

A

## Section 5.3 5.4 5.5

Ex. 38

$$a) \text{ pmf: } T_0 \begin{array}{|c|c|c|c|c|c|} \hline 0 & 1 & 2 & 3 & 4 & \\ \hline \end{array}$$

$$P(T_0) \begin{array}{|c|c|c|c|c|c|} \hline 0.04 & 0.2 & 0.37 & 0.3 & 0.09 & \\ \hline \end{array}$$

$$b) E(T_0) \hat{=} \mu_{T_0} = 0 \times 0.04 + 1 \times 0.2 + \dots + 4 \times 0.09 = 2.2 = 2 \mu$$

$$c) \sigma_{T_0}^2 = E(T_0^2) - \mu_{T_0}^2, E(T_0^2) = 0^2 \times 0.04 + 1^2 \times 0.2 + \dots + 4^2 \times 0.09 = 5.82$$

$$\therefore \sigma_{T_0}^2 = 5.82 - 2.2^2 = 0.98$$

$$d) \text{ Now: } E(T) = 4 \times \mu = 4.4, V(T) = 4\sigma^2 = 4 \times 0.49 = 1.96$$

$$e) P(T_0=8) = (0.3)^4 = 0.0081$$

$$P(T_0 \geq 7) = P(T_0=7) + P(T_0=8) = (0.3)^3 \times 0.5 \times 4 + 0.0081 = 0.0621$$

Ex. 41

$$a) \bar{X} \begin{array}{|c|c|c|c|c|c|c|c|} \hline 1 & 1.5 & 2 & 2.5 & 3 & 3.5 & 4 & \\ \hline \end{array}$$

$$P(\bar{X}) \begin{array}{|c|c|c|c|c|c|c|c|} \hline 0.16 & 0.24 & 0.25 & 0.2 & 0.1 & 0.04 & 0.01 & \\ \hline \end{array}$$

$$b) P(\bar{X} \leq 2.5) = 0.16 + 0.24 + 0.25 + 0.2 = 0.85$$

$$c) R \begin{array}{|c|c|c|c|} \hline 0 & 1 & 2 & 3 & \\ \hline \end{array}$$

$$P(R) \begin{array}{|c|c|c|c|} \hline 0.3 & 0.4 & 0.22 & 0.08 & \\ \hline \end{array}$$

$$d) P(\bar{X} \leq 1.5) = (0.4)^4 + C_4^2 \cdot (0.4)^2 \cdot (0.3)^2 + C_4^1 \cdot (0.4)^3 \cdot (0.2)$$

$$= 0.0256 + 6 \times 0.16 \times 0.09 + 4 \times 0.064 \times 0.2$$

$$= 0.1632$$

## Section 5.4

Ex. 46

$$a) \text{ Center at } \mu=12, \sigma_{\bar{X}} = \frac{\sigma}{\sqrt{16}} = 0.01 \text{ cm}$$

$$b) \text{ Still center at } \mu=12, \sigma_{\bar{X}} = \frac{\sigma}{\sqrt{64}} = 0.005 \text{ cm}$$

$$c) \text{ part b) } \bar{X} \text{ is more likely to be within } 0.01 \text{ cm of } 12 \text{ cm.}$$

The reason is that: The larger sample size is, the more normal will be  
normaler (concentrated)

Ex. 51.

The first day:  $P(\bar{X} \leq 11) = P(\bar{X} \leq \frac{11-10}{2/\sqrt{5}}) = P(\bar{X} \leq 1.12) = 0.8686$  ✓The second day:  $P(\bar{X} \leq 11) = P(\bar{X} \leq \frac{11-10}{2/\sqrt{6}}) = P(\bar{X} \leq 1.22) = 0.8888$ So:  $p = 0.8686 \times 0.8888 = 0.772$  ✓ ✓

Ex. 55

a) As it is Poisson distribution: So:  $\sigma^2 = \mu = 50$ It  $\mu = 50$  is large enough, so we can use normal ~ to do it.

$$\begin{aligned} P(35 \leq X \leq 70) &= P\left(\frac{35-50}{\sqrt{50}} \leq X \leq \frac{70-50}{\sqrt{50}}\right) = P(-2.12 \leq X \leq 2.83) \\ &= P(2.83) - P(-2.12) \\ &= 0.9977 - 0.017 \\ &= 0.9807 \end{aligned}$$
 ✓

$$b) E(T_0) = 50 \times 5 = 250, V(T_0) = n\sigma^2 = 250 \quad \sigma_{T_0} = \sqrt{250} = 15.81$$

$$\begin{aligned} c) P(225 \leq T_0 \leq 275) &= P\left(\frac{225-250}{15.81} \leq T_0 \leq \frac{275-250}{15.81}\right) \\ &= P(-1.58) - P(1.58) \\ &= 0.9429 - 0.0571 \\ &= 0.8858 \end{aligned}$$
 ✓

Section 8.5

Ex. 58.

$$a) E(\text{Volume}) = 27 \times 200 + 125 \times 250 + 512 \times 100 = 87850$$
 ✓

$$V(\text{Volume}) = 27^2 \times (10)^2 + 125^2 \times (12)^2 + 512^2 \times (8)^2 = 1910016$$

b) The expected value is still correct, but variance not, because the correlation will influence the final result. ✓





Ex. 70.

a)  $E(Y_i) = 0.5$ ,  $E(W) = \sum_{i=1}^n i \cdot E(Y_i) = \frac{n(n+1)}{4}$

b)  $V(Y_i) = 0.5(1-0.5) = 0.25$ ,  $V(W) = \sum_{i=1}^n i^2 V(Y_i) = \frac{n(n+1)(2n+1)}{24}$

Ex. 73

a) Normal distribution (CLT Theorem)

b) still normal distribution, linear combination will not break it if it is normal before.

c)  $\mu = 105 - 100 = 5$ ,  $\sigma = \sqrt{\frac{64}{40} + \frac{36}{35}} = 1.62$

$P(-1 \leq \bar{X} - \bar{Y} \leq 1) = P\left(\frac{-1-5}{1.62} \leq \bar{X} - \bar{Y} \leq \frac{1-5}{1.62}\right) = P(-3.7 \leq \bar{X} - \bar{Y} \leq -2.47) = 0.0068$

d)  $P(\bar{X} - \bar{Y} > 10) = P\left(\bar{X} - \bar{Y} > \frac{10-5}{1.62}\right) = 0.001$ , too small!  
we will doubt whether  $\mu = 5$

