

Section 2.1

A

2.

$$a. A = \{ (C, L, L, L), (C, R, R, R), (S, S, S) \}$$

$$b. B = \{ (C, L, S, R), (C, L, R, S), (C, R, L, S), (C, R, S, L), \\ (S, R, L), (S, L, R) \}$$

$$c. C = \{ \cancel{(C, R, R, R)}, (C, R, R, S), (C, R, R, L), (C, R, S, R), (C, R, L, R), \\ (S, R, R), (L, R, R) \}$$

$$d. D = \{ (C, R, R, S), (C, R, R, L), (C, L, L, S), (C, L, L, R), \\ (S, S, R), (S, S, L), \\ (C, R, S, R), (C, R, L, R), (C, L, S, L), (C, L, R, L), \\ (S, R, S), (S, L, S), \\ (S, R, R), (L, R, R), (S, L, L), (C, R, L, L), \\ (R, S, S), (L, S, S) \}$$

$$e. D' = \{ (C, R, R, R), (C, L, L, L), (S, S, S), (C, L, S, R), (C, L, R, S), (C, R, L, S), \\ (C, R, S, L), (C, S, R, L), (C, S, L, R) \}$$

$$C \cup D = D, \quad C \cap D = C$$

4.

$$a. B = \{ (F, F, F, F), (F, F, F, V), (F, F, V, F), (F, F, V, V), (F, V, F, F), \\ (F, V, F, V), (F, V, V, F), (F, V, V, V), (V, F, F, F), (V, F, F, V), \\ (V, F, V, F), (V, F, V, V), (V, V, F, F), (V, V, F, V), (V, V, V, F), \\ (V, V, V, V) \}$$

b. Given that the event that exactly three of the selected mortgages are fixed rate is B.

$$B = \{(F, F, F, V), (F, F, V, F), (F, V, F, F), (V, F, F, F)\}$$

c. Given that the event that all four mortgages are of the same type is event C.

$$C = \{(F, F, F, F), (V, V, V, V)\}$$

d. Given that the event at most one of four is a variable-rate is D.

$$D = \{(F, F, F, F), (F, F, F, V), (F, F, V, F), (F, V, F, F), (V, F, F, F)\}$$

$$e. C \cup D = \{(F, F, F, F), (F, F, F, V), (F, F, V, F), (F, V, F, F), (V, F, F, F), (V, V, V, V)\}$$

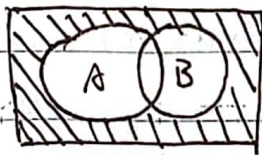
$$C \cap D = \{(F, F, F, F)\}$$

$$f. B \cup C = \{(F, F, F, F), (F, F, F, V), (F, F, V, F), (F, V, F, F), (V, F, F, F), (V, V, V, V)\}$$

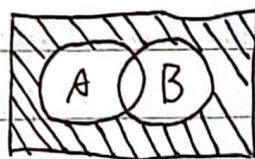
$$B \cap C = \emptyset$$

9.

a.

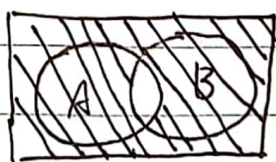


$$(A \cup B)'$$

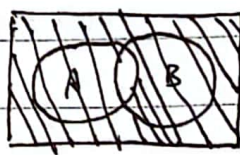


$$A' \cup B'$$

b.



$$(A \cap B)'$$



$$A' \cup B'$$

Section 2.2.

12. a. $P(A \cup B) = P(A) + P(B) - P(A \cap B) = 0.65$

b. Let A^c be the event that the selected individual has neither of the card.

$$P(A^c) = P((A \cup B)^c) = 0.35$$

c. Giving that the event ^{Dis} the selected student has ~~visa~~ but not MasterCard

~~P(B)~~

$$P(D) = P(A \cup B) - P(B) = 0.25$$

$$= P(A) - P(A \cap B) = 0.25$$

18. Let the A be the event that at least two bulbs must be selected to obtain one that is rated 75w.

$$P(A) = \frac{C(4,1) \cdot C(11,1) + C(4,2)}{C(15,2)} = \frac{14}{15} = 1 - \frac{4}{15} = \frac{11}{15}$$

