# 0.12 Candidate Keys

you-said

x (genreid, genre, runtime, title, movieid, isadult, year);  $F = \{\{genreid, title\} => \{runtime\}, \{genre\} => \{genreid\}, \{movieid\} => \{isadult\}, \{movieid\} => \{title\}, \{movieid\} => \{runtime\}, \{genreid\} => \{genre\}, \{runtime, title\} => \{year\}, \{movieid\} => \{year\}, \{genre, title\} => \{runtime\}, \{title\} => \{isadult\}. apply this algorithm to the above set of functional dependencies: functional dependencies (FD) of type -> for ith functional dependency. left = Union of all in FD right = Union of all in FD Initialize case_1, case_2, case_3, case_4 as empty sets. For x in attributes: if x left & x right: case_1.add(x) if x left & x right: case_2.add(x) return attributes in case_1, case_2, case_3, case_4.$ 

ChatGPT said:

Let's go through the algorithm step-by-step with the relation x (genreid, genre, runtime, title, movieid, isaduland the given functional dependencies:

step-1-identify-left-and-right-sets

# Step 1: Identify Left and Right Sets

# Functional Dependencies (FDs):

- 1.  $\{\text{genreid}, \text{title}\} \rightarrow \{\text{runtime}\} \{\text{genreid}, \text{title}\} \rightarrow \{\text{runtime}\}$
- 2.  $\{genre\} \rightarrow \{genreid\} \{genre\} \rightarrow \{genreid\}$
- 3.  $\{\text{movieid}\} \rightarrow \{\text{isadult}\} \{\text{movieid}\} \rightarrow \{\text{isadult}\}$
- 4.  $\{\text{movieid}\} \rightarrow \{\text{title}\} \{\text{movieid}\} \rightarrow \{\text{title}\}$
- 5.  $\{\text{movieid}\} \rightarrow \{\text{runtime}\} \{\text{movieid}\} \rightarrow \{\text{runtime}\}$
- 6.  $\{genreid\} \rightarrow \{genre\} \{genreid\} \rightarrow \{genre\}$
- 7.  $\{\text{runtime, title}\} \rightarrow \{\text{year}\} \{\text{runtime, title}\} \rightarrow \{\text{year}\}$
- 8.  $\{\text{movieid}\} \rightarrow \{\text{year}\} \{\text{movieid}\} \rightarrow \{\text{year}\}$
- 9.  $\{genre, title\} \rightarrow \{runtime\} \{genre, title\} \rightarrow \{runtime\}$
- 10.  $\{\text{title}\} \rightarrow \{\text{isadult}\} \{\text{title}\} \rightarrow \{\text{isadult}\}$

Now, find the union of all left-hand sides  $(\alpha)$  and right-hand sides  $(\beta)$ :

- Left (Union of  $\alpha$ ): genreid, title, genre, movieid, runtimegenreid, runtimege
- Right (Union of  $\beta$ ): runtime, genreid, isadult, title, year, genreruntime, genreid, isadult, title, year, genre step-2-classify-the-attributes

# Step 2: Classify the Attributes

Now we classify the attributes based on their membership in the "Left" and "Right" sets:

attributes-in-x-text genreid text genretext run time text title text movie id text is adult text year x genreid genrer untime text title text movie id text is adult text year x genreid genrer untime text title text movie id text is adult text year x genreid genrer untime text title text movie id text is adult text year x genreid genrer untime text title text movie id text is adult text year x genreid genrer untime text title text movie id text is adult text year x genreid genrer untime text title text movie id text is adult text year x genreid genrer untime text title text movie id text is adult text year x genreid genrer untime text title text movie id text is adult text year x genreid genrer untime text title text movie id text is adult text year x genreid genrer untime text title text movie id text is adult text year x genreid genrer untime text title text movie id text is adult text year x genreid genrer untime text title text movie id text is adult text year x genreid genrer untime text title text movie id text is adult text year x genreid genrer untime text year x genreid genre

# 1. genreid

In Left: Yes In Right: Yes

# Case 4

# 2. genre

In Left: Yes
In Right: Yes
Case 4

## 3. runtime

In Left: Yes
In Right: Yes
Case 4

## 4. title

In Left: Yes
In Right: Yes
Case 4

# 5. movieid

In Left: Yes In Right: Yes Case 4

## 6. isadult

In Left: No In Right: Yes Case 2 7. year

In Left: No In Right: Yes Case 2

step-3-final-output

# Step 3: Final Output

- Case 1 (not in Left, not in Right):
  None
- Case 2 (not in Left, but in Right): {isadult, year}{isadult, year}
- Case 3 (in Left, but not in Right):
  None
- Case 4 (in Left and in Right): {genreid, genre, runtime, title, movieid}{genreid, genre, runtime, title, movieid} result

