

A

2.4

46. We can find that  $P(A|B)$  instead of the probability of the individual being more than 6 ft tall, knowing that the individual is a professional basketball player. And  $P(B|A)$  is the probability of basketball players in the adult males more than 6 ft.  $P(A|B)$  will be larger because most of the basketball player is 6 ft or taller. It is a large number rather than  $P(B|A)$ .

50.

a.  $P(M \cap L \cap Pr) = 0.05$

b.  $P(M \cap Pr) = P(M \cap Pr \cap L) + P(M \cap Pr \cap S) = 0.05 + 0.07 = 0.12$

c.  $P(S) = 0.56$ ,  $P(L) = 1 - P(S) = 0.44$

d.  $P(M) = P(M \cap L) + P(M \cap S) = 0.49$ ,  $P(Pr|M) = \frac{P(M \cap Pr)}{P(M)} = \frac{0.12}{0.49} = \frac{12}{49}$

e.  $P(M|S) = \frac{P(M \cap S)}{P(S)} = \frac{0.27}{0.56} = \frac{27}{56}$

f.  $P(S|M) = \frac{P(M \cap S)}{P(M)} = \frac{0.27}{0.49} = \frac{27}{49}$ ,  $P(L|M) = \frac{P(M \cap L)}{P(M)} = \frac{0.22}{0.49} = \frac{22}{49}$

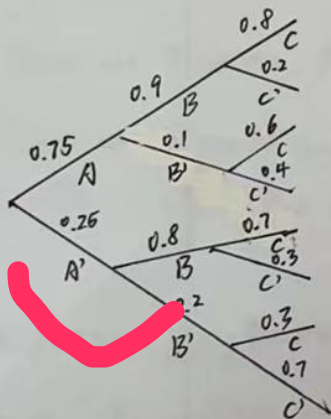
58.

$$\begin{aligned}
 & \text{Since } P(A|C) + P(B|C) - P(A \cap B|C) \\
 &= \frac{P(AC)}{P(C)} + \frac{P(BC)}{P(C)} - \frac{P(AB \cap C)}{P(C)} \\
 &= \frac{P(AC) + P(BC) - P(AB \cap C)}{P(C)} \\
 &= \frac{P(A \cup B \cap C)}{P(C)} \\
 &= P(A \cup B|C)
 \end{aligned}$$

There for,  $P(A \cup B|C) = P(A|C) + P(B|C) - P(A \cap B|C)$

63.

a.



$$\begin{aligned}
 b. P(A \cap B \cap C) &= P(A) \cdot P(B|A) \cdot P(C|A \cap B) \\
 &= 0.75 \times 0.9 \times 0.8 \\
 &= 0.54
 \end{aligned}$$

$$\begin{aligned}
 c. P(B \cap C) &= P(A \cap B \cap C) + P(A' \cap B \cap C) \\
 &= 0.54 + 0.25 \times 0.8 \times 0.7 \\
 &= 0.68
 \end{aligned}$$

$$\begin{aligned}
 d. P(C) &= P(A \cap B \cap C) + P(A \cap B' \cap C) + P(A' \cap B \cap C) + P(A' \cap B' \cap C) \\
 &= 0.54 + 0.75 \times 0.1 \times 0.6 + 0.25 \times 0.8 \times 0.7 + 0.25 \times 0.2 \times 0.3 \\
 &= 0.54 + 0.045 + 0.14 + 0.015 \\
 &= 0.74
 \end{aligned}$$

$$e. P(A|B \cap C) = \frac{P(A \cap B \cap C)}{P(B \cap C)} = \frac{0.54}{0.68} = \frac{27}{34}$$

2.5

71.

$$a. P(B' \cap A') = P(A') \cdot P(B') = 0.28 \text{ for } A, B \text{ are independent.}$$

$$b. P(\text{at least one is successful}) = P(A \cap B) + P(A \cap B') + P(A' \cap B) = 1 - P(A' \cap B') = 0.72$$

$$c. P(A \cap B' | \text{at least one is successful}) = \frac{P(A \cap B')}{P(\text{at least one is successful})} = \frac{0.4 \times (1 - 0.7)}{0.72} = \frac{1}{9}$$

72.