27. a. Let the A be the event that both Anderson and Box will be selected.

the outcomes = $\{(And, Box), (And, Cox), (And, Cra), (And, Fish),$

$(Box, Cox), (Box, Cra), (Box, Fish), (Cox, Cra), (Cox, Fish),$
 $(Cra, Fish)\}$

$$P(A) = \frac{1}{N(\text{outcomes})} = \frac{1}{10}$$

b. Let B be the event that at least one of two member whose name begin with "c".

$$P(B) = \frac{C(2,1) \cdot C(3,1) + C(2,2)}{N(\text{outcomes})} = \frac{7}{10}$$

c. the total years of the teaching experience respectively are

$\{9, 10, 13, 17, 13, 16, 20, 17, 21, 24\}$

The probability that two has total 15's teaching experience is $P = \frac{6}{10} = \frac{3}{5}$

Section 2.3.

30. a. There are $P(8,3) = \frac{8!}{5!} = 336$ ways.

b. There are $C(30,6) = \frac{30!}{24!6!} = 593775$ ways.

~~c. There are $C(8,2) \cdot C(10,2) \cdot C(12,2) = \frac{8!}{2!6!} \times \frac{10!}{2!8!} \times \frac{12!}{2!10!} = 83160$ ways.~~

~~d. For zinfandel, there are $C(8,2) \cdot C(22,4) = \frac{8!}{2!6!} \times \frac{22!}{4!18!} = 204820$ ways.~~

~~For merlot There are $C(10,2) \cdot C(20,4) = \frac{10!}{2!8!} \times \frac{20!}{4!16!} = 218025$ ways.~~

~~For cabernet, there are $C(12,2) \cdot C(18,4) = \frac{12!}{2!10!} \times \frac{18!}{4!14!} = 20196$ ways.~~

c. There are $C(8,2) \cdot C(10,2) \cdot C(12,2) = \frac{8!}{2!6!} \times \frac{10!}{2!8!} \times \frac{12!}{2!10!} = 8316$ ways.

d. The probability is $8316 / C(30,6) \approx 0.14$

e. There are $C(8,6) + C(10,6) + C(12,6) = \frac{8!}{2!6!} + \frac{10!}{4!6!} + \frac{12!}{6!6!} = 1162$ ways.

The probability: $\frac{1162}{C(30,6)} = 0.2 \times 10^{-3}$

38. a. Giving that A is the event that exactly two bulbs are rated 25 w

$$P(A) = \frac{C(6,2) \cdot C(9,1)}{C(15,3)} = \frac{21}{91}$$

455

b. Giving that B is the event that three of selected bulb are with same rate.

$$P(B) = \frac{C(6,3) + C(4,3) + C(5,3)}{C(15,3)} = \frac{34}{455}$$

c. Giving that C is the event that each type is selected.

$$P(C) = \frac{C(6,1) \cdot C(4,1) \cdot C(5,3)}{C(15,3)} = \frac{24}{91}$$

d. giving that D is the event that necessary to examine at least 6 bulbs.

$$P(D) = 1 - \frac{C(6,1) \cdot C(4,1) \cdot C(5,1)}{C(15,3)} - \frac{C(6,2) \cdot C(4,1)}{C(15,3)} - \frac{C(6,3)}{C(15,3)}$$

$$P(D) = 1 - \frac{C(6,1) \cdot C(4,1) \cdot C(5,1)}{C(15,3)} - \frac{C(6,2) \cdot C(4,1)}{C(15,3)} - \frac{C(6,3)}{C(15,3)} = 1 - \frac{24}{91} - \frac{15}{35} - \frac{1}{35} = 0.42$$

40. a. For each character there are $P(3,3) = 6$ ways.

There are $P(12,12) = 12!$ ways if they are distinguish.

There are $\frac{P(12,12)}{P(3,3)^4} = \frac{12!}{6^4} = 369600$ ways.

b. Giving that the ~~prob~~ event each type of element are close to is B

$$P(B) = \frac{P(4,4)}{369600} = 6.44 \times 10^{-5}$$