# Result:

- Case 1: None
- Case 2: {isadult, year}{isadult, year}
- Case 3: None
- Case 4: {genreid, genre, runtime, title, movieid}{genreid, genre, runtime, title, movieid}

you-said-1

movieid is not in right

ChatGPT said:

You're right! I mistakenly included **movieid** in the right set, but it doesn't actually appear on the right-hand side of any functional dependency. Let's correct the solution accordingly.

step-1-identify-left-and-right-sets-1

## Step 1: Identify Left and Right Sets

# Functional Dependencies (FDs):

- 1.  $\{genreid, title\} \rightarrow \{runtime\} \{genreid, title\} \rightarrow \{runtime\}$
- 2.  $\{genre\} \rightarrow \{genreid\} \{genre\} \rightarrow \{genreid\}$
- 3.  $\{\text{movieid}\} \rightarrow \{\text{isadult}\} \{\text{movieid}\} \rightarrow \{\text{isadult}\}$
- 4.  $\{\text{movieid}\} \rightarrow \{\text{title}\} \{\text{movieid}\} \rightarrow \{\text{title}\}$
- 5.  $\{\text{movieid}\} \rightarrow \{\text{runtime}\} \{\text{movieid}\} \rightarrow \{\text{runtime}\}$
- 6.  $\{genreid\} \rightarrow \{genre\} \{genreid\} \rightarrow \{genre\}$
- 7.  $\{\text{runtime}, \text{title}\} \rightarrow \{\text{year}\} \{\text{runtime}, \text{title}\} \rightarrow \{\text{year}\}$
- 8.  $\{\text{movieid}\} \rightarrow \{\text{year}\} \{\text{movieid}\} \rightarrow \{\text{year}\}$
- 9.  $\{\text{genre, title}\} \rightarrow \{\text{runtime}\} \{\text{genre, title}\} \rightarrow \{\text{runtime}\}$
- 10.  $\{\text{title}\} \rightarrow \{\text{isadult}\} \{\text{title}\} \rightarrow \{\text{isadult}\}$ 
  - Left (Union of  $\alpha$ ): genreid, title, genre, movieid, runtimegenreid, runtimege
  - Right (Union of  $\beta$ ): runtime, genreid, isadult, title, year, genreruntime, genreid, isadult, title, year, genre step-2-classify-the-attributes-1

#### Step 2: Classify the Attributes

Now we classify the attributes based on their membership in the "Left" and "Right" sets:

attributes-in-x-textgenreidtextgenretextruntimetext<br/>titletextmovieidtextisadulttextyearxgenreidgenreruntin<br/>1

## 1. genreid

In Left: Yes
In Right: Yes
Case 4

# 2. genre

In Left: Yes In Right: Yes Case 4

# 3. runtime

In Left: Yes In Right: Yes Case 4

## 4. title

In Left: Yes
In Right: Yes
Case 4

# 5. movieid

In Left: Yes
In Right: No
Case 3

# 6. isadult

In Left: No In Right: Yes Case 2

# 7. year

In Left: No In Right: Yes Case 2

step-3-final-output-1

# Step 3: Final Output

- Case 1 (not in Left, not in Right):
  None
- Case 2 (not in Left, but in Right): {isadult, year}{isadult, year}
- Case 3 (in Left, but not in Right): {movieid}{movieid}

• Case 4 (in Left and in Right): {genreid, genre, runtime, title}{genreid, genre, runtime, title}

corrected-result

#### **Corrected Result:**

- Case 1: None
- Case 2: {isadult, year}{isadult, year}
- Case 3: {movieid}{movieid}
- Case 4: {genreid, genre, runtime, title}{genreid, genre, runtime, title} vou-said-2

use this formula for closure: Closure of beta under F (beta+) result := beta Do For each gema  $\rightarrow$  delta in F: If (gema result): result := result Union delta While (result does not change) Return result give closure of case 3

ChatGPT said:

Let's apply the closure algorithm for **Case 3**, where the attribute is {movieid}{movieid}. given-functional-dependencies-fds