In exercises 13.

 $P(A_1, A_2) = 0.11 \neq P(A_1) \cdot P(A_2) = 0.055$ .  $A_1$  and  $A_2$  are not independent $P(A_1, A_3) = 0.05 \neq P(A_1) \cdot P(A_3) = 0.0616$ .  $A_1$  and  $A_3$  are not independent $P(A_2, A_3) = 0.07 = P(A_2) \cdot P(A_3) = 0.07$ .  $A_2$  and  $A_3$  are independent

80.

Since  $P(\text{system work}) = 1 - P(\text{system doesn't work})$ 

$$= 1 - (1 - 0.9) \times (1 - 0.9) \times (1 - 0.9 \times 0.9)$$

$$= 1 - 0.1 \times 0.1 \times 0.19$$

$$= 0.9981$$



84. Suppose the event of  $i$ th car pass is  $A_i$ ,  $P(A_i) = 0.7$  while  $A_i'$  means fail.

a.  $P(A_1 \cap A_2 \cap A_3) = P(A_1) \times P(A_2) \times P(A_3) = 0.343$

b.  $P(\text{at least one of three cars fails}) = 1 - P(A_1 \cap A_2 \cap A_3) = 0.637$

c.  $P(\text{exactly one of the next three inspected passes})$ ,

$$= P(A_1 \cap A_2' \cap A_3') + P(A_1' \cap A_2 \cap A_3') + P(A_1' \cap A_2' \cap A_3)$$

$$= (0.7 \times (1-0.7) \times (1-0.7)) \times 3$$

$$= 0.189$$

d.  $P(\text{at most one of the next three vehicles inspected passes})$ ,

$$= P(\text{exactly one of the next three inspected passes}) + P(A_1' \cap A_2' \cap A_3')$$

$$= 0.189 + (1-0.7)^3$$

$$= 0.216$$

e.  $P = \frac{P(A_1 \cap A_2 \cap A_3)}{P(\text{at least one of the next three vehicles inspected passes})}$

$$= \frac{0.343}{0.637}$$

$$= 0.5385$$

3.1

4.

$X = \{1, 2, 3, 4\}$ . For example,  $X=1$  for 100000,  $X=4$  for 528300.  
and  $X=2$  for 400010.

5. No. Through a coin until a head, it would get an infinite result set, but each time it is only two result.

8.

$Y=3: SSS$   $Y=4: FSSS$   $Y=5: FFSSS, SFSSS$

$Y=6: FFFSSS, FSFSSS, SFFSSS, SSFSSS$

$Y=7: FFFFSSS, SFFFSSS, FSFFSSS, FFSSFSSS, SSFFSSS, SFSSFSSS, FSSSFSSS$

10.

a.  $T = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$

b.  $X = \{-6, -5, -4, -3, -2, -1, 0, 1, 2, 3, 4\}$

c.  $V = \{0, 1, 2, 3, 4, 5, 6\}$

d.  $Z = \{0, 1, 2\}$

3.2

12.

a. Since it has 50 seats,  $P(Y \leq 50) = 0.05 + 0.1 + 0.12 + 0.14 + 0.25 + 0.17 = 0.83$

b.  $P(Y > 50) = 0.06 + 0.05 + 0.03 + 0.02 + 0.01 = 0.17$

c. While you can take the plane,  $P(Y \leq 49) = 0.05 + 0.1 + 0.12 + 0.14 + 0.25 = 0.66$   
while you are third person.  $P(Y \leq 47) = 0.05 + 0.1 + 0.12 = 0.27$

23.

a.  $P(X=2) = F(3) - F(2) = 0.39 - 0.19 = 0.2$

b.  $P(X > 3) = 1 - P(X \leq 3) = 1 - F(3) = 0.61$

c.  $P(2 \leq X \leq 5) = F(5) - F(1) = 0.78$

d.  $P(2 < X < 5) = F(4) - F(2) = 0.48$



25.

$$P(0) = P(X=0) = p$$

$$P(1) = P(X=1) = (1-p)p$$

$$P(2) = P(X=2) = (1-p)^2 p$$

$$\text{therefor, } P(n) = P(X=n) = (1-p)^n \cdot p$$