{A_{30}^6}{6!} = 593775$  ways to do this

c. There are  $C_8^2 C_{10}^2 C_{12}^2 = 83160$  ways to do this

d. The probability is  $\frac{C_8^2 C_{10}^2 C_{12}^2}{C_{30}^6} = \frac{83160}{593775} = \frac{1848}{13145}$

e. The probability is  $\frac{C_6^6 + C_{10}^6 + C_{12}^6}{C_{30}^6}$

38. a. Let the event be A

$$\text{The } P(A) = \frac{C_6^2 C_9^1}{C_{15}^3} = \frac{27}{91}$$

$$b. P = \frac{C_9^3 + C_5^3 + C_1^3}{C_{15}^3} = \frac{39}{455}$$

c. Let the event be B

$$\text{Then } P(B) = \frac{C_6^1 C_9^1 C_9^1}{C_{15}^3} = \frac{24}{91}$$

d. Let the event be C

$$\text{Then } P(C) = 1 - P(C') = 1 - \left(\frac{9}{15}\right)^3 = 1 - \left(\frac{3}{5}\right)^3 = \frac{288}{3125}$$

40.

a. Let the number be N

If the A, B, C, D can be distinguishable

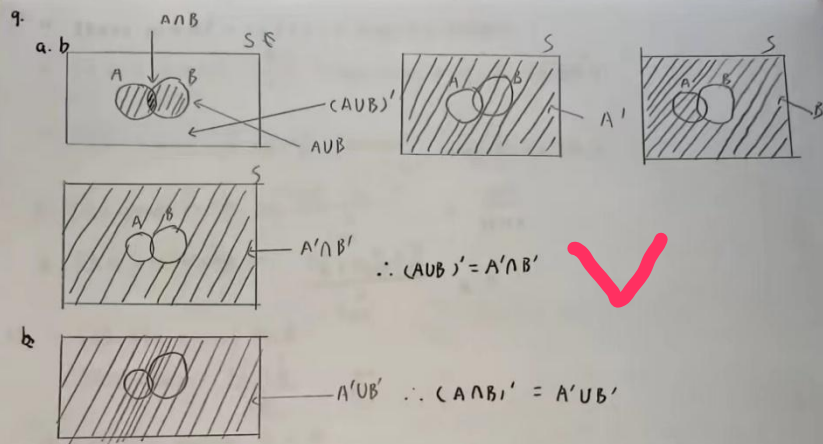
$$\text{Then the } N = 12!$$

If not

$$\text{Then the } N = \frac{C_{12}^3 \cdot C_9^3 \cdot C_6^3 \cdot C_4^3}{C_{16}^4 \cdot C_{12}^4 \cdot C_8^4 \cdot C_4^4}$$

b.

$$P = \frac{A_4^4}{C_{16}^4 \cdot C_{12}^4 \cdot C_8^4 \cdot C_4^4} \quad P = \frac{A_4^4}{C_{12}^3 \cdot C_9^3 \cdot C_6^3 \cdot C_3^3}$$



12.

a.  $P(A \cup B) = P(A) + P(B) - P(A \cap B) = 0.5 + 0.4 - 0.25 = 0.65$

b.  $P(\text{neither}) = 1 - P(A \cup B) = 1 - 0.65 = 0.35$

c.  $P(\text{event}) = P(A) - P(A \cap B) = 0.5 - 0.25 = 0.25$

$$\frac{225}{121}$$

18. Let sol: Let the probability of the event be  $P(A)$ ,

Then  $P(A) = 1 - P(A') = 1 - \frac{11}{15} = \frac{4}{15}$

27. a. The all outcome is  $\{AB', AC, AF, BC, BF, CF, (0, F), (1, F)\}$

So the probability of  $P(AB) = \frac{1}{10}$

b. Let the event be  $P(B)$

So  $P(B) = 1 - P(B') = 1 - \frac{3}{10} = \frac{7}{10}$

c. Let the event be  $C$

Because  $14 + 10 > 14 + 7 > 14 + 6 > 14 + 3 > 10 + 7 > 10 + 6 > 10 + 3$

So  $P(C) = \frac{6}{10} = \frac{3}{5}$