# Given Functional Dependencies (FDs):

- 1.  $\{genreid, title\} \rightarrow \{runtime\} \{genreid, title\} \rightarrow \{runtime\}$
- 2.  $\{genre\} \rightarrow \{genreid\} \{genre\} \rightarrow \{genreid\}$
- 3.  $\{\text{movieid}\} \rightarrow \{\text{isadult}\} \{\text{movieid}\} \rightarrow \{\text{isadult}\}$
- 4.  $\{\text{movieid}\} \rightarrow \{\text{title}\} \{\text{movieid}\} \rightarrow \{\text{title}\}$
- 5.  $\{\text{movieid}\} \rightarrow \{\text{runtime}\} \{\text{movieid}\} \rightarrow \{\text{runtime}\}$
- 6.  $\{genreid\} \rightarrow \{genreid\} \rightarrow \{genreid\} \rightarrow \{genre\}$
- 7.  $\{\text{runtime, title}\} \rightarrow \{\text{year}\} \{\text{runtime, title}\} \rightarrow \{\text{year}\}$
- 8.  $\{\text{movieid}\} \rightarrow \{\text{year}\} \{\text{movieid}\} \rightarrow \{\text{year}\}$
- 9.  $\{genre, title\} \rightarrow \{runtime\} \{genre, title\} \rightarrow \{runtime\}$
- 10.  $\{\text{title}\} \rightarrow \{\text{isadult}\} \{\text{title}\} \rightarrow \{\text{isadult}\}$

step-by-step-process-to-find-the-closure-of-textmovieidmovieid-denoted-betaux3b2

Step-by-Step Process to Find the Closure of  $\{\text{movieid}\}\{\text{movieid}\}\$  (denoted  $\beta^++$ ):Step-by-Step Process to Find the Closure of  $\{\text{movieid}\}\$  (denoted  $\beta^++$ ):

# 1. Initialize:

```
result := \{movieid\}
    result:={movieid}
2. Iterate through FDs:
    FD 3:
    \{\text{movieid}\} \rightarrow \{\text{isadult}\} \{\text{movieid}\} \rightarrow \{\text{isadult}\}
    Since \{\text{movieid}\}\subseteq \text{result}\{\text{movieid}\}\result, update result:
                                              result := \{movieid, isadult\}
    result:={movieid,isadult}
    FD 4:
    \{\text{movieid}\} \rightarrow \{\text{title}\} \{\text{movieid}\} \rightarrow \{\text{title}\}
    Since \{\text{movieid}\}\subseteq \text{result}\{\text{movieid}\}\result, update result:
                                          result := \{movieid, isadult, title\}
    result:={movieid,isadult,title}
    FD 5:
    \{\text{movieid}\} \rightarrow \{\text{runtime}\} \{\text{movieid}\} \rightarrow \{\text{runtime}\}
    Since \{\text{movieid}\}\subseteq \text{result}\{\text{movieid}\}\result, update result:
                                    result := \{movieid, isadult, title, runtime\}
    result:={movieid,isadult,title,runtime}
    FD 8:
    \{\text{movieid}\} \rightarrow \{\text{year}\} \{\text{movieid}\} \rightarrow \{\text{year}\}
    Since \{\text{movieid}\}\subseteq \text{result}\{\text{movieid}\}\result, update result:
                                result := \{movieid, is adult, title, runtime, year\}
    result:={movieid,isadult,title,runtime,year}
```

3. **No More Changes**: At this point, applying other FDs does not add any new attributes to the result. So, the closure process terminates.

final-closure-of-textmovieidmovieid

# Final Closure of $\{\text{movieid}\}\$ is Final Closure of $\{\text{text}\}\$ fmovieid $\}\$ ?

```
\{\text{movieid}\}^+ = \{\text{movieid}, \text{isadult}, \text{title}, \text{runtime}, \text{year}\}
```

{movieid}+={movieid,isadult,title,runtime,year}

This is the full closure of **movieid** under the given set of functional dependencies. you-said-3

use this formula for closure: Closure of beta under F (beta+) result := beta Do For each gema  $\rightarrow$  delta in F: If (gema result): result := result Union delta While (result does not change) Return result give closures of {movieid, genreid}, {movieid, genre}, {movieid, runtime}, {movieid, title}

ChatGPT said:

Let's apply the closure formula to the sets {movieid, genreid} {movieid, genreid}, {movieid, genre} {movieid, runtime}, and {movieid, title} {movieid, title}.

given-functional-dependencies-fds-1

# Given Functional Dependencies (FDs):

- 1.  $\{genreid, title\} \rightarrow \{runtime\} \{genreid, title\} \rightarrow \{runtime\}$
- 2.  $\{genre\} \rightarrow \{genreid\} \{genre\} \rightarrow \{genreid\}$
- 3.  $\{\text{movieid}\} \rightarrow \{\text{isadult}\} \{\text{movieid}\} \rightarrow \{\text{isadult}\}$
- 4.  $\{\text{movieid}\} \rightarrow \{\text{title}\} \{\text{movieid}\} \rightarrow \{\text{title}\}$
- 5.  $\{\text{movieid}\} \rightarrow \{\text{runtime}\} \{\text{movieid}\} \rightarrow \{\text{runtime}\}$
- 6.  $\{genreid\} \rightarrow \{genreid\} \rightarrow \{genreid\} \rightarrow \{genre\}$
- 7.  $\{\text{runtime, title}\} \rightarrow \{\text{year}\} \{\text{runtime, title}\} \rightarrow \{\text{year}\}$
- 8.  $\{\text{movieid}\} \rightarrow \{\text{year}\} \{\text{movieid}\} \rightarrow \{\text{year}\}$
- 9.  $\{genre, title\} \rightarrow \{runtime\} \{genre, title\} \rightarrow \{runtime\}$
- 10.  $\{\text{title}\} \rightarrow \{\text{isadult}\} \{\text{title}\} \rightarrow \{\text{isadult}\}$

closure-of-textmovieidtextgenreidmovieidgenreid

 $1. \ Closure \ of \ \{movieid, genreid\} \\ \{movieid, genreid\} \\ : 1. \ Closure \ of \ \{\text\{movieid\}, \text\{genreid\} \\ \\ step-by-step-process \\$ 

1. Initialize:

```
\label{eq:result} \operatorname{result} := \{\operatorname{movieid}, \operatorname{genreid}\} \operatorname{result} := \{\operatorname{movieid}, \operatorname{genreid}\}
```

2. Iterate through FDs:

```
FD 6:
```

```
\{genreid\} \rightarrow \{genre\} \{genreid\} \rightarrow \{genre\}
Since \{genreid\} \subseteq result\{genreid\} result, update result:
```

```
result := \{movieid, genreid, genre\}
```

result:={movieid,genreid,genre}

## **FD 3**:

```
\{\text{movieid}\} \rightarrow \{\text{isadult}\} \{\text{movieid}\} \rightarrow \{\text{isadult}\}
Since \{\text{movieid}\} \subseteq \text{result}\{\text{movieid}\} result, update result:
```

result := {movieid, genreid, genre, isadult}

result:={movieid,genreid,genre,isadult}

#### FD 4:

```
\{\text{movieid}\} \rightarrow \{\text{title}\} \{\text{movieid}\} \rightarrow \{\text{title}\}
Since \{\text{movieid}\} \subseteq \text{result}\{\text{movieid}\} result, update result:
```

result := {movieid, genreid, genre, isadult, title}

result:={movieid,genreid,genre,isadult,title}

# **FD** 5:

```
\begin{aligned} &\{\text{movieid}\} \to \{\text{runtime}\} \, \{\text{movieid}\} \!\!\to\! \{\text{runtime}\} \\ &\text{Since } \{\text{movieid}\} \subseteq \text{result} \{\text{movieid}\} \text{result}, \text{ update result:} \end{aligned}
```

result := {movieid, genreid, genre, isadult, title, runtime}

```
\begin{split} \textbf{FD 8:} \\ &\{ \textbf{movieid}, \textbf{genreid}, \textbf{genre}, \textbf{isadult}, \textbf{title}, \textbf{runtime} \} \\ &\{ \textbf{FD 8:} \\ &\{ \textbf{movieid} \} \rightarrow \{ \textbf{year} \} \{ \textbf{movieid} \} \rightarrow \{ \textbf{year} \} \\ &\text{Since } \{ \textbf{movieid} \} \subseteq \textbf{result} \{ \textbf{movieid} \} \textbf{result}, \textbf{ update result}: \\ &\quad \textbf{result} := \{ \textbf{movieid}, \textbf{genreid}, \textbf{genre}, \textbf{isadult}, \textbf{title}, \textbf{runtime}, \textbf{year} \} \\ &\quad \textbf{result} := \{ \textbf{movieid}, \textbf{genre}, \textbf{isadult}, \textbf{title}, \textbf{runtime}, \textbf{year} \} \end{split}
```

3. **No More Changes**: At this point, applying other FDs does not add new attributes to the result.

final-closure-of-textmovieidtextgenreidmovieidgenreid

 $Final\ Closure\ of\ \{movieid,genreid\}: Final\ Closure\ of\ \\ \\ \{\text{text}\{\text{movieid}\},\\ \\ \text{text}\{\text{genreid}\}: Final\ Closure\ of\ \\ \\ \{\text{text}\{\text{movieid}\},\\ \\ \text{text}\{\text{movieid}\},\\ \\ \text{text}\{\text{movieid}\}: Final\ Closure\ of\ \\ \\ \{\text{text}\{\text{movieid}\},\\ \\ \text{text}\{\text{movieid}\},\\ \\ \text{text}\{\text{movieid}\}: Final\ Closure\ of\ \\ \\ \text{text}\{\text{movieid}\},\\ \\ \text{text}\{\text{movieid}\}: Final\ Closure\ of\ \\ \\ \text{text}\{\text{movieid}\},\\ \\ \text{text}\{\text{movieid}\}: Final\ Closure\ of\ \\ \\ \text{text}\{\text{movieid}\}:$ 

- $\textbf{2. Closure of } \{ \textbf{movieid}, \textbf{genre} \} \} \} \{ \textbf{movieid}, \textbf{genre} \} \} \} \{ \textbf{movieid}, \textbf{genre} \} \} \} \{ \textbf{movieid}, \textbf{genre} \} \} \} \{ \textbf{movieid}, \textbf{genre} \} \} \} \{ \textbf{movieid}, \textbf{genre} \} \} \{ \textbf{movieid}, \textbf{genre} \} \} \} \{ \textbf{movieid}, \textbf{genre} \} \} \} \{ \textbf{movieid}, \textbf{genre} \} \} \{ \textbf{movieid}, \textbf{genre} \} \} \} \} \{ \textbf{movieid}, \textbf{genre} \} \} \} \{ \textbf{movieid}, \textbf{genre} \} \} \} \{ \textbf{movieid}, \textbf{genre} \} \} \} \} \{ \textbf{movieid}, \textbf{genre} \} \} \} \{ \textbf{movieid}, \textbf{genre} \} \} \} \} \{ \textbf{movieid}, \textbf{genre} \} \} \} \{ \textbf{movieid}, \textbf{genre} \} \} \} \{ \textbf{movieid}, \textbf{genre} \} \} \} \} \} \} \} \{ \textbf{movieid}, \textbf{genre} \} \} \} \} \} \{ \textbf$ 
  - 1. Initialize:

$$\label{eq:result} \operatorname{result} := \{\operatorname{movieid}, \operatorname{genre}\}$$
 
$$\operatorname{result} := \{\operatorname{movieid}, \operatorname{genre}\}$$

2. Iterate through FDs:

# **FD 2**:

```
\begin{split} & \{ genre \} \to \{ genreid \} \{ genre \} \! \to \! \{ genreid \} \\ & Since \; \{ genre \} \subseteq result \{ genre \} result, \; update \; result: \end{split}
```

 $result := \{movieid, genre, genreid\}$ 

```
result:={movieid,genre,genreid}
FD 6:
\{genreid\} \rightarrow \{genre\} \{genreid\} \rightarrow \{genre\}
(Already covered, no new updates)
FD 3:
\{\text{movieid}\} \rightarrow \{\text{isadult}\} \{\text{movieid}\} \rightarrow \{\text{isadult}\}
Since \{\text{movieid}\}\subseteq \text{result}\{\text{movieid}\}\result, update result:
                              result := \{movieid, genre, genreid, isadult\}
result:={movieid,genre,genreid,isadult}
FD 4:
\{\text{movieid}\} \rightarrow \{\text{title}\} \{\text{movieid}\} \rightarrow \{\text{title}\}
Since \{\text{movieid}\}\subseteq \text{result}\{\text{movieid}\}\result, update result:
                          result := {movieid, genre, genreid, isadult, title}
result:={movieid,genre,genreid,isadult,title}
FD 5:
\{\text{movieid}\} \rightarrow \{\text{runtime}\} \{\text{movieid}\} \rightarrow \{\text{runtime}\}
Since \{\text{movieid}\}\subseteq \text{result}\{\text{movieid}\}\result, update result:
                   result := {movieid, genre, genreid, isadult, title, runtime}
result:={movieid,genre,genreid,isadult,title,runtime}
FD 8:
\{\text{movieid}\} \rightarrow \{\text{year}\} \{\text{movieid}\} \rightarrow \{\text{year}\}
Since \{\text{movieid}\}\subseteq \text{result}\{\text{movieid}\}\result, update result:
                result := {movieid, genre, genreid, isadult, title, runtime, year}
result:={movieid,genre,genreid,isadult,title,runtime,year}
```

3. No More Changes: At this point, applying other FDs does not add new attributes to the result.

final-closure-of-textmovieidtextgenremovieidgenre

 $Final\ Closure\ of\ \{movieid,genre\}: Final\ Closure\ of\ \\ \\ \{\text{text}\{movieid\},\\ \\ \\ \text{text}\{genre\}: Final\ Closure\ of\ \\ \\ \\ \\ \text{text}\{movieid\},\\ \\ \text{text}\{genre\}: Final\ Closure\ of\ \\ \\ \\ \text{text}\{movieid\},\\ \\ \text{text}\{genre\}: Final\ Closure\ of\ \\ \\ \text{text}\{movieid\},\\ \\ \text{text}\{genre\}: Final\ Closure\ of\ \\ \\ \text{text}\{ge$ 

- 3. Closure of {movieid, runtime}{movieid, runtime}:3. Closure of \{\text{movieid}, \text{runtime} step-by-step-process-2
  - 1. Initialize:

```
\label{eq:result} \operatorname{result} := \{\operatorname{movieid}, \operatorname{runtime}\} \operatorname{result} := \{\operatorname{movieid}, \operatorname{runtime}\}
```

2. Iterate through FDs:

```
FD 3:
```

```
\begin{aligned} &\{\text{movieid}\} \to \{\text{isadult}\} \{\text{movieid}\} \to \{\text{isadult}\} \\ &\text{Since } \{\text{movieid}\} \subseteq \text{result} \{\text{movieid}\} \text{result}, \text{ update result:} \end{aligned}
```

 $result := \{movieid, runtime, is adult\}$ 

result:={movieid,runtime,isadult}

# FD 4:

```
\{\text{movieid}\} \rightarrow \{\text{title}\} \{\text{movieid}\} \rightarrow \{\text{title}\}
Since \{\text{movieid}\} \subseteq \text{result}\{\text{movieid}\} result, update result:
```

 $result := \{movieid, runtime, is adult, title\}$ 

result:={movieid,runtime,isadult,title}

## FD 8:

```
\begin{aligned} &\{\text{movieid}\} \to \{\text{year}\} \, \{\text{movieid}\} \to \{\text{year}\} \\ &\text{Since } \{\text{movieid}\} \subseteq \text{result} \{\text{movieid}\} \text{result}, \text{ update result} \end{aligned}
```

 $result := \{movieid, runtime, is adult, title, year\}$ 

result:={movieid,runtime,isadult,title,year}

3. **No More Changes**: At this point, applying other FDs does not add new attributes to the result.

final-closure-of-textmovieidtextruntimemovieidruntime

 $Final\ Closure\ of\ \{movieid, runtime\} : Final\ Closure\ of\ \\ \{\ text\{movieid\}, \ text{text}\}$ 

```
\{movieid, runtime\}^+ = \{movieid, runtime, is adult, title, year\} \{movieid, runtime\} + = \{movieid, runtime, is adult, title, year\}
```

- ${\bf closure\hbox{-}of\hbox{-}text movie id text title movie id title}$
- 4. Closure of  $\{\text{movieid}, \text{title}\}$  {movieid, title}:4. Closure of  $\{\text{title}\}$ ,  $\{\text{title}\}$  {movieid} step-by-step-process-3
  - 1. Initialize:

$$\label{eq:result} \begin{aligned} \text{result} &:= \{\text{movieid}, \text{title}\} \\ \text{result} &:= \{\text{movieid}, \text{title}\} \end{aligned}$$

2. Iterate through FDs:

```
FD 3:
```

```
\begin{aligned} &\{\text{movieid}\} \rightarrow \{\text{isadult}\} \, \{\text{movieid}\} \rightarrow \{\text{isadult}\} \\ &\text{Since } \{\text{movieid}\} \subseteq \text{result} \{\text{movieid}\} \text{result}, \text{ update result:} \end{aligned}
```

```
result := \{movieid, title, is adult\}
```

result:={movieid,title,isadult}

#### **FD** 5:

```
\begin{aligned} &\{\text{movieid}\} \to \{\text{runtime}\} \, \{\text{movieid}\} \to \{\text{runtime}\} \\ &\text{Since } \{\text{movieid}\} \subseteq \text{result} \{\text{movieid}\} \text{result}, \text{ update result:} \end{aligned}
```

```
result := \{movieid, title, is adult, runtime\}
```

result:={movieid,title,isadult,runtime}

#### FD 8:

```
 \begin{split} \{\text{movieid}\} &\to \{\text{year}\} \, \{\text{movieid}\} \to \{\text{year}\} \\ \text{Since } \{\text{movieid}\} \subseteq \text{result} \{\text{movieid}\} \text{result}, \text{ update result}: \\ & \text{result} := \{\text{movieid}, \text{title}, \text{isadult}, \text{runtime}, \text{year}\} \\ \text{result} := \{\text{movieid}, \text{title}, \text{isadult}, \text{runtime}, \text{year}\} \end{split}
```

3. **No More Changes**: At this point, applying other FDs does not add new attributes to the result.

final-closure-of-textmovieidtexttitlemovieidtitle

# $Final\ Closure\ of\ \{movieid, title\} \{movieid, title\} : Final\ Closure\ of\ \{\ text\{movieid\}, \ text\{title\} \} \} = \{movieid, title\} : Final\ Closure\ of\ \{\ text\{movieid\}, \ text\{title\} \} \} = \{movieid, title\} : Final\ Closure\ of\ \{\ text\{movieid\}, \ text\{title\}, \ text\{titl$

```
\{movieid, title\}^+ = \{movieid, title, is adult, runtime, year\} \{movieid, title\} + = \{movieid, title, is adult, runtime, year\} \underline{\qquad \qquad } summary-of-closures
```

# **Summary of Closures:**

- $1. \ \{movieid, genreid\}^+ = \{movieid, genreid, genre, is adult, title, runtime, year\} \{movieid, genreid\} + = \{mo$
- $2. \ \{movieid, genre\}^+ = \{movieid, genre, genreid, is adult, title, runtime, year\} \{movieid, genre\} + = \{moviei$
- $3. \ \{\text{movieid}, \text{runtime}\}^+ = \{\text{movieid}, \text{runtime}, \text{isadult}, \text{title}, \text{year}\} \{\text{movieid}, \text{runtime}\} + = \{\text{movieid}, \text{runtime}, \text{isadult}, \text{title}, \text{year}\} \{\text{movieid}, \text{runtime}\} + = \{\text{movieid}, \text{runtime}, \text{isadult}, \text{title}, \text{year}\} \{\text{movieid}, \text{runtime}\} + = \{\text{movieid}, \text{runtime}, \text{isadult}, \text{title}, \text{year}\} \{\text{movieid}, \text{runtime}\} + = \{\text{movieid}, \text{runtime}, \text{isadult}, \text{title}, \text{year}\} \{\text{movieid}, \text{runtime}\} + = \{\text{movieid}, \text{runtime}, \text{isadult}, \text{title}, \text{year}\} \{\text{movieid}, \text{runtime}\} + = \{\text{movieid}, \text{runtime}, \text{isadult}, \text{title}, \text{year}\} \{\text{movieid}, \text{runtime}\} + = \{\text{movieid}, \text{runtime}, \text{isadult}, \text{title}, \text{year}\} \{\text{movieid}, \text{runtime}\} + = \{\text{movieid}, \text{runtime}, \text{isadult}, \text{title}, \text{year}\} \{\text{movieid}, \text{runtime}\} + = \{\text{movieid}, \text{runtime}, \text{isadult}, \text{title}, \text{year}\} \{\text{movieid}, \text{runtime}\} + = \{\text{movieid}, \text{runtime}, \text{isadult}, \text{title}, \text{year}\} \{\text{movieid}, \text{runtime}\} + = \{\text{movieid}, \text{runtime}, \text{isadult}, \text{title}, \text{year}\} \} \{\text{movieid}, \text{runtime}\} + = \{\text{movieid}, \text{runtime}, \text{title}, \text{year}\} \} \{\text{movieid}, \text{runtime}\} + = \{\text{movieid}, \text{runtime}, \text{title}, \text{year}\} \} \{\text{movieid}, \text{runtime}\} + = \{\text{movieid}, \text{runtime}, \text{title}, \text{year}\} \} \{\text{movieid}, \text{title}, \text{title},$
- 4.  $\{\text{movieid, title}\}^+ = \{\text{movieid, title, is adult, runtime, year}\} \{\text{movieid, title}\} + = \{\text{movieid, title, is adult, runtime, you-said-4}\}$

use this algorithm completely for closure: Closure of beta under F (beta+) result := beta Do For each gema  $\rightarrow$  delta in F: If (gema result): result := result Union delta While (result does not change) Return result give closure of {movieid, runtime, title}

ChatGPT said:

Let's apply the closure algorithm step by step for the set {movieid, runtime, title} {movieid, runtime, title} under the given set of functional dependencies (FDs).

given-functional-dependencies-fds-2

# Given Functional Dependencies (FDs):

- 1.  $\{\text{genreid}, \text{title}\} \rightarrow \{\text{runtime}\} \{\text{genreid}, \text{title}\} \rightarrow \{\text{runtime}\}$
- 2.  $\{genre\} \rightarrow \{genreid\} \{genre\} \rightarrow \{genreid\}$
- 3.  $\{\text{movieid}\} \rightarrow \{\text{isadult}\} \{\text{movieid}\} \rightarrow \{\text{isadult}\}$
- 4.  $\{\text{movieid}\} \rightarrow \{\text{title}\} \{\text{movieid}\} \rightarrow \{\text{title}\}$
- 5.  $\{\text{movieid}\} \rightarrow \{\text{runtime}\} \{\text{movieid}\} \rightarrow \{\text{runtime}\}$
- 6.  $\{genreid\} \rightarrow \{genre\} \{genreid\} \rightarrow \{genre\}$
- 7.  $\{\text{runtime}, \text{title}\} \rightarrow \{\text{year}\} \{\text{runtime}, \text{title}\} \rightarrow \{\text{year}\}$
- 8.  $\{\text{movieid}\} \rightarrow \{\text{year}\} \{\text{movieid}\} \rightarrow \{\text{year}\}$
- 9.  $\{genre, title\} \rightarrow \{runtime\} \{genre, title\} \rightarrow \{runtime\}$
- 10.  $\{\text{title}\} \rightarrow \{\text{isadult}\} \{\text{title}\} \rightarrow \{\text{isadult}\}$ step-by-step-process-4

# Step-by-Step Process:

step-1-initialize

$$result := \{movieid, runtime, title\}$$

result:={movieid,runtime,title} step-2-apply-functional-dependencies-iteratively

1. **FD 3**:  $\{\text{movieid}\} \rightarrow \{\text{isadult}\} \{\text{movieid}\} \rightarrow \{\text{isadult}\}$  $\{\text{movieid}\} \subseteq \text{result}\{\text{movieid}\} \text{result}, \text{so:}$ 

$$result := \{movieid, runtime, title, is adult\}$$
 
$$result := \{movieid, runtime, title, is adult\}$$

2. **FD 4**:  $\{\text{movieid}\} \rightarrow \{\text{title}\} \{\text{movieid}\} \rightarrow \{\text{title}\}$  (Already in resultresult, no change)

- 3. **FD 5**:  $\{\text{movieid}\} \rightarrow \{\text{runtime}\} \{\text{movieid}\} \rightarrow \{\text{runtime}\}$  (Already in resultresult, no change)
- 4. **FD 7**: {runtime, title}  $\rightarrow$  {year} {runtime, title}  $\rightarrow$  {year} {runtime, title}  $\subseteq$  result{runtime, title} result, so:

result := {movieid, runtime, title, isadult, year}

result:={movieid,runtime,title,isadult,year}

- 5. **FD 8**:  $\{\text{movieid}\} \rightarrow \{\text{year}\} \{\text{movieid}\} \rightarrow \{\text{year}\}$  (Already in resultresult, no change)
- 6. **FD 10**:  $\{\text{title}\} \rightarrow \{\text{isadult}\} \{\text{title}\} \rightarrow \{\text{isadult}\}$  (Already in resultresult, no change)

step-3-no-more-changes

At this point, no other functional dependency adds new attributes to the result. final-closure-of-textmovieidtextruntimetexttitlemovieidruntimetitle

Final Closure of {movieid, runtime, title}{movieid, runtime, title}:Final Closure of \{\text{movieid},\text{runtime},\text{title}\}{movieid, runtime, title}:

 $\{\text{movieid}, \text{runtime}, \text{title}\}^+ = \{\text{movieid}, \text{runtime}, \text{title}, \text{isadult}, \text{year}\}$ 

{movieid,runtime,title}+={movieid,runtime,title,isadult,year}

This is the closure of the set {movieid, runtime, title}{movieid, runtime, title}. you-said-5

So the candidate keys are the ones whose closure contained all the attributes. Here the candidate keys are {genre, movieid}, {genreid, movieid}

2/2

ChatGPT said:

Yes, you're correct! The candidate keys are those attribute sets whose closure contains all the attributes of the relation. In this case, the closure of both {genre, movieid} {genreid, movieid} {genreid, movieid} includes all the attributes of the relation:

attributes-in-the-relation

#### Attributes in the relation:

```
{genreid, genre, runtime, title, movieid, isadult, year}
{genreid,genre,runtime,title,movieid,isadult,year}
lets-check-the-closures
Let's check the closures:
```

# 1. Closure of {genre, movieid}{genre, movieid}:

• Using the closure algorithm, the closure of {genre, movieid} {genre, movieid} results in all the attributes:

```
 \{genre, movieid\}^+ = \{genre, movieid, genreid, is adult, title, runtime, year\} \\ \{genre, movieid\} += \{genre, movieid, genreid, is adult, title, runtime, year\}
```

# 2. Closure of {genreid, movieid}{genreid, movieid}:

• Similarly, the closure of {genreid, movieid}{genreid, movieid} also results in all the attributes:

```
 \{genreid, movieid\}^+ = \{genreid, movieid, genre, is adult, title, runtime, year\}   \{genreid, movieid\} + = \{genreid, movieid, genre, is adult, title, runtime, year\}  therefore-the-candidate-keys-are
```

## Therefore, the candidate keys are:

```
\{genre, movieid\}, \{genreid, movieid\}
```

{genre,movieid},{genreid,movieid}

These are the minimal sets of attributes whose closures contain all the attributes of the relation, making them the candidate keys.

You've hit the Free plan limit for GPT-4o.

Responses will use another model until your limit resets after 11:08 PM.

Get Plus prompt-textarea composer-background